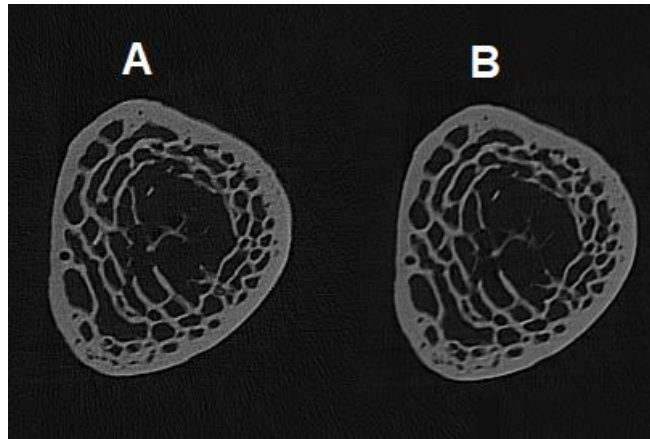
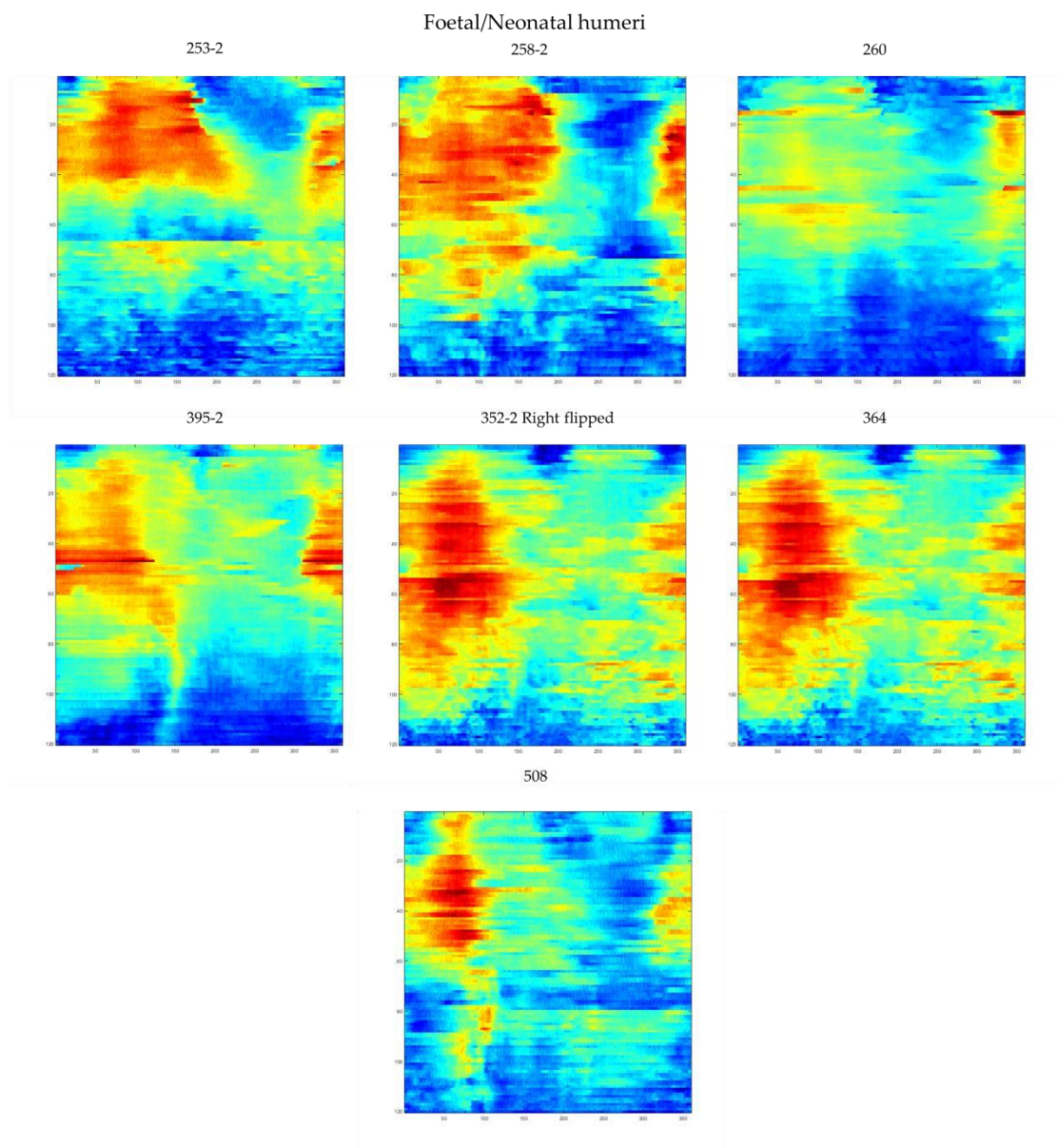


## 1.1 S1. Example of downsampling



Effects of downsampling. A: Original resolution slice, B: Downsampled slice. As downsampling was in the Z plane, the downsampling had little effect on X-Y resolution.

1    1.2    *S2. Cortical thickness maps for all specimens*



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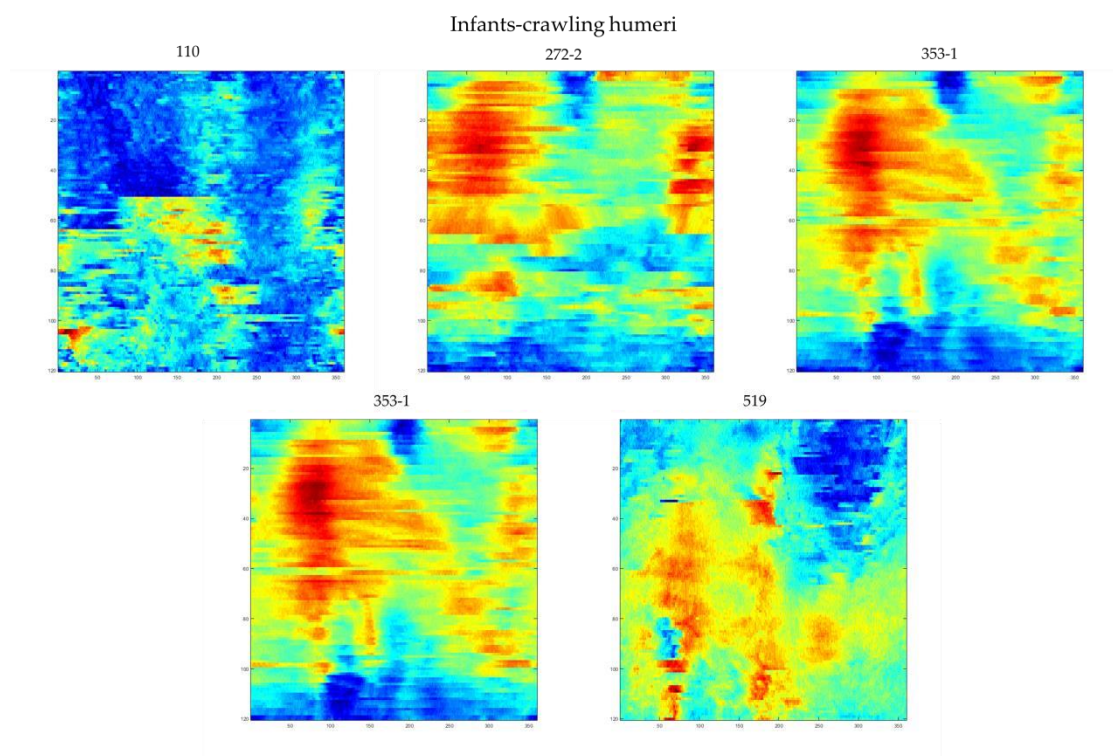
7

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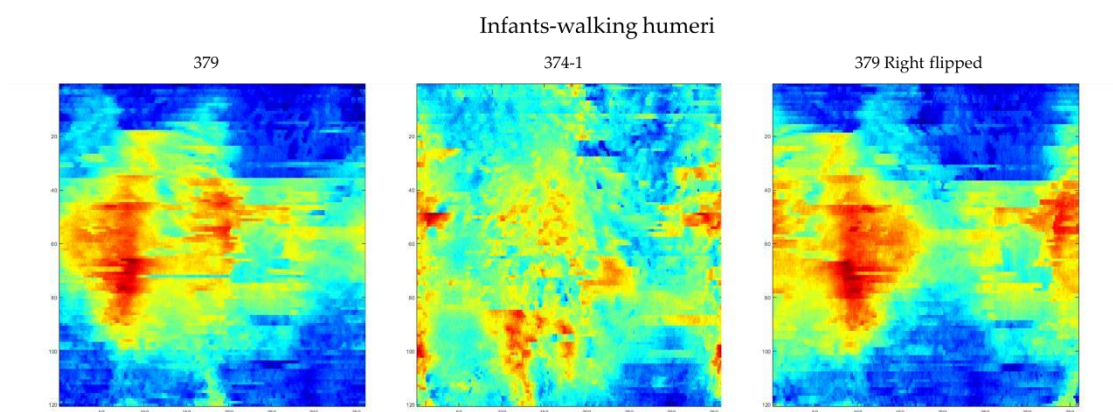
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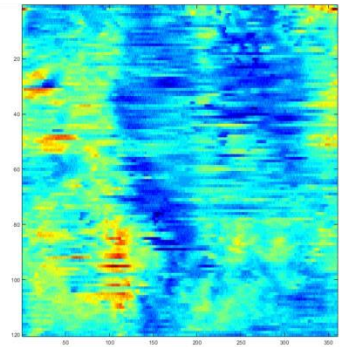
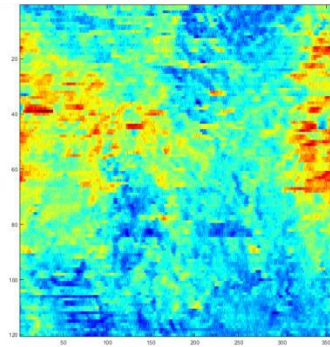
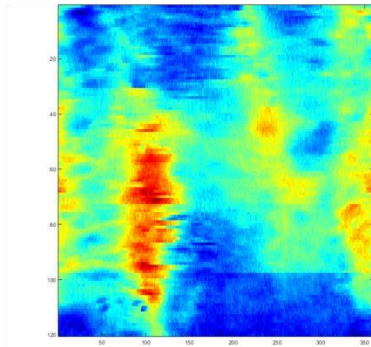


Younger child humeri

1

101 Right flipped

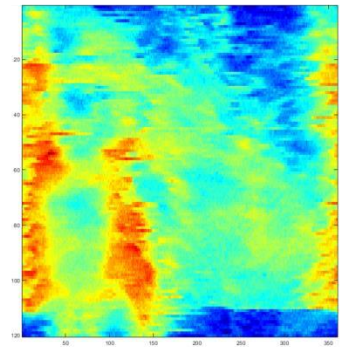
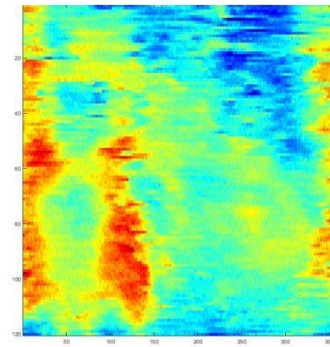
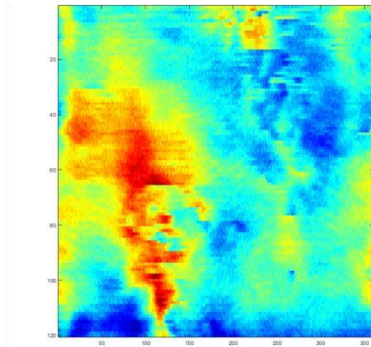
227 Right flipped



231 Right flipped

278-1

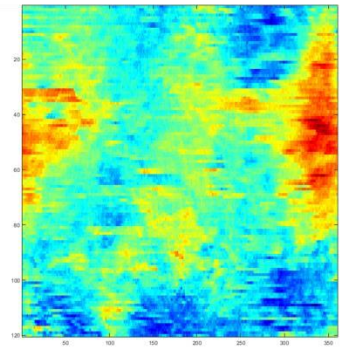
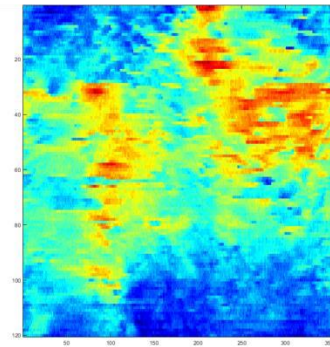
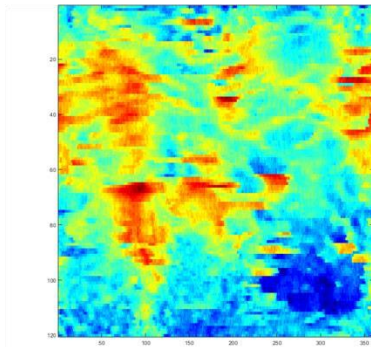
278-2



357-2 Right

361

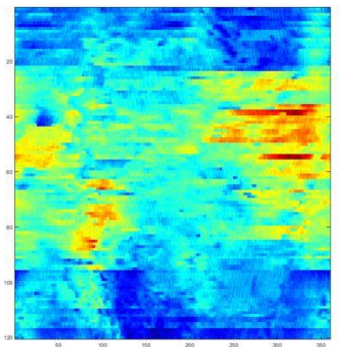
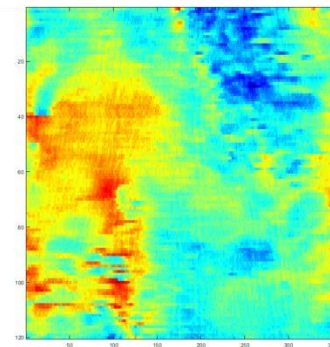
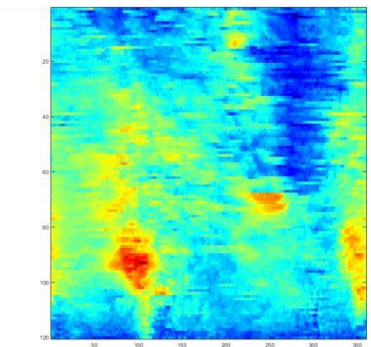
372



39

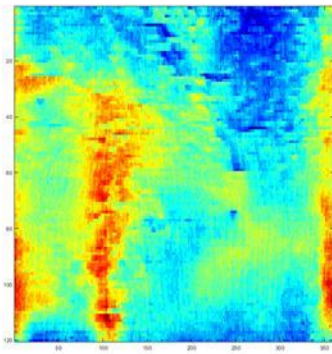
48

438

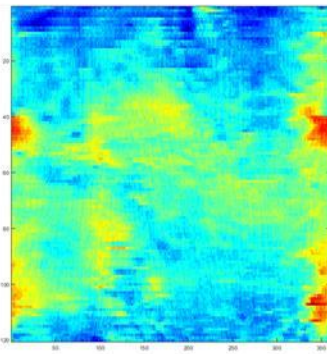


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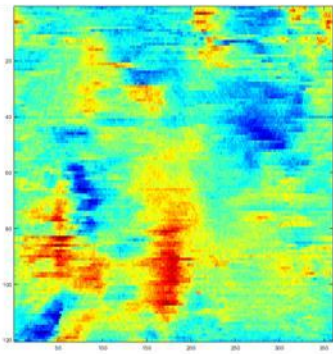
477-2



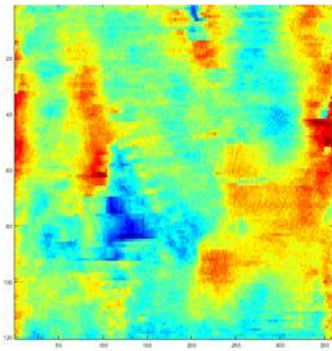
486



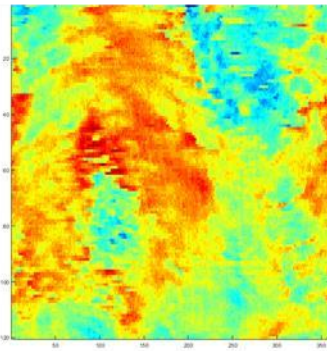
510-2



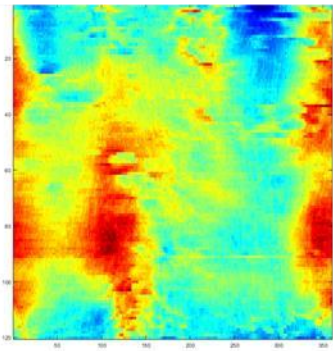
546-1



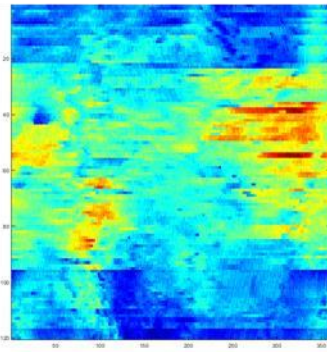
574 Right flipped



584



431



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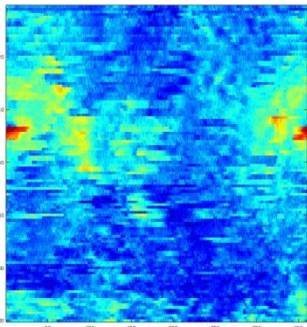
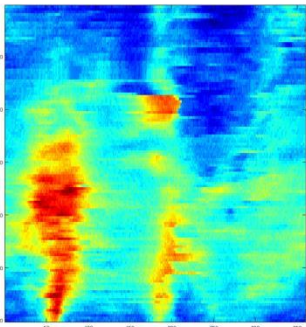
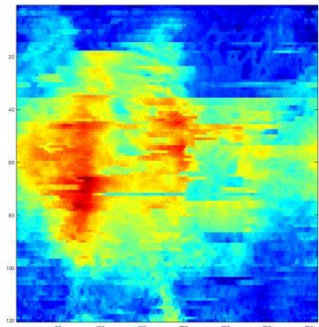


Older child humeri

379

135 Right flipped

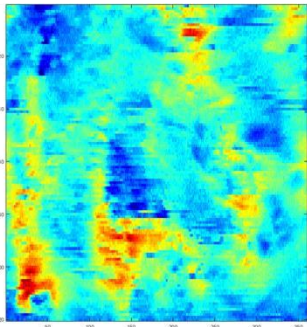
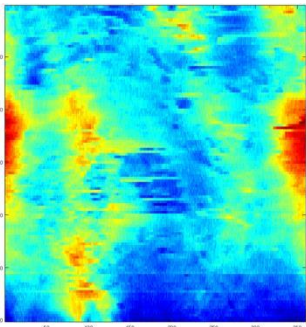
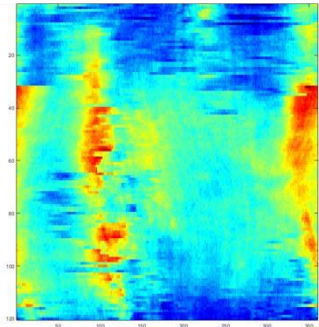
171



247 Right flipped

311

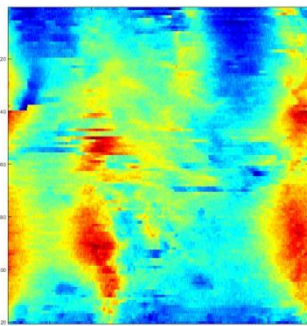
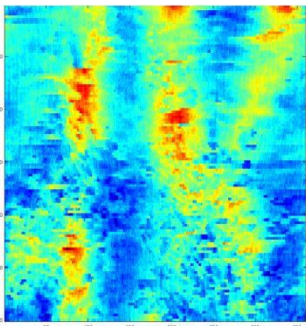
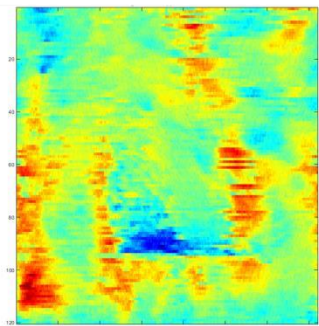
383



383 Right flipped

399 Right flipped

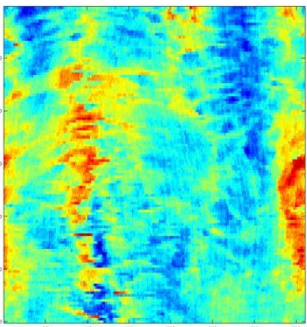
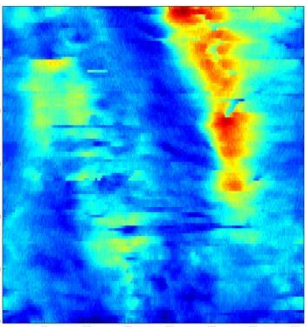
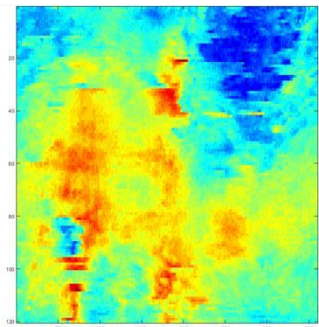
509-1 Right flipped



551-2

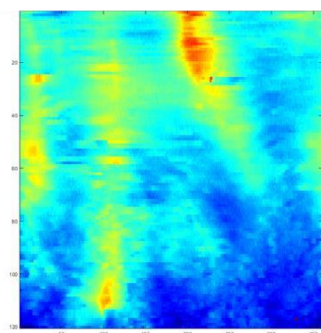
568

575 Right flipped

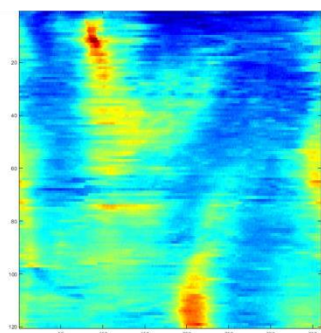


# Adolescent humeri

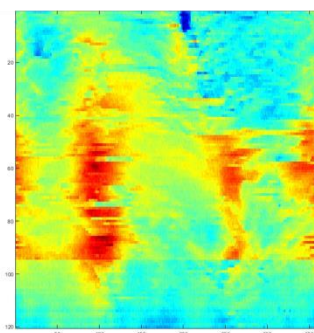
Z4



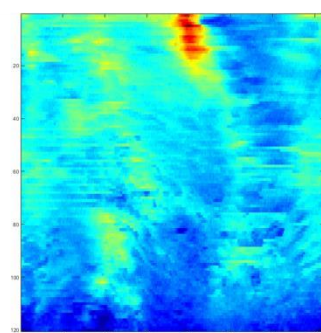
Z1



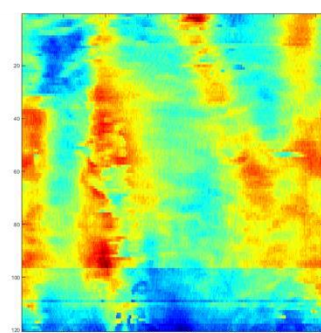
Z2



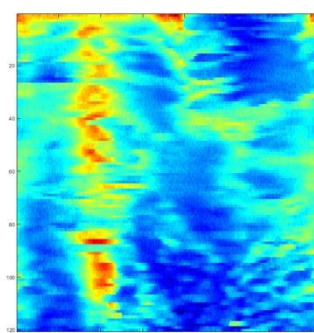
Z3



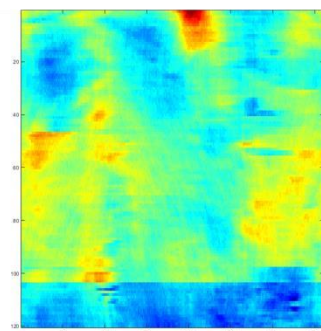
96



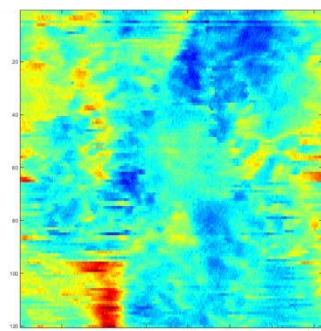
187 R flipped



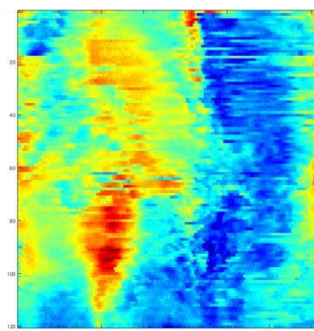
570



573



573 R flipped



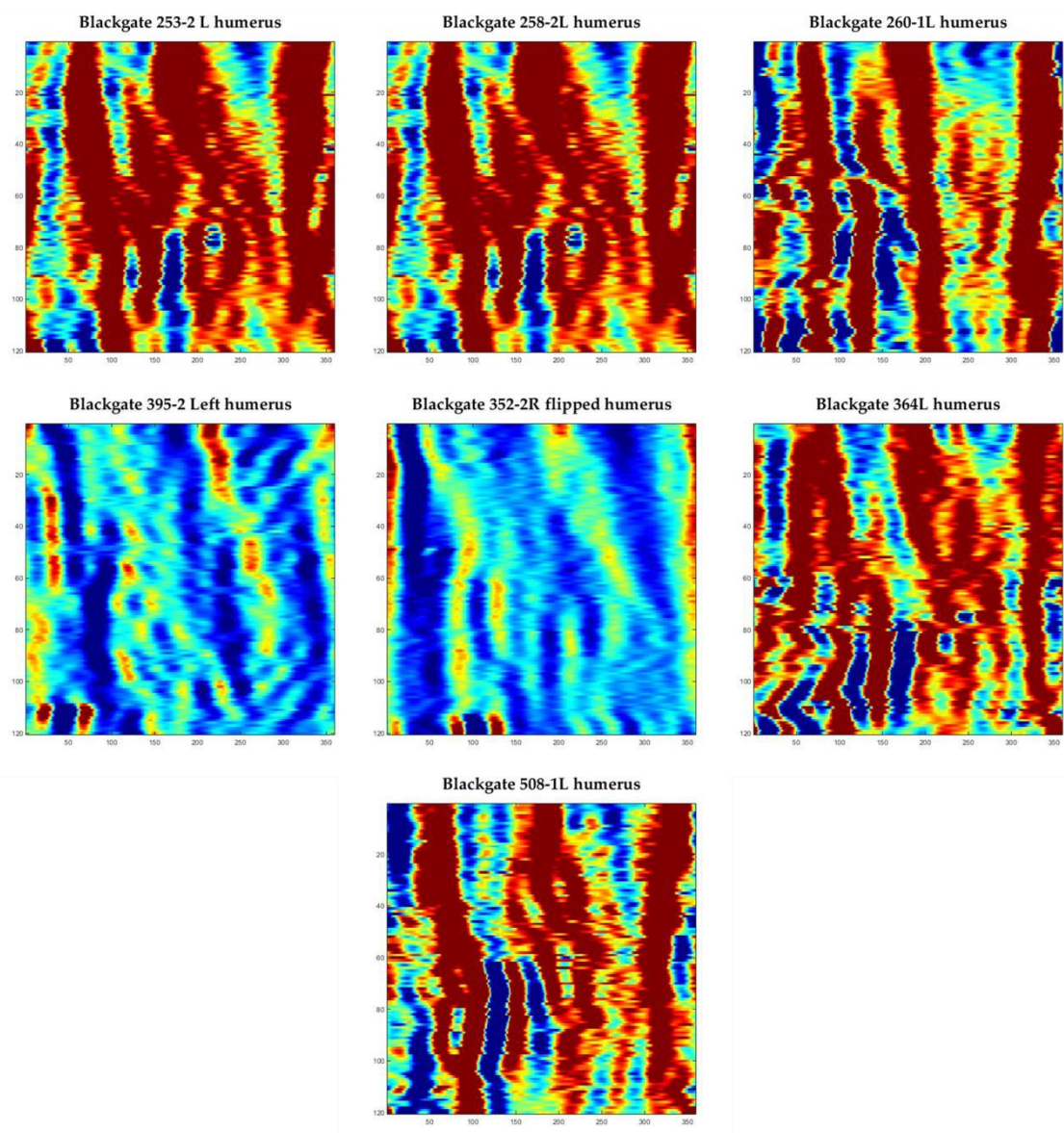
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1

2    1.3    *S3. Periosteal curvature maps for all specimens*

Foetal/neonatal humeri

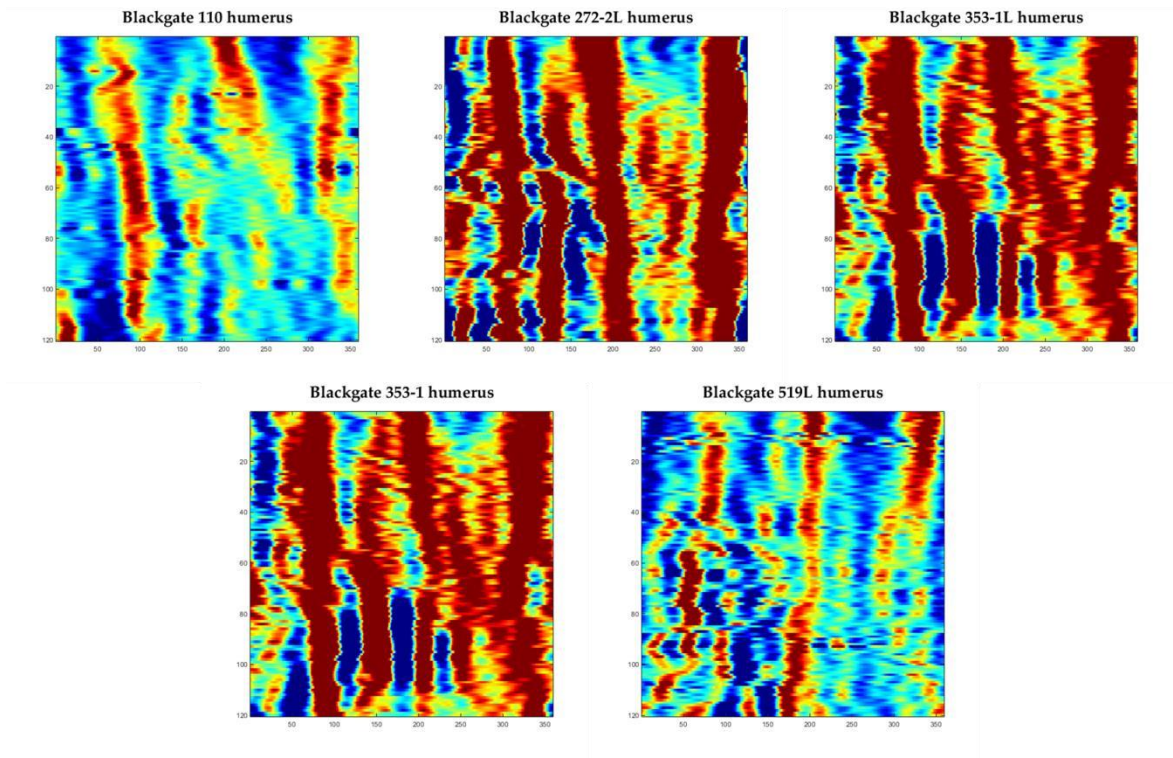


3

4

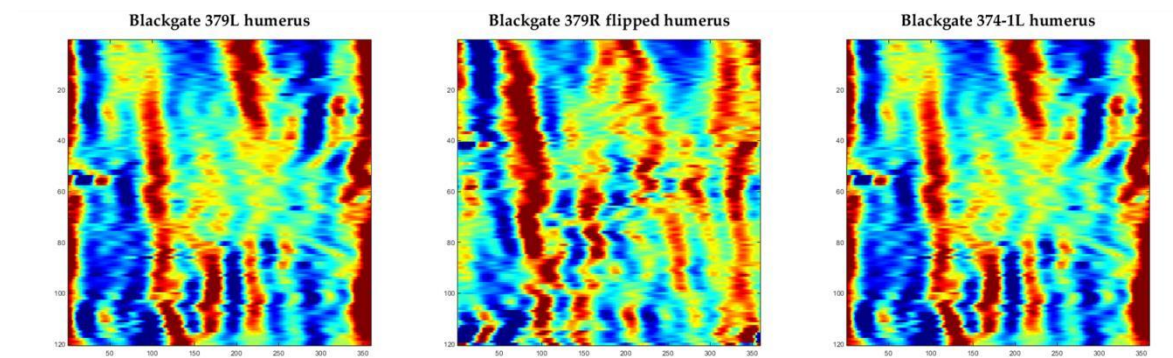


## Infant-crawling humeri



1

## Infant-walking humeri



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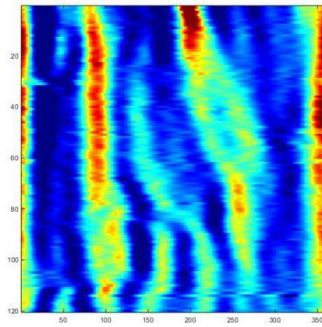
3

4

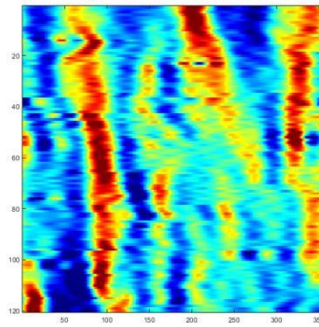
5

## Young child humeri

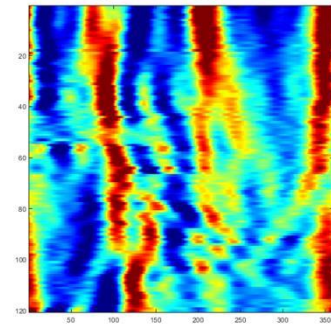
Blackgate 1L humerus



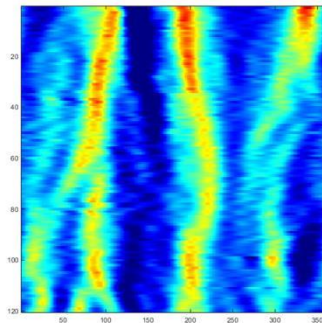
Blackgate 101-1R flipped humerus



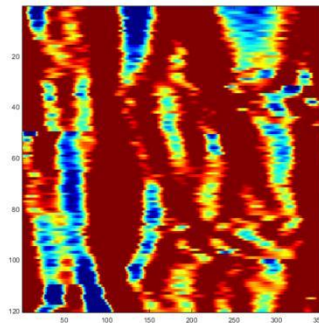
Blackgate 227R Flipped humerus



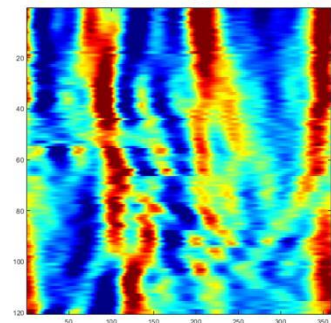
Blackgate 39L humerus



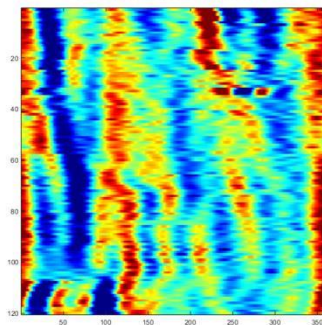
Blackgate 48-1L humerus



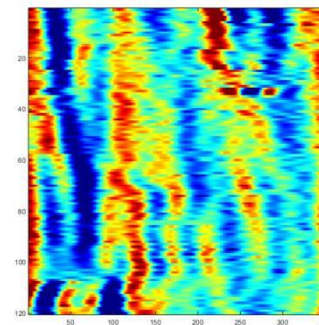
Blackgate 231R flipped humerus



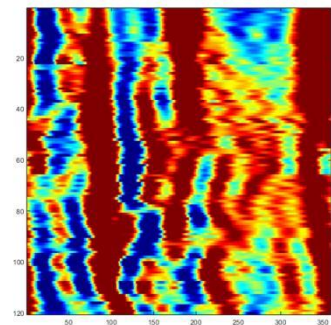
Blackgate 278-1L humerus



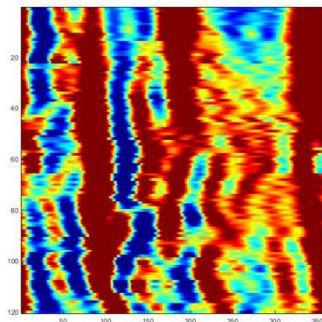
Blackgate 278-2L humerus



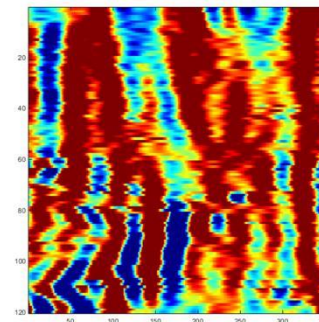
Blackgate 357-2R flipped humerus



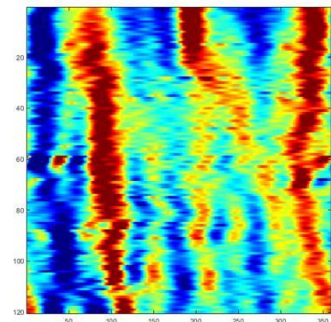
Blackgate 361L humerus



Blackgate 372L humerus



Blackgate 431L humerus



1

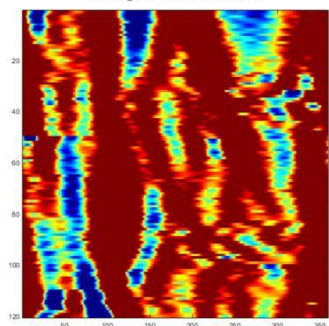
2

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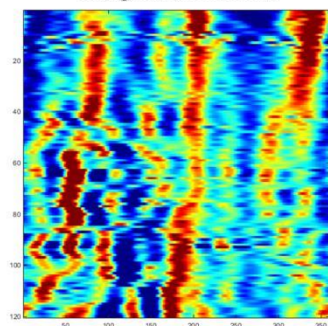


1

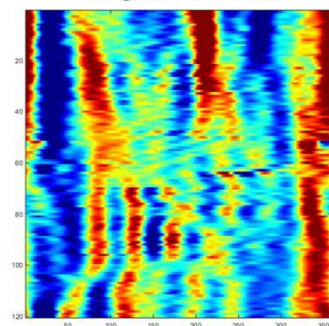
Blackgate 486L humerus



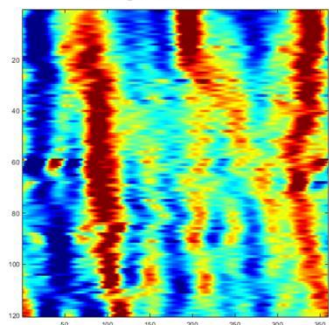
Blackgate 510-2L humerus



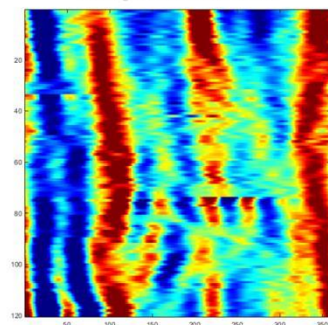
Blackgate 546-1L humerus



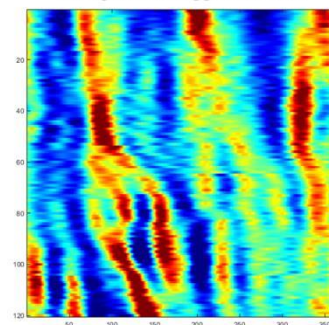
Blackgate 438L humerus



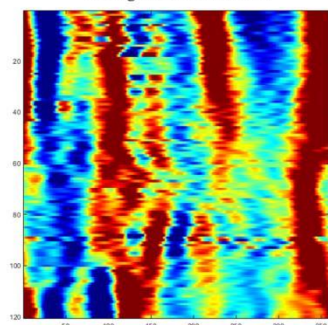
Blackgate 477-2L humerus



Blackgate 574R flipped humerus



Blackgate 584L humerus



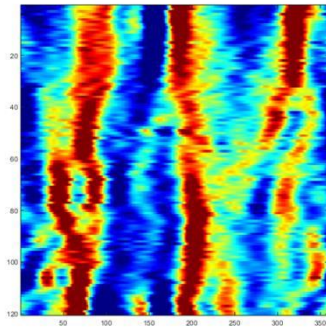
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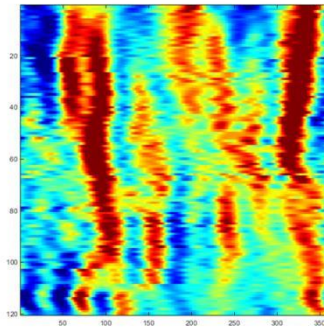
4

## Older child humeri

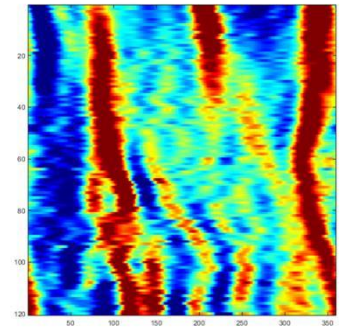
Blackgate 135R flipped humerus



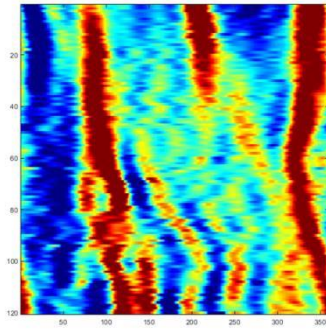
Blackgate 171L humerus



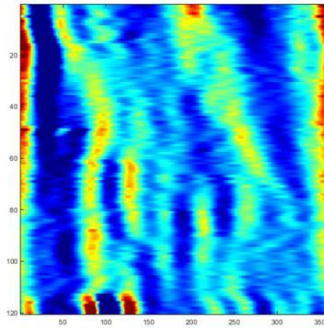
**Blackgate 242 L mirrored humerus**



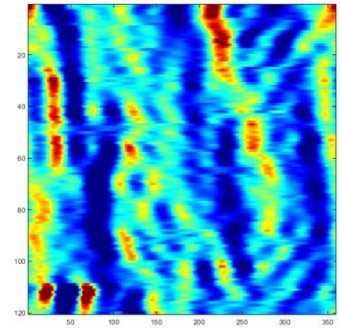
### Blackgate 247 flipped humerus



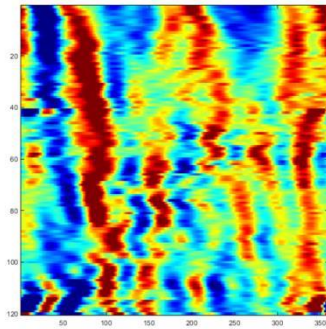
### Blackgate 311L humerus



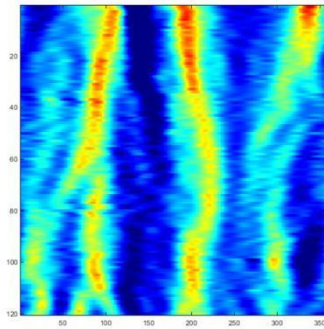
Blackgate 383L humerus



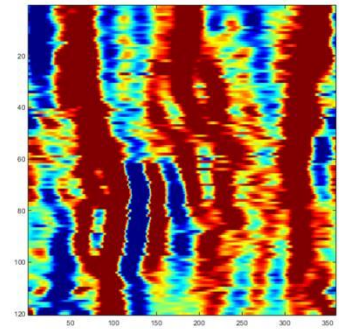
Blackgate 383-R flipped humerus



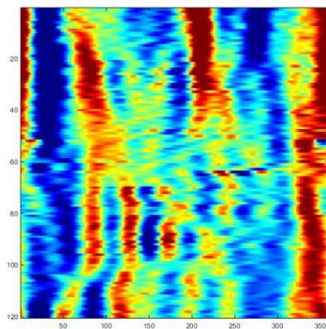
**Blackgate 399R flipped humerus**



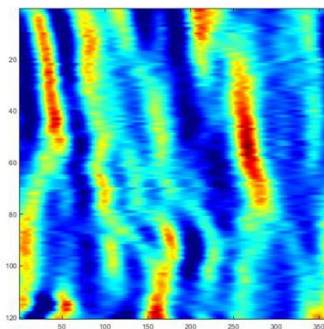
Blackgate 509-1R flipped humerus



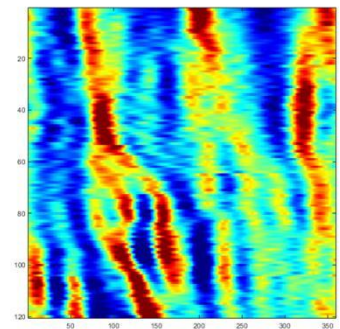
Blackgate 551-2L humerus



### Blackgate 568L humerus



Blackgate 575 flipped humerus

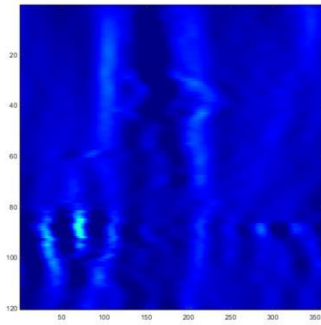


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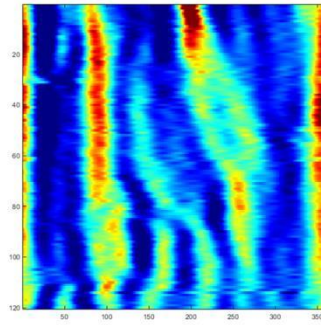


## Adolescent humeri

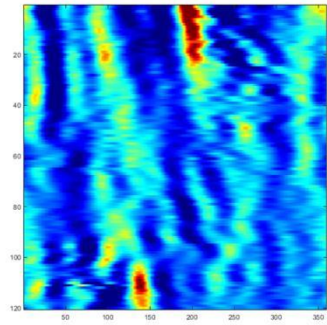
BGZ1 humerus



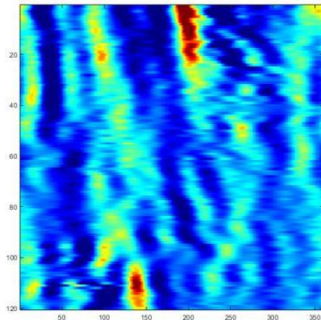
BGZ2 humerus



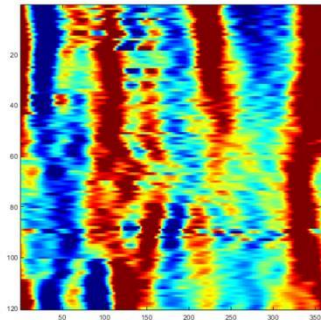
Blackgate Z3 humerus



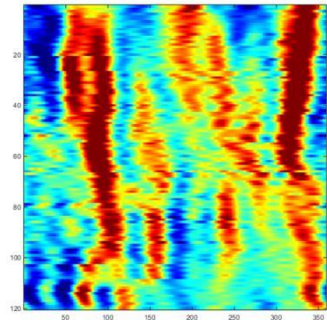
Blackgate Z4 humerus



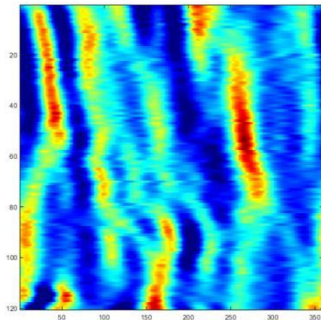
Blackgate 96L humerus



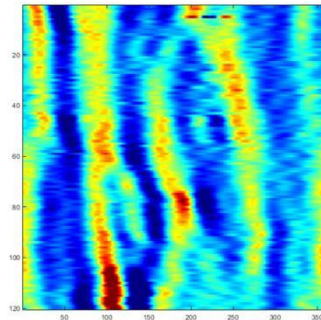
Blackgate 187R flipped humerus



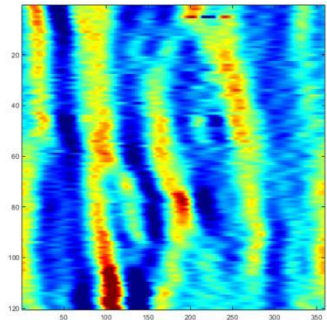
Blackgate 570L humerus



Blackgate 573L humerus



Blackgate 573R flipped humerus



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# 1 1.4 S4 specimen age estimates and scan parameters

Specimen no.	Age group	new group	Age Estimate*	Original voxel size	No. of slices	Source to object	Source to detector	Resliced Z res. /mm	Length/mm
1	Young	Young		0.086	201	524.4	1198.	0.86640	
	Child	Child	5-6	038	4	794	746	2	173.3
39	Young			0.069	172	426.8	1227.	0.59898	
	Child	Infant	1.5-2.5	528	3	844	944	6	119.8
48	Young	Young		0.069	159	426.8	1227.		
	Child	Child	5-6	528	0	844	944	0.55275	110.5
48	Young	Young		0.069	159	426.8	1227.		
	Child	Child	5-6	528	0	844	944	0.55275	110.5
96	Adolescent	Adolescent	12-15	0.057	146	289.1	1007.	0.41959	
				4	2	936	005	4	83.9
96	Adolescent	Adolescent	12-15	0.057	146	289.1	1007.	0.41959	
				4	2	936	005	4	83.9
101	Young			0.069	166	426.8	1227.	0.57882	
	Child	Infant	1-1.5	528	5	844	944	3	115.8
				0.067	141	356.9	1061.	0.47614	
110	Infant	Infant	0.5-1.5	3	5	686	448	8	95.2
	Older	Older		0.097	168	591.4	1217.	0.82001	
135	Child	Child	6-8	158	8	458	49	5	164.0
	Young	Young		0.086	190	507.0	1178.	0.81951	
141	Child	Child	4.5-5.5	038	5	948	77	1	163.9
				0.108	126	703.7	1296.	0.68907	
171	Infant	Infant	0.5-1	602	9	958	104	8	137.8
				0.108	126	703.7	1296.	0.68527	
171	Infant	Infant	0.5-1	602	2	958	104	7	137.1
	Adolescent	Adolescent		0.108	200	703.7	1296.	1.08873	
187	t	t	10-12	602	5	958	104	3	217.7
	Young	Young		0.080	163	478.9	1186.	0.65896	
227	Child	Child	2.5-3.5	756	2	878	264	7	131.8
	Young	Young		0.080	163	478.9	1186.	0.65896	
227	Child	Child	2.5-3.5	756	2	878	264	7	131.8
	Young	Young		0.086	182	507.0	1178.	0.78595	
231	Child	Child	4.5-5.5	038	7	945	771	6	157.2
	Older	Older		0.097	172	591.4	1217.	0.83653	
247	Child	Child	8-9	158	2	458	49	2	167.3
			36-38						
253	Foetal/Neonate	Foetal/Neonate	weeks	0.097	172	591.4	1217.	0.83653	
			l.u	158	2	458	49	2	167.3
			36-38						
258	Foetal/Neonate	Foetal/Neonate	weeks	0.057	131	289.1	1007.	0.37654	
			l.u	4	2	936	005	4	75.3
			36-38						
258	Foetal/Neonate	Foetal/Neonate	weeks	0.057	131	289.1	1007.	0.37654	
			l.u	4	2	936	005	4	75.3
260	Foetal/Neonate	Foetal/Neonate	1-1.25 MO	0.057	131	289.1	1007.	0.37654	
				4	2	936	005	4	75.3



	Foetal/Ne		3-6	0.051	135	261.6	1007.	0.35071	
272	onate	Infant	MO	958	0	095	003	7	70.1
	Young	Young		0.086	188	507.0	1178.	0.80918	
278	Child	Child	5-6	038	1	945	771	6	161.8
	Young	Young		0.086	188	507.0	1178.	0.80918	
278	Child	Child	5-6	038	1	945	771	6	161.8
	Older	Older	9.5-	0.108	210	703.7	1296.	1.14303	
311	Child	Child	12.5	602	5	958	104	4	228.6
			32-34						
	Foetal/Ne	Foetal/Ne	weeks	0.038	134	194.0	1007.	0.25843	
352	onate	onate	l.u	4	6	1	005	2	51.7
	Foetal/Ne		3-6	0.057	143	289.1	1007.	0.41299	
353	onate	Infant	MO	4	9	936	005	3	82.6
	Foetal/Ne		3-6	0.057	143	289.1	1007.	0.41299	
353	onate	Infant	MO	4	9	936	005	3	82.6
	Foetal/Ne	Foetal/Ne	0-1	0.044	146	228.4	1034.	0.32422	
357	onate	onate	MO	172	8	256	253	3	64.8
	Young	Young		0.080	156	478.9	1186.	0.62989	
361	Child	Child	2.5-3.5	756	0	878	264	4	126.0
	Foetal/Ne	Foetal/Ne	0-2	0.044	160	228.4	1034.	0.35403	
364	onate	onate	MO	172	3	256	253	9	70.8
	Young			0.064	171	359.8	1123.	0.54779	
372	Child	Infant	1-1.5	069	0	926	446	3	109.6
		Foetal/Ne	0-1	0.086	170	507.0	1178.	0.73175	
374	Infant	onate	MO	038	1	948	77	3	146.4
		Foetal/Ne	0-1	0.086	170	507.0	1178.	0.73175	
374	Infant	onate	month	038	1	948	77	3	146.4
			6-9	0.069	135	426.8	1227.	0.46966	
379	Infant	Infant	MO	528	1	844	944	4	93.9
	Older	Older		0.108	198	703.7	1296.	1.07841	
383	Child	Child	8.5-9.5	602	6	958	104	6	215.7
	Older	Older		0.108	198	703.7	1296.	1.07841	
383	Child	Child	8.5-9.5	602	6	958	104	6	215.7
	Older	Older		0.108	169	703.7	1296.	0.91768	
384	Child	Child	7-8	602	0	982	102	9	183.5
	Young	Young		0.086	177	507.0	1178.	0.76530	
388	Child	Child	4-5	038	9	945	771	7	153.1
	Foetal/Ne	Foetal/Ne	0-1	0.044	151	228.4	1034.	0.33394	
395	onate	onate	MO	172	2	256	253	1	66.8
	Older	Older		0.108	213	703.7	1296.	1.15715	
399	Child	Child	11-12	602	1	958	104	2	231.4
	Young			0.080	143	478.9	1186.	0.57901	
406	Child	Infant	1.5-2.5	756	4	878	264	8	115.8
	Young	Young		0.080	156	478.9	1186.	0.63231	
431	Child	Child	5-6	756	6	878	264	7	126.5
	Young	Young		0.064	166	359.8	1123.	0.53465	
438	Child	Child	5-6	069	9	926	446	9	106.9
	Young	Young		0.064	166	359.8	1123.	0.53465	
477	Child	Child	3.5-4.5	069	9	926	446	9	106.9
	Young			0.069	157	426.8	1227.	0.54649	
478	Child	Infant	1-2	528	2	844	944	3	109.3

	Young			0.080	155	478.9	1186.	0.62585	
486	Child	Infant	1.5-2.5	756	0	878	264	7	125.2
	Foetal/Ne	Foetal/Ne	0-2	0.051	131	261.6	1007.	0.34214	
508	onate	onate	MO	958	7	095	003	4	68.4
	Older	Older		0.108	162	703.7	1296.	1.84135	
509	Child	Child	5.5-6.5	602	9	982	102	1	176.9
	Young	Young		0.108	172	703.7	1296.	0.93669	
510	Child	Child	5-6	602	5	982	102	4	187.3
			1-3	0.051	138	261.6	1007.	0.36058	
519	Infant	Infant	MO	958	8	095	003	9	72.1
	Young	Young		0.108	161	703.7	1296.	0.87479	
546	Child	Child	4.5-5.5	602	1	982	102	1	175.0
	Young	Young		0.108	161	703.7	1296.	0.87479	
546	Child	Child	4.5-5.5	602	1	982	102	1	175.0
		Young		0.108	161	703.7	1296.	0.87479	
551	Infant	Child	3.5-4.5	602	1	982	102	1	175.0
	Adolescen	Older	9-11	0.108	211	703.7	1296.	1.14629	
568	t	Child	years	602	1	958	104	2	229.3
	Adolescen	Adolescen		0.108	211	703.7	1296.	1.14629	
570	t	t	15-17	602	1	958	104	2	229.3
	Adolescen	Adolescen		0.108	211	703.7	1296.	1.14629	
573	t	t	15-17	602	1	958	104	2	229.3
	Adolescen	Adolescen		0.108	211	703.7	1296.	1.14629	
573	t	t	15-17	602	1	958	104	2	229.3
	Young	Young		0.108	155	703.7	1296.	0.84275	
574	Child	Child	5-6	602	2	982	102	3	168.6
	Older	Older		0.108	175	703.7	1296.	0.95352	
575	Child	Child	11-12	602	6	982	102	8	190.7
	Young	Young	2-3	0.080	153	478.9	1186.	0.61778	
584	Child	Child	years	756	0	878	264	1	123.6

1

2 \*Unless otherwise stated-age is in years

1 1.5 *Supplementary figures S5-S7.*

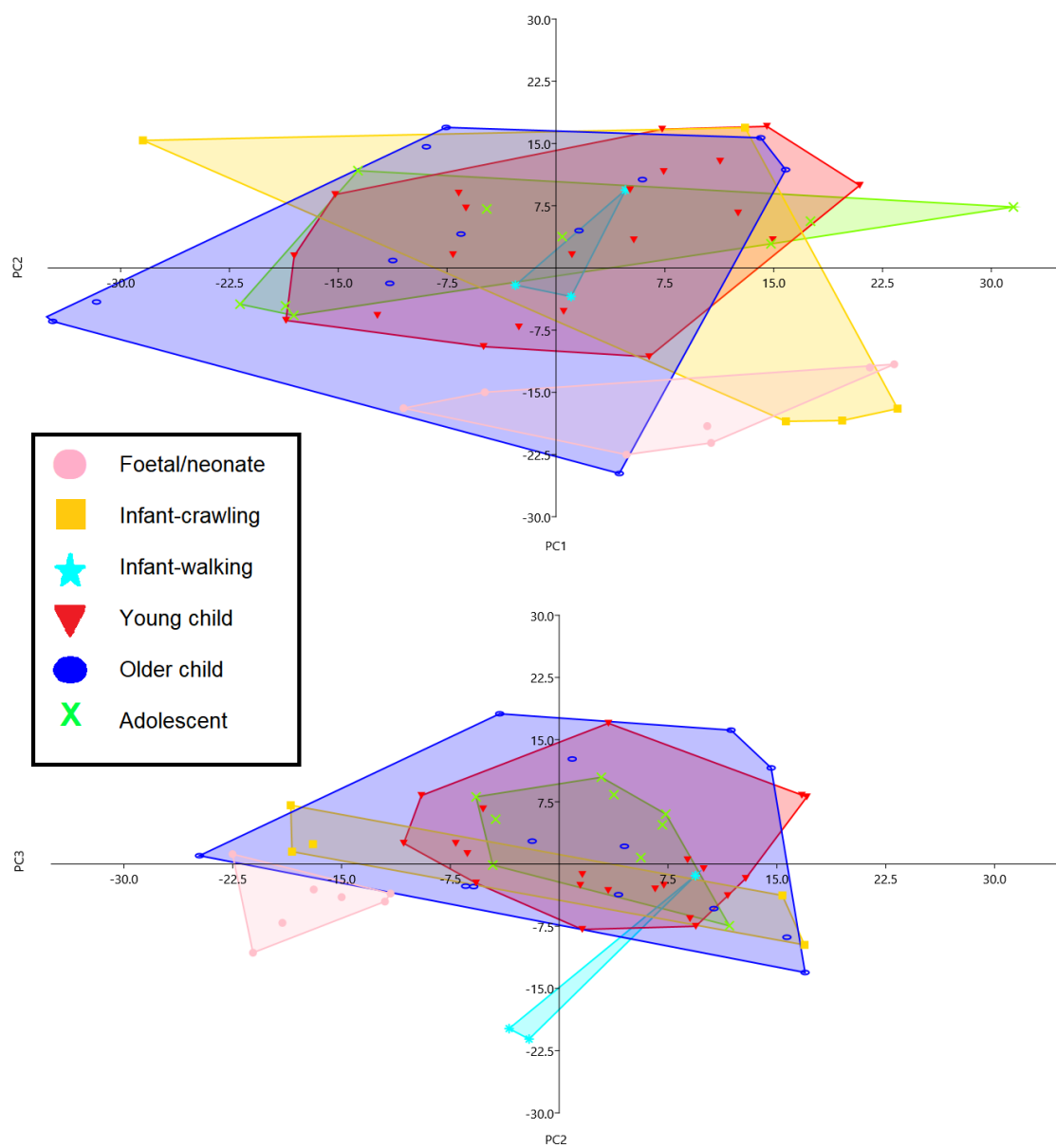
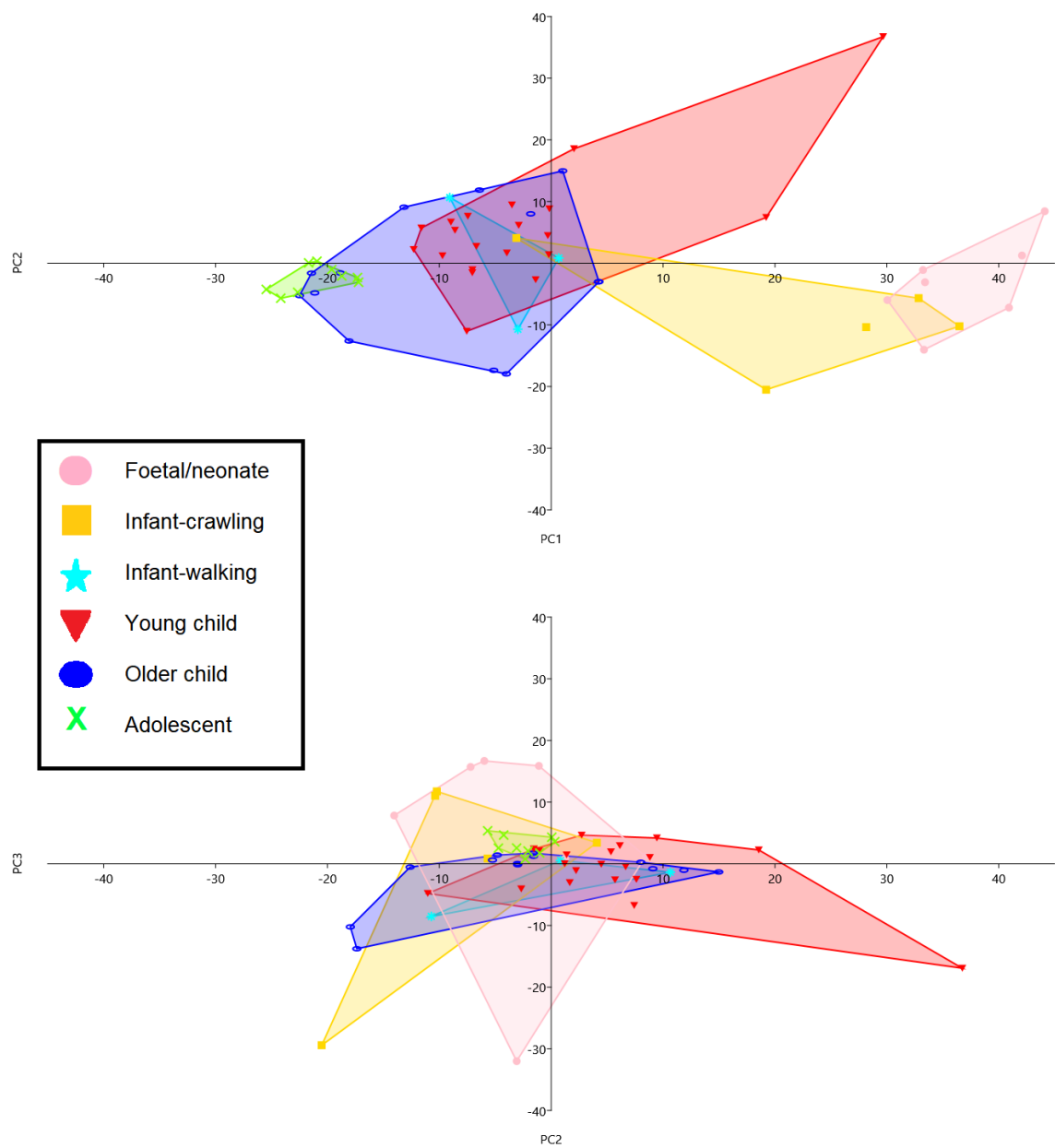


Figure S5. PCA of thickness scores

2  
3  
4





*Figure S6. PCA of periosteal curvature scores*

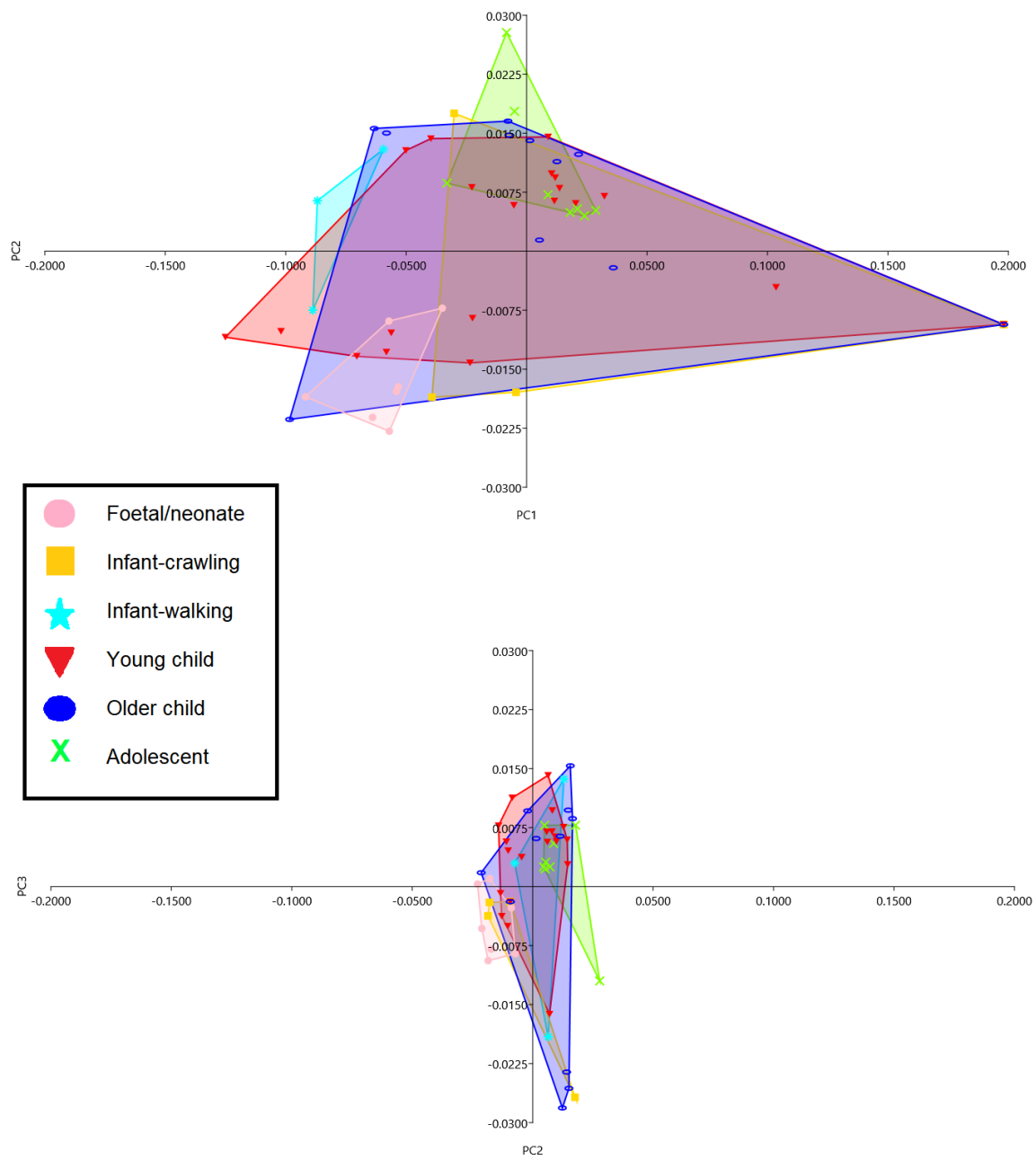


Figure S7. PCA of GMM coordinates

## 1.6 S8. MATLAB code for thickness calculations

```
function calculate_thickness_map
% This function looks at all the .tif files in a folder and calculates a thickness map
% it assumes that each tiff file is part of an image stack
num_samples = 360; % this is the number of samples per revolution, so 360 would give a 1 degree
interval
slice_subsample = 6; % this is the subsample factor for the innerpoint and outerpoint files
sample_subsample = 90; % this is the subsample factor for each slice for the innerpoint and
outerpoint files
% first get a folder from the user
folder_name = uigetdir('', 'Choose the folder that contains the image stack'); if
folder_name == 0    error('No folder selected');
end
%
%save_name = uigetdir('', 'Choose the folder to save results into');
%if save_name == 0
%error('No folder selected');
%end
% Change the code below to the directory you want to save the results to if
~exist(['C:\Users\~\'], 'dir') mkdir(['C:\Users\~\']) end
save_name = 'C:\Users\mqbpkto2\Dropbox (The University of Manchester)\Thesis
chapters\thickness mapping\JULY18'

file_list = dir(fullfile(folder_name, '*.tif')); if
isempty(file_list)
    error('No .tif files found in folder')
end
%this code will automatically read a csv with metadata in. Change the columns below to %reflect
where your voxel sizes are
excel_file_list = dir(fullfile(folder_name, '*metadata.csv')); if
isempty(excel_file_list)    error('No .csv files found in
folder')
end
for file_number = 1:length(excel_file_list)    file_name =
[folder_name '/' excel_file_list(file_number).name];    metadata =
xlsread(file_name);
end mm_per_pixel =
metadata(2) slice_thickness =
metadata(3)
%This dialogue lets you tell Matlab the dimensions of your file.
%response = inputdlg(['X-Y resolution in mm', 'Z resolution in mm'], 'Image Resolution', [1 50; 1
50]);
%if isempty(response)
%    error('The size of each image pixel must be specified')
%end

%mm_per_pixel = str2double(response{1});
```



```

1  %slice_thickness = str2double(response{2});
2  %this dialogue lets you input the start and end percentage for your sequence. %This
3  means that you can just leave all your images in the folder, and not %worry about
4  moving the unwanted slices to another folder.
5  %responseb = inputdlg('Start %','end %', 'Image Start and End Percent', [1 50; 1 50]);
6  %if isempty(responseb)
7      %error('The start and end Percentage must be specified')
8  %end
9  %start_image = str2double(responseb{1});
10 %end_image = str2double(responseb{2});
11 % or you can alter this code below, if you are going to be doing the same set of measurements
12 repeatedly start_image = 40; end_image = 160; start_perc = start_image;
13 end_perc = end_image;
14
15 %start_image = round((length(file_list)/100)*(str2double(responseb{1})));
16 %end_image = round((length(file_list)/100)*(str2double(responseb{2})));
17 %start_image = (round((length(file_list)/100)*(start_perc)));
18 %end_image = round((length(file_list)/100)*(end_perc));
19 file_numbers = end_image - start_image; file_list_subsample =
20 file_list(start_image:end_image); if ~exist([save_name
21 '\outerpoints\'],'dir') mkdir([save_name '\outerpoints\']) end
22 if ~exist([save_name '\innerpoints\'],'dir')
23 mkdir([save_name '\innerpoints\']) end
24 if ~exist([save_name '\slice_geometry\'],'dir')
25 mkdir([save_name '\slice_geometry\']) end
26 if ~exist([save_name '\outerpoints_subsample\'],'dir')
27 mkdir([save_name '\outerpoints_subsample\']) end
28 if ~exist([save_name '\thickness\'],'dir')
29 mkdir([save_name '\thickness\']) end
30 if ~exist([save_name '\innerpoints_subsample\'],'dir')
31 mkdir([save_name '\innerpoints_subsample\']) end
32 if ~exist([save_name '\thickness_plots\'],'dir')
33 mkdir([save_name '\thickness_plots\']) end
34 if ~exist([save_name '\thickness_images\'],'dir')
35 mkdir([save_name '\thickness_images\']) end
36 if ~exist([save_name '\J\'],'dir')
37 mkdir([save_name '\J\']) end
38 if ~exist([save_name '\CA\'],'dir')
39 mkdir([save_name '\CA\']) end
40 if ~exist([save_name '\Ix_Iy\'],'dir')
41 mkdir([save_name '\Ix_Iy\']) end
42 if ~exist([save_name '\Imax_Imin\'],'dir')
43 mkdir([save_name '\Imax_Imin\']) end
44 %thickness_image = zeros(num_samples,(length(end_image-start_image)));
45 thickness_image = zeros(file_numbers, num_samples);
46
47 [pathstr, name, ext] = fileparts(folder_name);

```

```

1  outerpoints_file = fopen([save_name '\outerpoints\' name '_outerpoints.csv'], 'w'); innerpoints_file =
2  fopen([save_name '\innerpoints\' name '_innerpoints.csv'], 'w'); outerpoints_subsample_file =
3  fopen([save_name '\outerpoints_subsample\' name
4  '_outerpoints_subsample.csv'], 'w');
5  innerpoints_subsample_file = fopen([save_name '\innerpoints_subsample\' name
6  '_innerpoints_subsample.csv'], 'w');
7  J_file = fopen([save_name '\J\' name '_J.csv'], 'w');
8  CA_file = fopen([save_name '\CA\' name '_CA.csv'], 'w');
9  Ix_Iy_file = fopen([save_name '\Ix_Iy\' name '_Ix_Iy.csv'], 'w');
10 Imax_Imin_file = fopen([save_name '\Imax_Imin\' name '_Imax_Imin.csv'], 'w'); centroids_file =
11 fopen([save_name '\slice_geometry\' name '_slice_geometry.csv'], 'w'); fprintf(centroids_file, 'slice,
12 centroid_x, centroid_y, min_thickness, max_thickness, TA, Cortical area, Trabecular area, J, Ix/Iy,
13 Imax/Imin\n', 'w');
14 fprintf(J_file, 'slice, J\n', 'w'); fprintf(CA_file, 'slice,
15 CA\n', 'w'); fprintf(Ix_Iy_file, 'slice, Ix/Iy\n', 'w');
16 fprintf(Imax_Imin_file, 'slice, Imax/Imin\n', 'w');
17 %thickness_file = fopen([save_name '\thickness\' name '_thickness.csv'], 'w');
18
19 for slice_counter = 1: length(file_list_subsample);
20
21     current_file = fullfile(folder_name, file_list_subsample(slice_counter).name);    fprintf('%s\n',
22     current_file);
23
24     [thickness, thickness_start, thickness_end, centroid_x, centroid_y] =
25     calculate_thickness(current_file, num_samples);    thickness = thickness .*
26     mm_per_pixel;    thickness_start = thickness_start .* mm_per_pixel;
27     thickness_end = thickness_end .* mm_per_pixel;    centroid_x = centroid_x
28     .* mm_per_pixel;    centroid_y = centroid_y .* mm_per_pixel;
29     max_thickness = max(thickness);
30     min_thickness = min(thickness);
31
32 %these following formulae calculate conventional cross sectional properties.    TotalA =
33 (polyarea(thickness_end(1:1,1:360), thickness_end(2:2,1:360)));
34 TrabA = (polyarea(thickness_start(1:1,1:360), thickness_start(2:2,1:360)));
35 Cortical_area = TotalA - TrabA;
36 %find Imax    distances = sqrt((thickness_end(1:1,1:360) -
37 centroid_x).^2 + ((thickness_end(2:2,1:360) - centroid_y).^2);
38 [maxRadius, maxRadiusIndex] = max(distances);    maxPointCoord =
39 thickness_end(:, maxRadiusIndex);    maxPointCoordiner =
40 thickness_start(:, maxRadiusIndex);    opp_point = maxRadiusIndex + 180;
41 if opp_point > 360    opp_point =
42 opp_point - 360
43 else
44     opp_point = opp_point
45 end
46 opp_pointCoord = thickness_end(:, opp_point);
47 opp_pointCoordiner = thickness_start(:, opp_point);    %extract Imax

```



```

1     Imax = sqrt((((maxPointCoord(1))-
2 (opp_pointCoord(1))).^2)+((((maxPointCoord(2))(opp_pointCoord(2))).^2)));
3     Imax_inner = sqrt((((maxPointCoordinner(1))-
4 (opp_pointCoordinner(1))).^2)+((((maxPointCoordinner(2))-(opp_pointCoordinner(2))).^2)));
5     %find Imin
6     [minRadius, minRadiusIndex] = min(distances); minPointCoord =
7 thickness_end(:,minRadiusIndex); minPointCoordinner =
8 thickness_start(:,minRadiusIndex); opp_pointmin =
9 minRadiusIndex+180;
10    if opp_pointmin>360
11        opp_pointmin = opp_pointmin-360    else
12        opp_pointmin = opp_pointmin    end
13    opp_pointminCoord = thickness_end(:,opp_pointmin); opp_pointminCoordinner =
14 thickness_start(:,opp_pointmin);
15    %extract Imin
16    Imin = sqrt((((minPointCoord(1))-(opp_pointminCoord(1))).^2)+((((minPointCoord(2))-
17 (opp_pointminCoord(2))).^2)));
18    Imin_inner = sqrt((((minPointCoordinner(1))-
19 (opp_pointminCoordinner(1))).^2)+((((minPointCoordinner(2))-
20 (opp_pointminCoordinner(2))).^2)));
21
22    %extract max and min second moments of area
23    Second_moment_of_area_min = (pi*((Imin^4)-(Imin_inner^4))/32
24    Second_moment_of_area_max = (pi*((Imax^4)-(Imax_inner^4))/32
25
26    %extractImax/Imin for circularity measure
27    Ix_Iy = Imax/Imin;
28    %extract J
29    J = Second_moment_of_area_min+Second_moment_of_area_max;
30    %Extract moments of area divided
31    Imax_Imin = Second_moment_of_area_max/Second_moment_of_area_min;
32
33    fprintf('Max thickness = %f\n', max_thickness); fprintf('Min
34 thickness = %f\n', min_thickness);
35    %fprintf('TA = %f\n', TotalA);
36    %fprintf('Cortical area = %f\n', Cortical_area);
37    %fprintf('Trabecular area = %f\n', TrabA);
38    %fprintf('J = %f\n', J);
39    %fprintf('Ix/Iy = %f\n', Ix_Iy);
40    %fprintf('Imax/Imin = %f\n', Imax_Imin);
41
42    fprintf(centroids_file, '%d,%g,%g,%g,%g,%g,%g,%g,%g,%g\n', slice_counter, centroid_x,
43 centroid_y, min_thickness, max_thickness, TotalA, Cortical_area, TrabA, J, Ix_Iy, Imax_Imin);
44    fprintf(J_file, '%d, %g\n', slice_counter, J);
45    fprintf(CA_file, '%d, %g\n', slice_counter, Cortical_area); fprintf(Ix_Iy_file,
46 '%d, %g\n', slice_counter, Ix_Iy);
47    fprintf(Imax_Imin_file, '%d, %g\n', slice_counter, Imax_Imin);
48

```

```

1
2
3     thickness_image(slice_counter, :) = thickness;
4
5
6     for sample_counter = 1: length(thickness_start);
7         fprintf(innerpoints_file, '%d,%g,%g\n', (slice_counter*slice_thickness), thickness_start(1,
8 sample_counter), thickness_start(2, sample_counter));
9         fprintf(outerpoints_file, '%d,%g,%g\n', (slice_counter*slice_thickness), thickness_end(1,
10 sample_counter), thickness_end(2, sample_counter));
11         fprintf(thickness_file, thickness);
12         if (mod(slice_counter, slice_subsample) == 0 && mod(sample_counter, sample_subsample) ==
13 0)
14             fprintf(innerpoints_subsample_file, '%d,%g,%g\n', slice_counter.*slice_thickness,
15 thickness_start(1), thickness_start(2));
16             fprintf(outerpoints_subsample_file, '%d,%g,%g\n', slice_counter.*slice_thickness,
17 thickness_end(1), thickness_end(2));      end
18
19     end
20
21 end
22
23 fclose(outerpoints_file); fclose(innerpoints_file);
24 fclose(outerpoints_subsample_file);
25 fclose(innerpoints_subsample_file);
26 fclose(centroids_file);
27 fclose(CA_file); fclose(J_file);
28 fclose(Ix_Iy_file);
29 fclose(Imax_Imin_file);
30
31 %thickness_image2 = thickness_image(start_image:end);
32 % write the thickness data to a CSV file
33 %csvwrite((fullfile([folder_name] 'thickness_output.csv'), thickness_image);
34 %[pathstr, name, ext] = fileparts(folder_name);
35 %csvwrite([save_name '\thickness\' name 'thickness2.csv'], thickness_image2);
36 %csvwrite([save_name '\thickness\' name 'thickness.csv'], thickness_image);
37
38 % produce a suitable image of the thickness map
39
40 graph_title1 = ('Cortical thickness of '); graph_title2 = ('
41 humerus. Colour scale is in mm'); graph_bone =
42 (excel_file_list.name(1:end-12)); %graph_bone2 =
43 graph_bone(1:end-12);
44 graph_title = [graph_title1, graph_bone, graph_title2];
45 [pathstr, name, ext] = fileparts(folder_name); figure(1);
46 clf('reset'); set(gcf, 'Color', 'w'); set(gcf, 'Units', 'pixels'); set(gcf,
47 'Position', [50, 50, 1000, 1000]);

```



```

1  set(gcf,'PaperType','<custom>'); set(gcf,'Units','inches'); set(gcf,'PaperUnits','inches'); position =
2  get(gcf,'Position'); set(gcf,'PaperPosition',[0,0,position(3:4)]); set(gcf,'PaperSize',position(3:4));
3  imagesc(thickness_image); colormap(jet(256));
4  %axes1 = axes('Parent',figure(1),...
5      %'XTickLabel',{'Anterior','Medial','Posterior','Lateral','Anterior'},...
6      % 'XTick',[0 90 180 270 360],...
7      %'Layer','top',...
8      %'YDir','reverse',...
9      %'YTick',zeros(1,0));
10 %% Uncomment the following line to preserve the X-limits of the axes
11 % xlim(axes1,[0.5 360.5]);
12 %% Uncomment the following line to preserve the Y-limits of the axes
13 % ylim(axes1,[0.5 4.5]);
14 %box(axes1,'on');
15 %hold(axes1,'on');
16
17 % Create image
18 %image(cdata1,'Parent',axes1,'CDataMapping','scaled');
19
20 % Create xlabel
21 xlabel('Bone Position');
22
23 % Create ylabel
24 ylabel({'Distal to proximal humerus.'});
25
26 % Create title title(graph_title);
27 % Create colorbar colorbar('EastOutside'); % Create arrow
28 annotation('arrow',[0.0613750000000001 0.0593750000000001],...
29     [0.922330097087376 0.107142857142857]); set(gca,
30 'XTick',[0 90 180 270 360]);
31 'XTickLabel',{'Anterior','Medial','Posterior','Lateral','Anterior'};...
32 plot_name = fullfile(folder_name, 'thickness_plot');
33 print(gcf,'-dpdf',[save_name '\thickness_plots\' name 'thickness plot', '.pdf'],'-r 150') print(gcf,'-
34 depsc2',[save_name '\thickness_plots\' name 'thickness plot', '.eps'],'-r 150') print(gcf,'-
35 dtiff',[save_name '\thickness_plots\' name 'thickness plot', '.png'],'-r 72') figure(2);
36 clf('reset'); set(gcf, 'Color', 'w'); set(gcf,'Units','pixels'); set(gcf,
37 'Position', [50, 50, 1000, 1000]);
38 set(gcf,'PaperType','<custom>'); set(gcf,'Units','inches'); set(gcf,'PaperUnits','inches'); position =
39 get(gcf,'Position'); set(gcf,'PaperPosition',[0,0,position(3:4)]); set(gcf,'PaperSize',position(3:4));
40 imagesc(thickness_image); colormap(jet(256));
41 plot_name2 = fullfile(folder_name, 'thickness_image');
42 print(gcf,'-dpdf',[save_name '\thickness_images\' name 'thickness_image', '.pdf'],'-r 150') print(gcf,'-
43 depsc2',[save_name '\thickness_images\' name 'thickness_image', '.eps'],'-r 150') print(gcf,'-
44 dtiff',[save_name '\thickness_images\' name 'thickness_image', '.png'],'-r 72')
45
46 % ask if the thickness file should be saved somewhere %[pathstr,
47 name, ext] = fileparts(folder_name); default_name = [name,
48 '_thickness.csv'];

```

```

1  %[file_name, path_name] = uiputfile('*.csv', 'Save the thickness image', default_name);
2  %if file_name ~= 0
3      %csvwrite(fullfile(path_name, file_name), thickness_image); return
4  function [thickness, thickness_start, thickness_end, centroid_x, centroid_y] =
5  calculate_thickness(current_file, num_samples)
6
7  % this function calculates the thickness of the bone wall
8  % it produces num_samples values from angle zero to 360
9  % zero angle is aligned with the X axis and increases counterclockwise
10
11 % read the image data =
12 imread(current_file); [height,
13 width, channels] = size(data);
14
15 % now do some sanity checking on the image
16 if channels ~= 1
17     error('Only greyscale images supported'); end
18
19 if data(1, 1) ~= data(1, width) || data(1, 1) ~= data(height, width) || data(1, 1) ~= data(height, 1)
20     error('All 4 corners of the image must have the same greyscale value'); end
21
22 background = data(1, 1);
23
24 % find the centroid xsum
25 = 0; ysum = 0; count = 0;
26 for ix = 1: width    for iy
27 = 1: height
28     if data(iy, ix) ~= background
29 xsum = xsum + ix;        ysum = ysum
30 + iy;        count = count + 1;
31     end
32     end end
33 if count == 0 % must be a completely blank image so set all the thicknesses to zero
34 fprintf('Centroid not found\n');    thickness = zeros(1, file_numbers);    return end
35 centroid_x = xsum / count; centroid_y =
36 ysum / count;
37 fprintf('Centroid x = %f y = %f\n', centroid_x, centroid_y);
38 % now work radially around from centroid
39 thickness = 9999 * ones(1, num_samples); % create a suitable row vector to hold the thicknesses using
40 dummy big values
41 thickness_start = zeros(2, num_samples);
42 thickness_end = zeros(2, num_samples); for i = 1:
43 num_samples
44     circle_fraction = (i - 1) / num_samples;
45 angle = 2 * pi() * circle_fraction;    del_x =
46 cos(angle);    del_y = sin(angle);    % look for
47 the inner edge

```

```

1     for r = 0: 0.5: max([width, height]) % the 0.5 here gets us around any potential rounding error
2     problems
3         x = r * del_x + centroid_x;      y
4     = r * del_y + centroid_y;      ix =
5     round(x);      iy = round(y);
6         if (ix < 1 || ix > width || iy < 1 || iy > height)
7             % if we can't find the inner edge then there is a complete hole here so set the thickness to zero
8             thickness(i) = 0;
9             break;
10        end
11        if data(iy, ix) ~= background % found the inner edge
12        thickness_start(1, i) = ix;      thickness_start(2, i) = iy;
13            break;      end
14    end    if thickness(i) ~=
15    0
16        % look for the outer edge
17        for r = max([width, height]): -0.5: 0 % the -0.5 here gets us around any potential rounding error
18        problems
19            x = r * del_x + centroid_x;
20        y = r * del_y + centroid_y;      ix
21        = round(x);      iy = round(y);
22            if (ix < 1 || ix > width || iy < 1 || iy > height)
23                continue; % this isn't an error, we just haven't found the edge of the image yet
24        end
25            if data(iy, ix) ~= background % found the outer edge
26        thickness_end(1, i) = ix;      thickness_end(2, i) = iy;
27                break;
28        end    end
29        % if the outer edge is the same as the inner edge it means that the radial line has met at the same
30        pixel
31        % so in fact the distance between the outer edge and inner edge is always 1 pixel too small so
32        %we need to correct for this
33        thickness(i) = 1 + sqrt((thickness_end(1, i) - thickness_start(1, i))^2 + (thickness_end(2, i) -
34        thickness_start(2, i))^2);
35
36    end
37
38    end
39
40    return
41
42
43
44

```



## 1.7 S9. MATLAB code for periosteal curvature calculations

```
function k_fouriercurvature

%subsample = 10

% read the csv folder containing the outline coordinates for each stack
folder_name = uigetdir('','Choose the folder that contains the image stack'); if
folder_name == 0    error('No folder selected');
end
file_list = dir(fullfile(folder_name,'*.csv')); if
isempty(file_list)
    error('No .csv files found in folder')
end
%make a subdirectory for each output to be saved in.
if ~exist([folder_name '\curvature_rawpoints\'],'dir')
mkdir([folder_name '\curvature_rawpoints\']) end
if ~exist([folder_name '\curvature_heatmap\'],'dir')
mkdir([folder_name '\curvature_heatmap\']) end
if ~exist([folder_name '\curvature_2dgraph\'],'dir')
mkdir([folder_name '\curvature_2dgraph\']) end
if ~exist([folder_name '\curvature_values\'],'dir')
mkdir([folder_name '\curvature_values\']) end
if ~exist([folder_name '\smoothed_values\'],'dir')
mkdir([folder_name '\smoothed_values\']) end

for file_number = 1:length(file_list)

    file_name = [folder_name '/' file_list(file_number).name];
    [pathstr, name, ext] = fileparts(file_name);
    file_name2 = [folder_name '\curvature_values\' file_list(file_number).name(1:end-4)
'curvature.csv'];
    file_name3 = [folder_name '\smoothed_values\' file_list(file_number).name(1:end-4) 'smoothed
outline.csv'];
    heatmap_name = [folder_name '\curvature_heatmap\' file_list(file_number).name(1:end-4)
'curvature_heatmap'];
    smoothoutline_name = [folder_name '\curvature_2dgraph\' file_list(file_number).name(1:end-4)
'curvature_smoothed'];
    outline_name = [folder_name '\curvature_rawpoints\' file_list(file_number).name(1:end-4)
'original_curvature'];
    graph_bone_name = [name(1:end-12)];
    fourierpoints = csvread(file_name);

    slice_number = fourierpoints(:, 1); x_list =
    fourierpoints(:, 2);
    y_list = fourierpoints(:, 3);
```

```

1  % count the number of points in a slice
2  points_per_slice = 1; for i = 1:
3  length(slice_number) - 1    if (slice_number(i +
4  1) ~= slice_number(i))      break;    end
5      points_per_slice = points_per_slice + 1; end
6
7  slice_number = reshape(slice_number, [points_per_slice, length(slice_number) / points_per_slice]);
8  % this reshape needs checking
9  x_list = reshape(x_list, [points_per_slice, length(x_list) / points_per_slice]); y_list =
10 reshape(y_list, [points_per_slice, length(y_list) / points_per_slice]);
11
12 [r, c] = size(slice_number); num_slices =
13 c; num_points_wanted = 360;
14 k_map = zeros(num_slices, num_points_wanted);
15 l = zeros(num_slices*num_points_wanted,3);
16 for i = 1:3    figure(i)    clf('reset');    set(gcf,
17 'Color', 'w');    set(gcf,'Units','pixels');
18    set(gcf, 'Position', [i + 50, i + 50, 1000, 1000]); end
19
20
21 for slice = 1: num_slices
22 x = x_list(1:points_per_slice, slice);
23 y = y_list(1:points_per_slice, slice);
24
25    figure(1);    plot(x,
26 y);
27    hold on;
28    plot_name3 = outline_name;
29    title(['Original endosteal contour of ' graph_bone_name ' humerus from a  $\mu$ CT scan']);
30 xlabel('X'); ylabel('Y');
31    %print(gcf,'-dtiff',[plot_name3, '.png'],'-r 72');
32    %print({(gcf'-dtiff', plot_name3, '.png')} '-r 72');
33    %print(gcf,'-depsc2','eps')
34    %hold off;
35    %print(gcf,'-dtiff',[plot_name3, '.png'],'-r 72')
36
37
38    outline = [x, y];
39    iNoOfHarmonicsAnalyse = points_per_slice / 2;
40    bNormaliseSizeState = 0;    bNormaliseOrientationState
41 = 0;
42    rFSDs = fEfourier(outline, iNoOfHarmonicsAnalyse, bNormaliseSizeState,
43 bNormaliseOrientationState);
44
45    % the degree of smoothing depends on the number of harmonics we choose
46 iNoOfHarmonicsReconstruct = 10;    iNoOfPointsReconstruct =
47 num_points_wanted;
48    smoothed_outln = rEfourier(rFSDs, iNoOfHarmonicsReconstruct, iNoOfPointsReconstruct);

```

```

1
2
3     %%%%% Jamie added in bit to output smoothed_outln variable
4 smoothed_outln_stored(:,2*slice-1) = smoothed_outln(:,1); smoothed_outln_stored(:,2*slice) =
5 smoothed_outln(:,2);
6
7     if slice == num_slices
8         %B = reshape(smoothed_outln_stored,[],2)
9         csvwrite([file_name(1:end-4) '_smoothed_outln.csv'],smoothed_outln_stored)
10        %csvwrite([file_name(1:end-4) '_smoothed_outln2.csv'],B) end
11    if slice == num_slices
12        B = reshape(smoothed_outln_stored,[],2)
13        csvwrite([file_name(1:end-4) '_smoothed_outln2.csv'],B) end
14
15    %%%%%%%%%%%%%%%
16    %%%%%%%%%%
17
18    %l_map(slice, :) = smoothed_outln; figure(2);
19    plot(smoothed_outln(:, 1), smoothed_outln(:, 2)); hold
20    on;
21    k_coeff = calc_k_coefficient(smoothed_outln(:, 1), smoothed_outln(:, 2)); k_map(slice,
22    :) = k_coeff;
23
24    title(['Smoothed endosteal contour of ' graph_bone_name ' humerus from a  $\mu$ CT scan']); xlabel('X');
25    ylabel('Y');
26    plot_name2 = smoothoutline_name;
27    %print(gcf,'-dtiff',[plot_name2, '.png'],'-r 72'); end
28    print(gcf,'-dtiff',[plot_name2, '.png'],'-r 72')
29    print(gcf,'-dtiff',[plot_name3, '.png'],'-r 72')
30    figure(3) clf('reset'); set(gcf, 'Color', 'w');
31    set(gcf,'Units','pixels');
32    set(gcf, 'Position', [50, 50, 1000, 1000]); imagesc(k_map);
33
34    set(gcf,'PaperType','<custom>');
35    set(gcf,'Units','inches');
36    set(gcf,'PaperUnits','inches'); position =
37    get(gcf,'Position');
38    set(gcf,'PaperPosition',[0,0,position(3:4)]);
39    set(gcf,'PaperSize',position(3:4)); plot_name =
40    [heatmap_name];
41    colormap(jet(256));
42    colorbar('EastOutside'); xlabel('Bone
43    Position'); ylabel('Slice
44    number.','Lower numbers are more
45    proximal')); title(['Surface curvature of '
46    graph_bone_name ' humerus']);
47    %print(gcf,'-dtiff',[plot_name3, '.png'],'-r 72');
48    %print(gcf,'-dpdf','Curvature Map.pdf','-r 150')

```



```

1  %print(gcf,'-depsc2','Curvature Map.eps','-r 150')
2  %print (gcf,'-depsc2','filename2 Curvature Map.eps','-r 150')
3
4  print(gcf,'-dpdf',[plot_name, '.pdf'],'-r 300') print(gcf,'-depsc2',[plot_name,
5  '.eps'],'-r 300') print(gcf,'-dtiff',[plot_name, '.png'],'-r 72')
6  % output the k values per slice to a file
7
8  %if (file_name2 ~= 0)  fout =
9  fopen((file_name2), 'w');  for slice =
10  1: num_slices      fprintf(fout, '%d',
11  slice);      k = k_map(slice, :);      for
12  t = 1: length(k)      fprintf(fout,
13  ',%f', k(t));      end
14      fprintf(fout, '\n');
15  end  fclose(fout);
16  fout2 = fopen((file_name3), 'w');
17
18  end
19  function rFSDs = fEfourier(outline, iNoOfHarmonicsAnalyse, bNormaliseSizeState,
20  bNormaliseOrientationState)
21  % Forward elliptical Fourier transform - see Kuhl FP and Giardina CR %
22  "Elliptic Fourier features of a closed contour" Computer Graphics and %
23  Image Processing 18:236-258 1982 for theory.
24  % Returns a shape spectrum of input x,y data "outline" with %
25  iNoOfHarmonicsAnalyse elements.
26  % The output FSDs will be normalised for location, size and orientation
27  % if bNormaliseSizeState and bNormaliseOrientationState are TRUE
28
29  % Pre-calculate some constant arrays
30  % n * 2 * pi
31  % n^2 * 2* pi^2
32  % where n is the number of harmonics to be used in the analysis rTwoNPi =
33  (1:1:iNoOfHarmonicsAnalyse)* 2 * pi; rTwoNSqPiSq = (1:1:iNoOfHarmonicsAnalyse) .*
34  (1:1:iNoOfHarmonicsAnalyse)* 2 * pi * pi;
35
36  iNoOfPoints = size(outline,1) - 1; % hence there is 1 more data point in outline than iNoOfPoints
37  rDeltaX = zeros(iNoOfPoints+1,1); % pre-allocate some arrays rDeltaY = zeros(iNoOfPoints+1,1);
38  rDeltaT = zeros(iNoOfPoints+1,1);
39
40  for iCount = 2 : iNoOfPoints + 1
41      rDeltaX(iCount-1) = outline(iCount,1) - outline(iCount-1,1);
42      rDeltaY(iCount-1) = outline(iCount,2) - outline(iCount-1,2); end
43
44  % Calculate 'time' differences from point to point - actually distances, but we are
45  % carrying on the fiction of a point running around the closed figure at constant speed.
46  % We are analysing the projections on to the x and y axes of this point's path around the figure for
47  iCount = 1 : iNoOfPoints

```

```

1      rDeltaT(iCount) = sqrt((rDeltaX(iCount)^2) + (rDeltaY(iCount)^2));
2  end check = (rDeltaT ~= 0); % remove zeros from rDeltaT, rDeltaX...
3  rDeltaT = rDeltaT(check); rDeltaX =
4  rDeltaX(check); rDeltaY =
5  rDeltaY(check);
6
7  iNoOfPoints = size(rDeltaT,1) - 1; % we have removed duplicate points %
8  now sum the incremental times to get the time at any point rTime(1) = 0;
9  for iCount = 2 : iNoOfPoints + 1
10     rTime(iCount) = rTime(iCount - 1) + rDeltaT(iCount-1); end
11
12  rPeriod = rTime(iNoOfPoints+1); % rPeriod defined for readability
13  % calculate the A-sub-0 coefficient rSum1 =
14  0;
15  for iP = 2 : iNoOfPoints + 1
16     rSum2 = 0;    rSum3 = 0;
17     rInnerDiff = 0;
18     % calculate the partial sums - these are 0 for iCount = 1
19     if iP > 1      for iJ = 2 : iP-1
20         rSum2 = rSum2 + rDeltaX(iJ-1);
21     rSum3 = rSum3 + rDeltaT(iJ-1);    end
22     rInnerDiff = rSum2 - ((rDeltaX(iP-1) / rDeltaT(iP-1)) * rSum3); end
23     rIncr1 = ((rDeltaX(iP-1) / (2*rDeltaT(iP-1)))*(rTime(iP)^2-rTime(iP-1)^2) +
24     rInnerDiff*(rTime(iP)rTime(iP-1)));    rSum1 = rSum1 + rIncr1; end
25     rFSDs(1,1) = ((1 / rPeriod) * rSum1) + outline(1,1); % store A-sub-0 in output FSDs array - this array
26     will be 4 x iNoOfHarmonicsAnalyse % calculate the a-sub-n coefficients
27     for iHNo = 2 : iNoOfHarmonicsAnalyse
28         rSum1 = 0;    for iP = 1 : iNoOfPoints
29             rIncr1 = (rDeltaX(iP) / rDeltaT(iP))*((cos(rTwoNPi(iHNo-1)*rTime(iP+1)/rPeriod) -
30             cos(rTwoNPi(iHNo-1)*rTime(iP)/rPeriod)));
31             rSum1 = rSum1 + rIncr1;
32         end
33         rFSDs(1,iHNo) = (rPeriod / rTwoNSqPiSq(iHNo-1)) * rSum1; end %
34     "foriHNo = 1 :..."
35
36     rFSDs(2,1) = 0; % there is no 0th order sine coefficient
37     % calculate the b-sub-n coefficients
38     for iHNo = 2 : iNoOfHarmonicsAnalyse
39         rSum1 = 0;    for iP = 1 : iNoOfPoints
40             rIncr1 = (rDeltaX(iP) / rDeltaT(iP))*((sin(rTwoNPi(iHNo-1)*rTime(iP+1)/rPeriod) -
41             sin(rTwoNPi(iHNo-1)*rTime(iP)/rPeriod)));
42             rSum1 = rSum1 + rIncr1;    end
43             rFSDs(2,iHNo) = (rPeriod / rTwoNSqPiSq(iHNo-1)) * rSum1;
44     end % "foriHNo = 1 :..." % calculate the C-sub-0 coefficient
45     rSum1 = 0;
46     for iP = 2 : iNoOfPoints + 1
47         rSum2 = 0;    rSum3 = 0;
48         rInnerDiff = 0;

```

```

1      % calculate the partial sums - these are 0 for iCount = 1
2  if iP > 1      for iJ = 2 : iP-1
3      rSum2 = rSum2 + rDeltaY(iJ-1);
4  rSum3 = rSum3 + rDeltaT(iJ-1);      end
5      rInnerDiff = rSum2 - ((rDeltaY(iP-1) / rDeltaT(iP-1)) * rSum3);      end
6      rIncr1 = ((rDeltaY(iP-1) / (2*rDeltaT(iP-1)))*(rTime(iP)^2-rTime(iP-1)^2) +
7  rInnerDiff*(rTime(iP)rTime(iP-1)));      rSum1 = rSum1 + rIncr1; end
8  rFSDs(3,1) = ((1 / rPeriod) * rSum1) + outline(1,2); % store C-sub-0 in output FSDs array - this array
9  will be 4 x iNoOfHarmonicsAnalyse
10
11  % calculate the C-sub-n coefficients
12  for iHNo = 2 : iNoOfHarmonicsAnalyse
13  rSum1 = 0;      for iP = 1 : iNoOfPoints
14      rIncr1 = (rDeltaY(iP) / rDeltaT(iP))*((cos(rTwoNPi(iHNo-1)*rTime(iP+1)/rPeriod) -
15  cos(rTwoNPi(iHNo-1)*rTime(iP)/rPeriod)));
16      rSum1 = rSum1 + rIncr1;
17  end
18      rFSDs(3,iHNo) = (rPeriod / rTwoNSqPiSq(iHNo-1)) * rSum1; end %
19  "foriHNo = 1 :..."
20
21  rFSDs(4,1) = 0; % there is no 0th order sine coefficient
22
23  % calculate the D-sub-n coefficients
24  for iHNo = 2 : iNoOfHarmonicsAnalyse
25  rSum1 = 0;      for iP = 1 : iNoOfPoints
26      rIncr1 = (rDeltaY(iP) / rDeltaT(iP))*((sin(rTwoNPi(iHNo-1)*rTime(iP+1)/rPeriod) -
27  sin(rTwoNPi(iHNo-1)*rTime(iP)/rPeriod)));
28      rSum1 = rSum1 + rIncr1;
29  end
30      rFSDs(4,iHNo) = (rPeriod / rTwoNSqPiSq(iHNo-1)) * rSum1; end %
31  "foriHNo = 1 :..."
32
33  % the non-normalised coefficients are now in rFSDs % if we want the
34  normalised ones, this is where it happens if (bNormaliseSizeState == 1) ||
35  (bNormaliseOrientationState == 1)      % rTheta1 is the angle through
36  which the starting position of the first
37  % harmonic phasor must be rotated to be aligned with the major axis of
38  % the first harmonic ellipse      rFSDsTemp
39  = rFSDs;
40      rTheta1 = 0.5 * atan(2 * (rFSDsTemp(1,2) * rFSDsTemp(2,2) + rFSDsTemp(3,2) * rFSDsTemp(4,2)) /
41  ...
42      (rFSDsTemp(1,2)^2 + rFSDsTemp(3,2)^2 - rFSDsTemp(2,2)^2 - rFSDsTemp(4,2)^2));
43      % calculate the partially normalised coefficients - normalised for
44      % starting point
45      for iHNo = 1 : iNoOfHarmonicsAnalyse
46          rStarFSDs(1,iHNo) = cos((iHNo-1) * rTheta1) * rFSDsTemp(1,iHNo) + sin((iHNo-1) * rTheta1) *
47  rFSDsTemp(2,iHNo);
48          rStarFSDs(2,iHNo) = -sin((iHNo-1) * rTheta1) * rFSDsTemp(1,iHNo) + cos((iHNo-1) * rTheta1)

```

```

1  * rFSDsTemp(2,iHNo);
2      rStarFSDs(3,iHNo) = cos((iHNo-1) * rTheta1) * rFSDsTemp(3,iHNo) + sin((iHNo-1) * rTheta1) *
3  rFSDsTemp(4,iHNo);
4      rStarFSDs(4,iHNo) = -sin((iHNo-1) * rTheta1) * rFSDsTemp(3,iHNo) + cos((iHNo-1) * rTheta1)
5  * rFSDsTemp(4,iHNo);
6  end % for iHNo = 1 : iNoOfHarmonicsAnalyse
7
8      rPsi1 = atan(rStarFSDs(3,2) / rStarFSDs(1,2));
9      rSemiMajor = sqrt(rStarFSDs(1,2)^2 + rStarFSDs(3,2)^2); % find the semi-major axis of the first
10 ellipse
11
12      rFSDs(:, :) = rStarFSDs(:, :) ./ rSemiMajor; % if we haven't asked for normalisation of orientation,
13 % return the coefficients normalised for starting point and size      if bNormaliseOrientationState
14 == 1
15          % now find the orientation normalised values - return them in rFSDs
16 for iHNo = 1 : iNoOfHarmonicsAnalyse
17     rFSDsTemp(1,iHNo) = (cos(rPsi1) * rStarFSDs(1,iHNo) + sin(rPsi1) * rStarFSDs(3,iHNo)) /
18 rSemiMajor;
19     rFSDsTemp(2,iHNo) = (cos(rPsi1) * rStarFSDs(2,iHNo) + sin(rPsi1) * rStarFSDs(4,iHNo)) /
20 rSemiMajor;
21     rFSDsTemp(3,iHNo) = (-sin(rPsi1) * rStarFSDs(1,iHNo) + cos(rPsi1) * rStarFSDs(3,iHNo)) /
22 rSemiMajor;
23     rFSDsTemp(4,iHNo) = (-sin(rPsi1) * rStarFSDs(2,iHNo) + cos(rPsi1) * rStarFSDs(4,iHNo)) /
24 rSemiMajor;
25 end % for iHNo = 1 : iNoOfHarmonicsAnalyse      rFSDs =
26 rFSDsTemp; % return fully normlised coefficients      end
27 end % if (bNormaliseSizeState == 1) || (bNormaliseOrientationState == 1)
28
29 return
30
31 function outln = rEfouier( rFSDs, iNoOfHarmonicsReconstruct,iNoOfPointsReconstruct)
32 % Reverse elliptical Fourier transform on the input Fourier series
33 % rFSDs generated by fEfouier.m. This reconstructs an approximation to the original outline figure
34 % using the specified number of harmonics and data points. See Kuhl FP and Giardina CR %
35 "Elliptic Fourier features of a closed contour" Computer Graphics and % Image Processing
36 18:236-258 1982 for theory and details.
37
38 iStartHarmonic = 2; % start at 2 - No.1 is just an offset and is added in later (lines 17 & 27)
39 ReconnedOutline = 0; % reconstruct the
40 x-projection for iTime =
41 1:iNoOfPointsReconstruct
42     rSum = 0.0;
43     for iHNo = iStartHarmonic:iNoOfHarmonicsReconstruct      rSum = rSum + (rFSDs(1,iHNo)
44 * cos(2*(iHNo-1)*pi*iTime / iNoOfPointsReconstruct) + ...
45     rFSDs(2,iHNo) * sin(2*(iHNo-1)*pi*iTime / iNoOfPointsReconstruct));
46     end % for iHNo = 1 : iNoOfHarmonicsReconstruct      ReconnedOutline(iTime,1)
47 = rFSDs(1,1) + rSum; end % for iTime = 1 : iNoOfPointsReconstruct
48

```



```

1  % reconstruct the y-projection for iTime =
2  1:iNoOfPointsReconstruct
3      rSum = 0.0;
4      for iHNo = iStartHarmonic:iNoOfHarmonicsReconstruct      rSum = rSum + (rFSDs(3,iHNo) *
5  cos(2*(iHNo-1)*pi*iTime / iNoOfPointsReconstruct) + ...
6      rFSDs(4,iHNo) * sin(2*(iHNo-1)*pi*iTime / iNoOfPointsReconstruct));
7      end % for iHNo = 1 : iNoOfHarmonicsReconstruct
8  ReconnedOutline(iTime,2) = rFSDs(3,1) + rSum; end % for
9  iTime = 1 : iNoOfPointsReconstruct outln =
10 ReconnedOutline;
11
12 return
13
14 function k_coeff = calc_k_coefficient(x, y)
15
16     x_diff = circular_diff(x, 1);    x_diff2 =
17     circular_diff(x_diff, 1);    y_diff =
18     circular_diff(y, 1);
19     y_diff2 = circular_diff(y_diff, 1);
20
21     k_coeff = zeros(1, length(x_diff));    for t =
22     1: length(x_diff)
23         numerator = x_diff(t) * y_diff2(t) - y_diff(t) * x_diff2(t);
24         denominator = (x_diff(t)^2 + y_diff(t)^2)^(3/2);    k_coeff(t) =
25         numerator / denominator;    end
26
27 return
28     % do a simple linear difference differentiation on circular data
29 function yy = circular_diff(xx, interval) yy = xx; for i = 1: length(xx)    if
30 (i == 1)
31     yy(i) = (xx(i + 1) - xx(end)) / (2 * interval);
32 continue    end
33     if (i == length(xx))
34     yy(i) = (xx(1) - xx(i - 1)) / (2 * interval);
35 continue    end
36     yy(i) = (xx(i + 1) - xx(i - 1)) / (2 * interval); end
37 return
38
39

```

## 1.8 S10. MATLAB code for size standardisation of thickness maps

```
function standardise_gridto1
%This function will standardise a matrix so that all values fall between 0
%and 1. It can also be used to standardise values according to the matrices
%median values by uncommenting the appropriate commands
% first get a folder from the user
folder_name = uigetdir('','Choose the folder that contains the landmark coordinates');
if folder_name == 0
    error('No folder selected');
end
% make a series of folders for your results to go into
file_list = dir(fullfile(folder_name, '*.csv'));
if isempty(file_list)
    error('No .csv files found in folder')
end
if ~exist([folder_name '\normgrids0_1\'],'dir')
    mkdir([folder_name '\normgrids0_1\'])
end
%if ~exist([folder_name '\normgridstomedian\'],'dir')
%mkdir([folder_name '\normgridstomedian\'])
%end
if ~exist([folder_name '\norm_heatmap0_1\'],'dir')
    mkdir([folder_name '\norm_heatmap0_1\'])
end
if ~exist([folder_name '\norm_heatmap0_1b\'],'dir')
    mkdir([folder_name '\norm_heatmap0_1b\'])
end
file_number = 1:length(file_list)

    file_name = [folder_name '/' file_list(file_number).name];
    [pathstr, name, ext] = fileparts(file_name);

%This standardises all the values to the overall median value of the matrix
for file_number = 1:length(file_list)
    file_name = [folder_name '/' file_list(file_number).name];
    grid = csvread(file_name);
    ncols = size(grid,2)
    grid2 = grid([1:120],[1:ncols])
    gridmax = max(grid2(:))
    gridmin = min(grid2(:))
    standmin = (grid2-gridmin)
    stan0_1 = standmin./(gridmax-gridmin)
    %medianvalue = median(grid2(:))
    %standardised_grid = 1./grid2
    %standardised_grid2=grid2-medianvalue
    heatmap_name = [folder_name '\norm_heatmap0_1\' file_list(file_number).name(1:end-4)
'stand_heatmap'];
    heatmap_name2 = [folder_name '\norm_heatmap0_1b\' file_list(file_number).name(1:end-4)
'stand_heatmap2'];
```

```

1     csvwrite([folder_name '\normgrids0_1\' file_list(file_number).name(1:end-4) 'normgrid.csv'],
2     stan0_1);
3     % csvwrite([folder_name '\normgridstomedian\' file_list(file_number).name(1:end-4)
4     'normgrid2.csv'], standardised_grid2);
5     graph_bone_name = [file_list(file_number).name(1:end-4)];
6     figure(1)
7     clf('reset');
8     set(gcf, 'Color', 'w');
9     set(gcf, 'Units', 'pixels');
10    set(gcf, 'Position', [50, 50, 1000, 1000]);
11    imagesc(stan0_1)
12    %plot_name = heatmap_name
13    set(gcf, 'PaperType', '<custom>');
14    set(gcf, 'Units', 'inches');
15    set(gcf, 'PaperUnits', 'inches');
16    position = get(gcf, 'Position');
17    set(gcf, 'PaperPosition', [0,0,position(3:4)]);
18    set(gcf, 'PaperSize', position(3:4));
19    %axes1 = axes('Parent',figure1,...
20
21    plot_name = [heatmap_name];
22    colormap(jet(256));
23    colorbar('EastOutside');
24    xlabel('Bone Position');
25    ylabel({'Slice number.', 'Lower numbers are more proximal'});
26    %MODIFY THIS TITLE AS SEEN FIT
27    title(['Standardised cortical thickness of ' file_list(file_number).name(1:13) ' humerus']);
28    print(gcf, '-dtiff', [plot_name, '.png'], '-r 72')
29
30    figure(2)
31    clf('reset');
32    set(gcf, 'Color', 'w');
33    set(gcf, 'Units', 'pixels');
34    set(gcf, 'Position', [50, 50, 1000, 1000]);
35
36    imagesc(stan0_1)
37    set(gcf, 'PaperType', '<custom>');
38    set(gcf, 'Units', 'inches');
39    set(gcf, 'PaperUnits', 'inches');
40    position = get(gcf, 'Position');
41    set(gcf, 'PaperPosition', [0,0,position(3:4)]);
42    set(gcf, 'PaperSize', position(3:4));
43    plot_name2 = [heatmap_name2];
44    colormap(jet(256));
45    print(gcf, '-dtiff', [plot_name2, '.png'], '-r 72')
46    end
47
48
49
50

```

## 1.9 S11 MATLAB code for combining matrices and running PCA.

```
function combine_run_pca
% first get a folder from the user
folder_name = uigetdir('', 'Choose the folder that contains the landmark
coordinates');
if folder_name == 0
    error('No folder selected');
end
9
10 file_list = dir(fullfile(folder_name, '*.csv'));
11 if isempty(file_list)
12     error('No .csv files found in folder')
13 end
14 for file_number = 1:length(file_list)
15
16     file_name = [folder_name '/' file_list(file_number).name];
17     data1 = csvread(file_name);
18     data1 = data1(1:120,1:360)
19     data1a=reshape(data1,43200,1)
20
21     combineda(file_number,:) = horzcat(data1a);
22
23 end
24 %Runs PCA and exports csv files of scores.Replace *NAME* with an
25 appropriate prefix.
26 [coeff,score,latent,tsquared,explained,mu] = pca(combineda)
27 csvwrite('*NAME*combinedvaluesforpca.csv',combineda)
28 csvwrite('*NAME*_scores.csv',score)
29 csvwrite('*NAME*_coeff.csv',coeff)
30 csvwrite('*NAME*_explained.csv',explained)
31
32 end
```