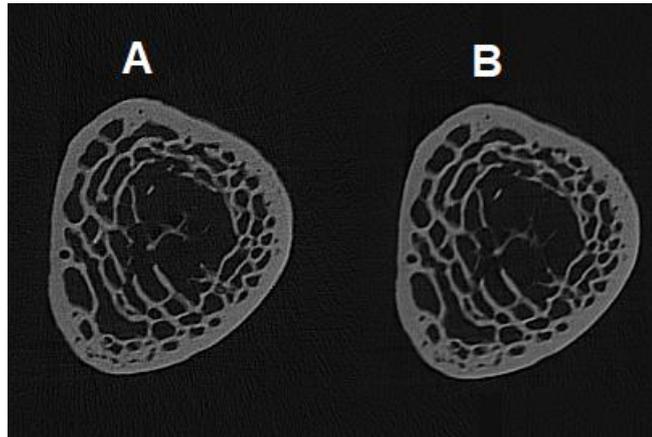


1 **1.1 S1. Example of downsampling**

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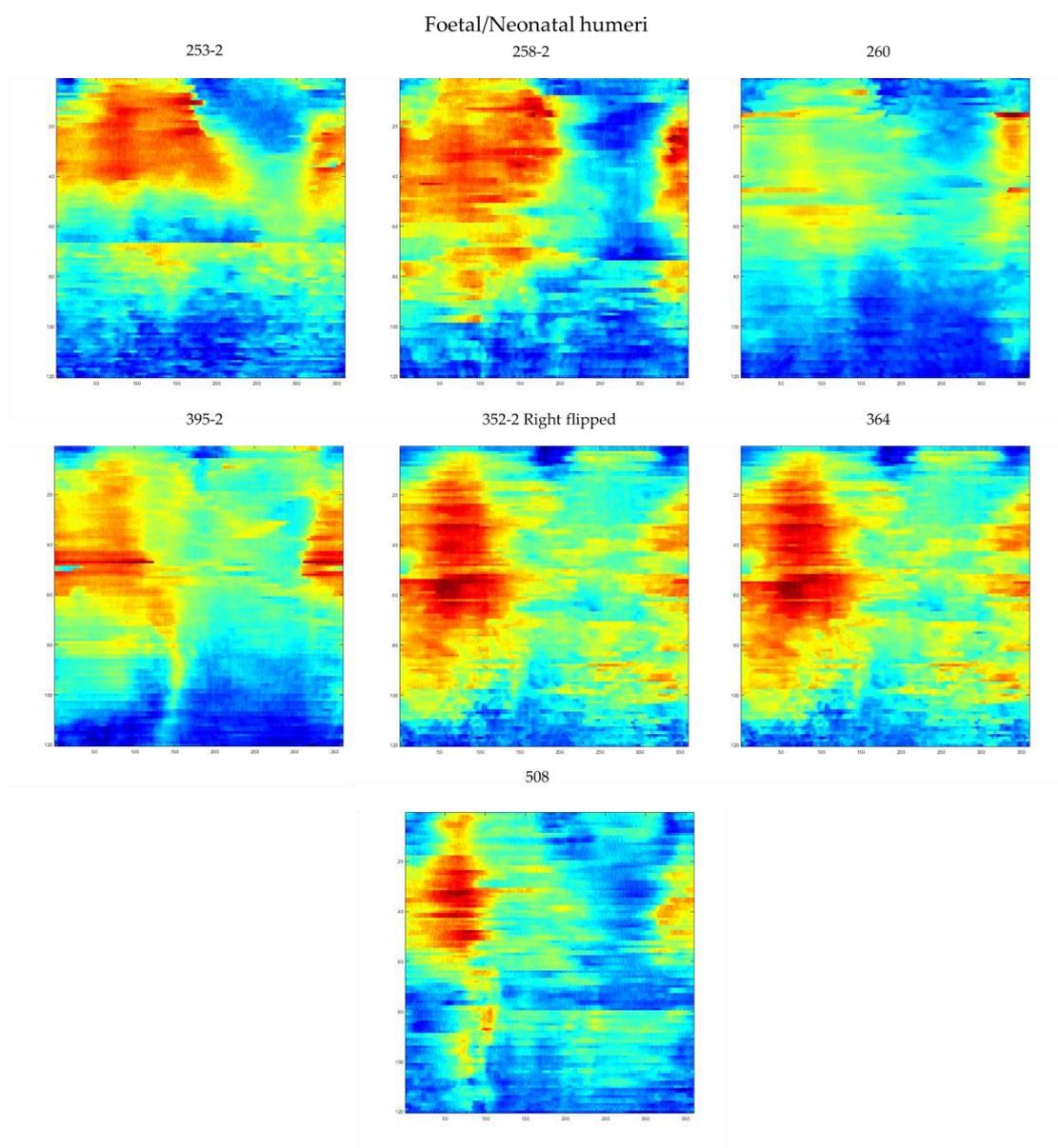
4

Effects of downsampling. A: Original resolution slice, B: Downsampled slice. As
5 downsampling was in the Z plane, the downsampling had little effect on X-Y
6 resolution.
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1 1.2 S2. Cortical thickness maps for all specimens



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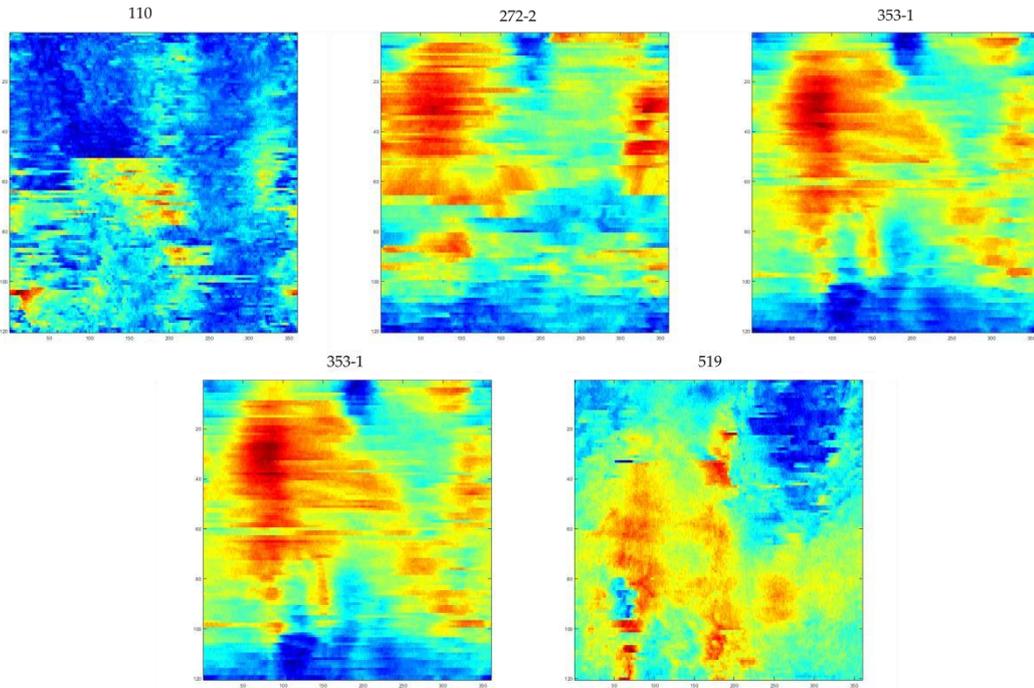
8

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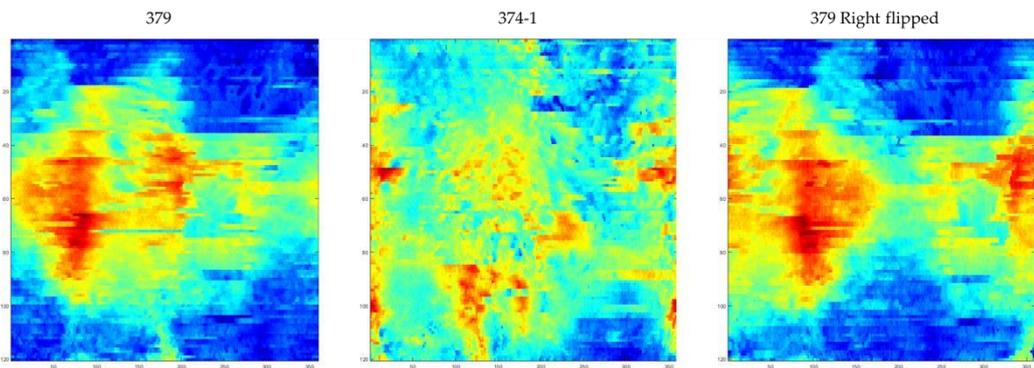
3

Infants-crawling humeri



4

Infants-walking humeri



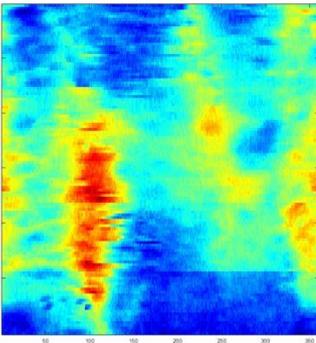
5

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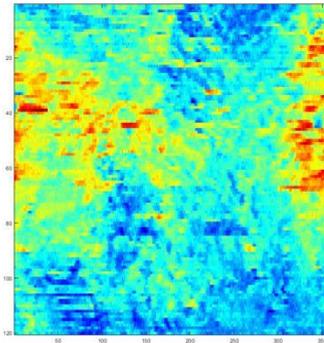
7

Younger child humeri

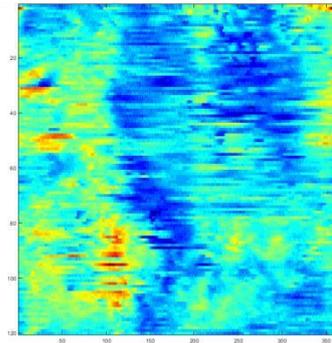
1



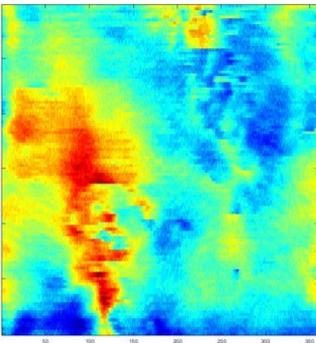
101 Right flipped



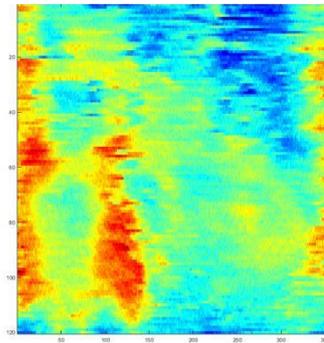
227 Right flipped



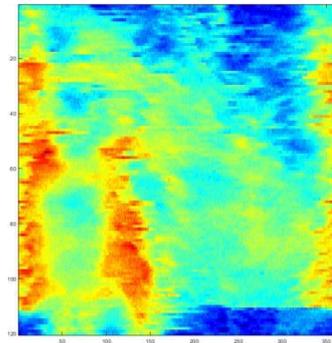
231 Right flipped



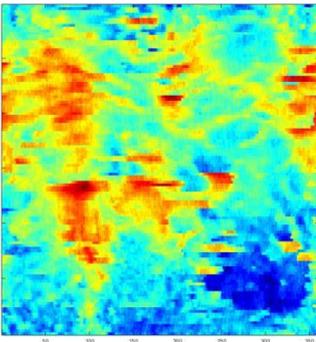
278-1



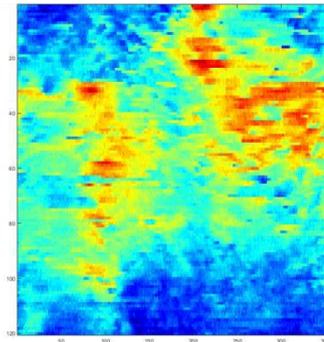
278-2



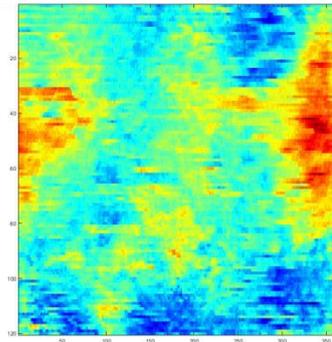
357-2 Right



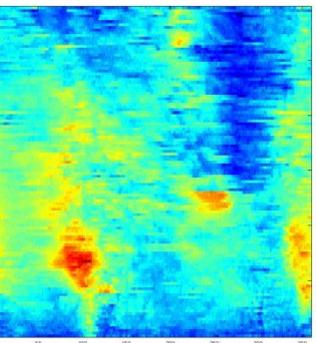
361



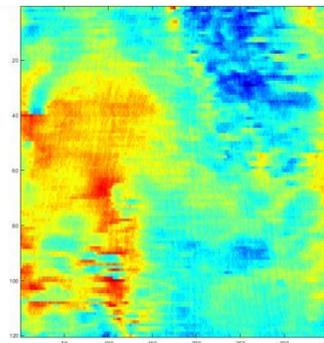
372



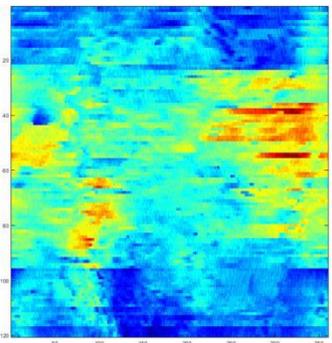
39



48

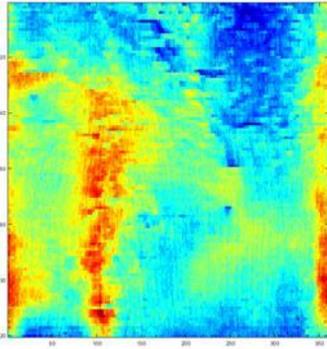


438

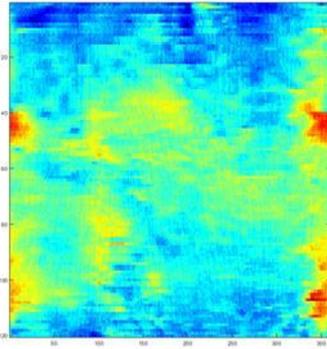


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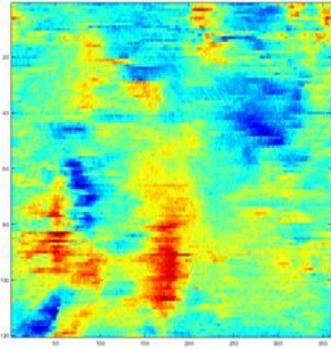
477-2



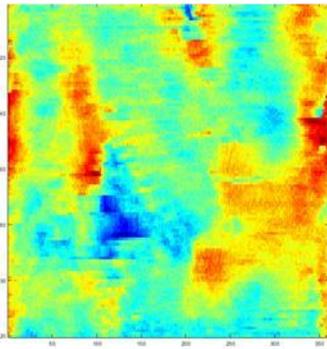
486



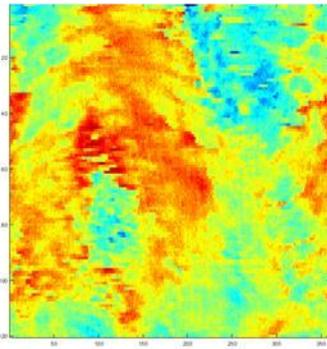
510-2



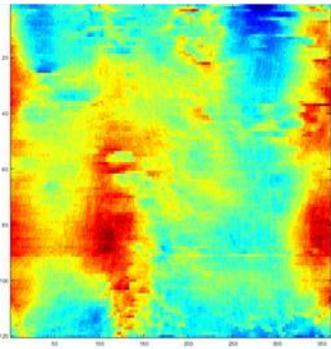
546-1



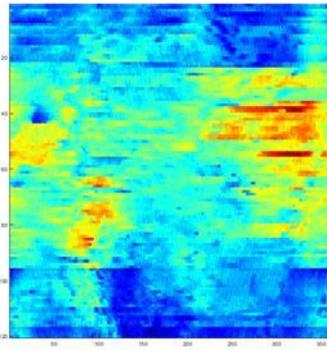
574 Right flipped



584



431



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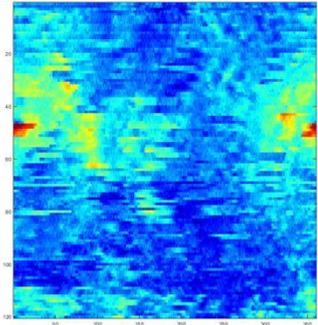
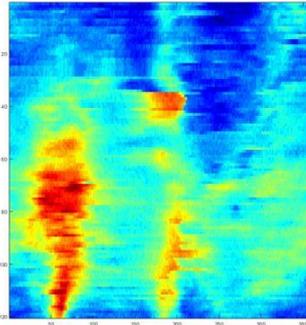
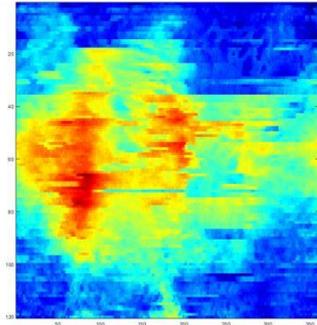
3

Older child humeri

379

135 Right flipped

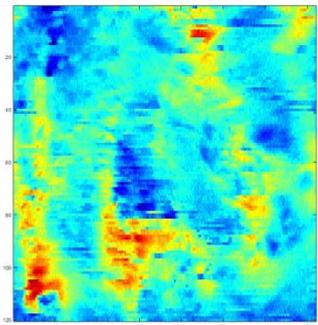
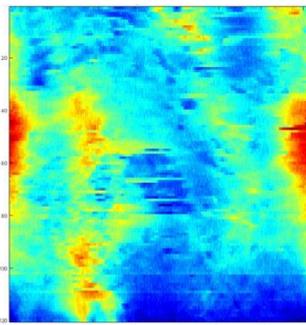
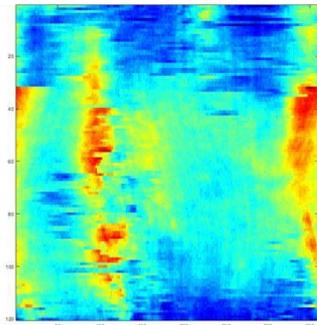
171



247 Right flipped

311

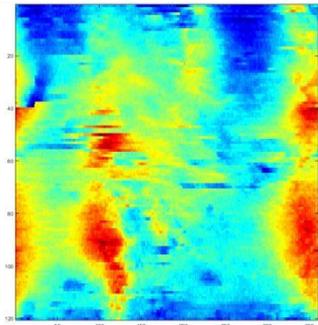
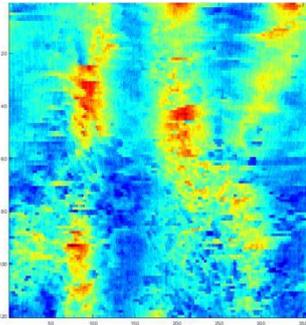
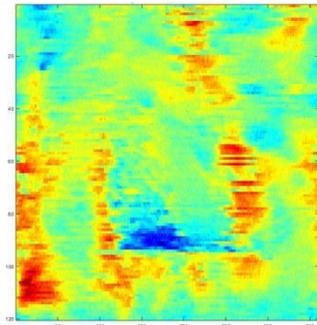
383



383 Right flipped

399 Right flipped

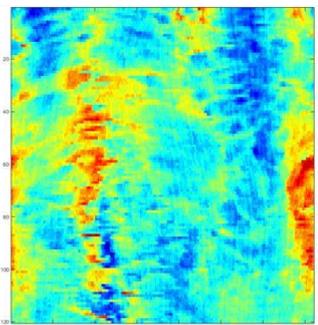
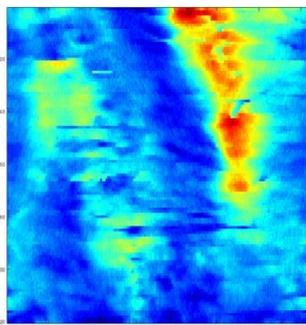
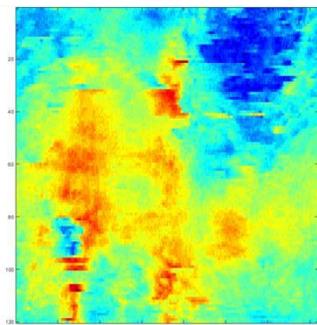
509-1 Right flipped



551-2

568

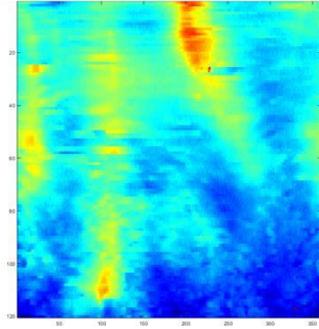
575 Right flipped



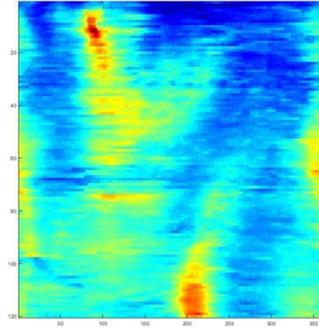
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Adolescent humeri

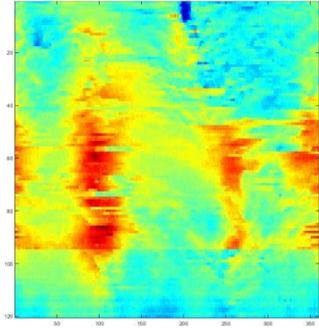
Z4



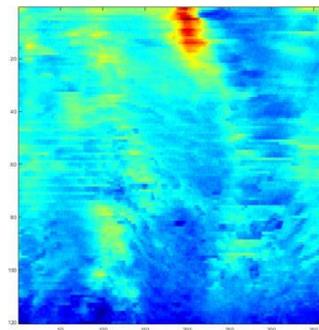
Z1



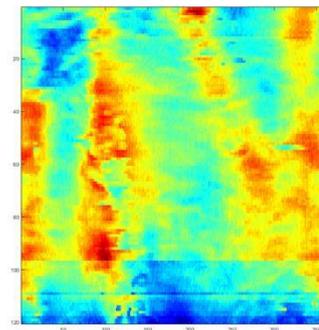
Z2



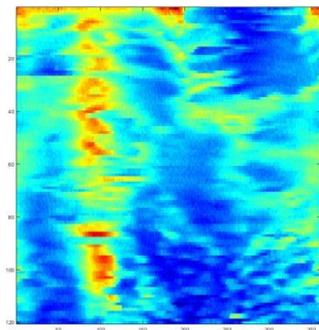
Z3



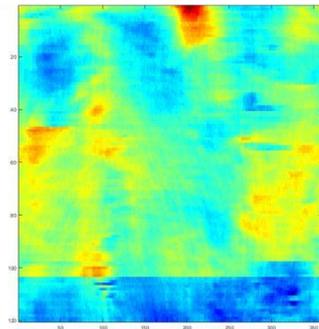
96



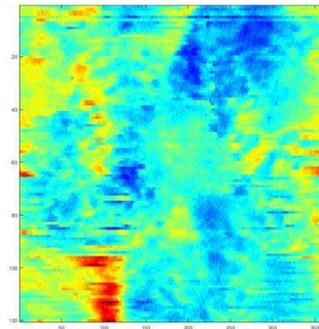
187 R flipped



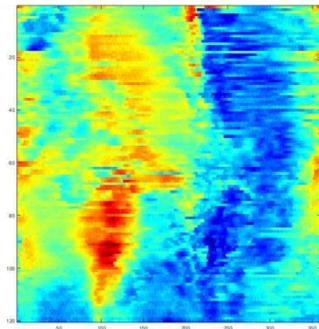
570



573



573 R flipped



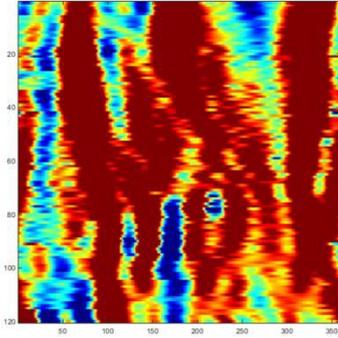
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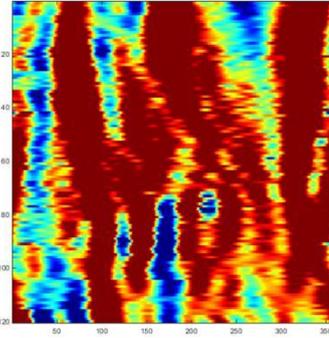
2 1.3 S3. Periosteal curvature maps for all specimens

Foetal/neonatal humeri

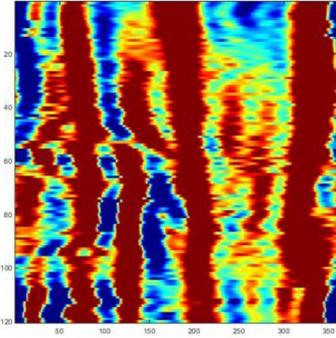
Blackgate 253-2 L humerus



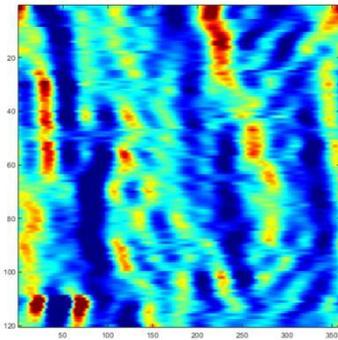
Blackgate 258-2L humerus



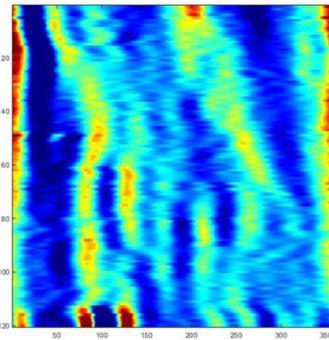
Blackgate 260-1L humerus



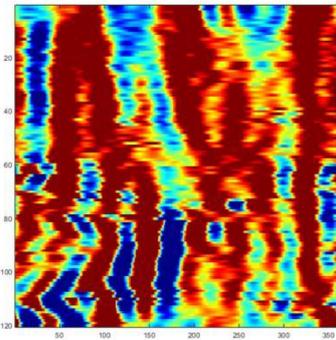
Blackgate 395-2 Left humerus



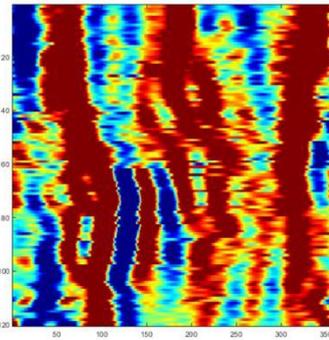
Blackgate 352-2R flipped humerus



Blackgate 364L humerus



Blackgate 508-1L humerus

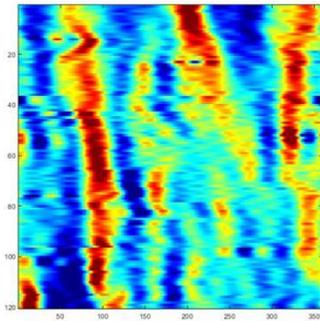


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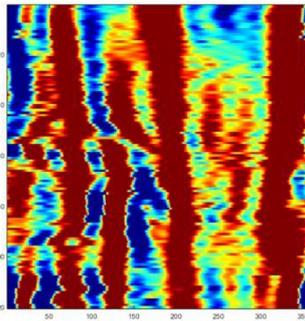
4

Infant-crawling humeri

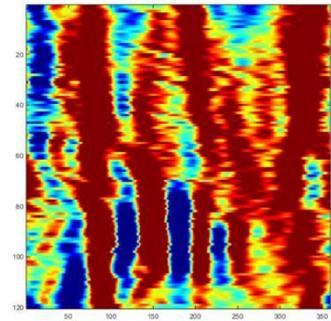
Blackgate 110 humerus



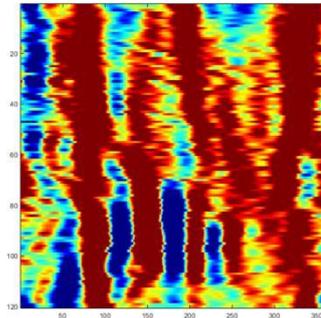
Blackgate 272-2L humerus



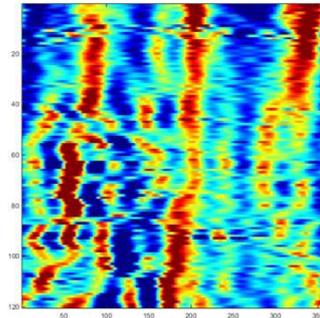
Blackgate 353-1L humerus



Blackgate 353-1 humerus



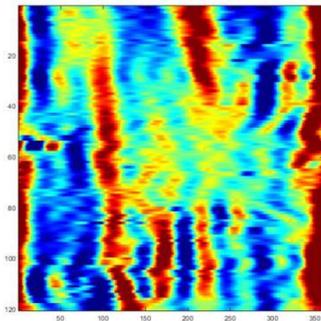
Blackgate 519L humerus



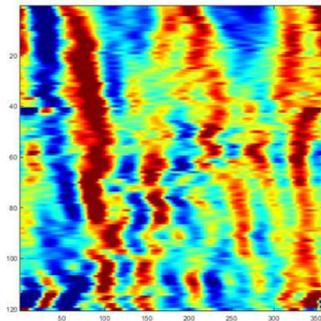
1

Infant-walking humeri

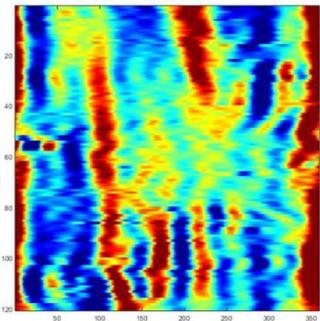
Blackgate 379L humerus



Blackgate 379R flipped humerus



Blackgate 374-1L humerus



2

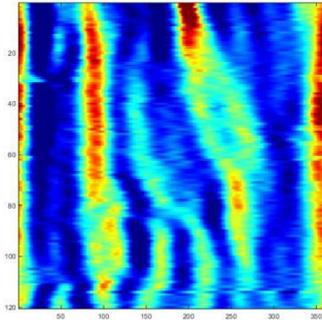
3

4

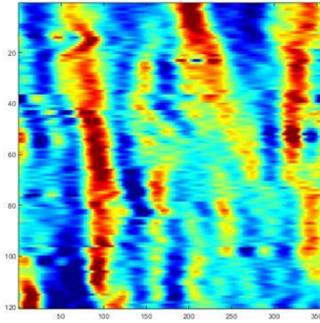
5

Young child humeri

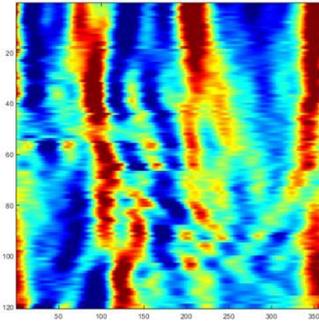
Blackgate 1L humerus



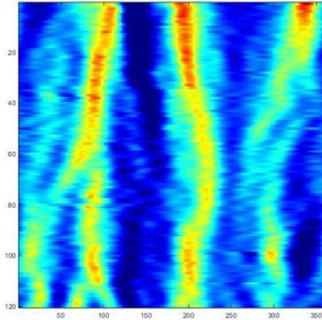
Blackgate 101-1R flipped humerus



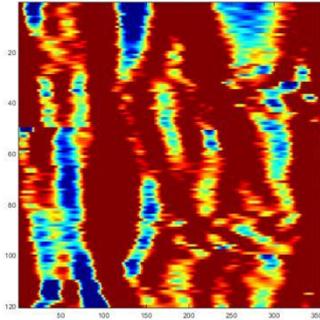
Blackgate 227R Flipped humerus



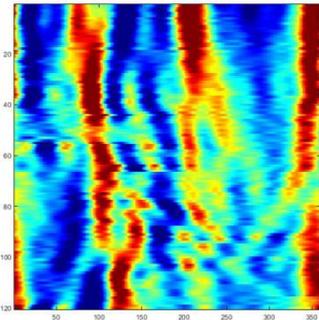
Blackgate 39L humerus



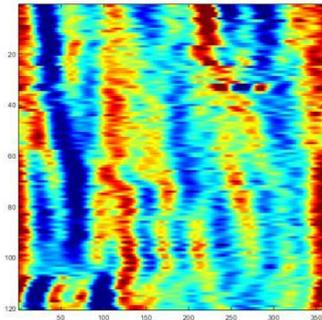
Blackgate 48-1L humerus



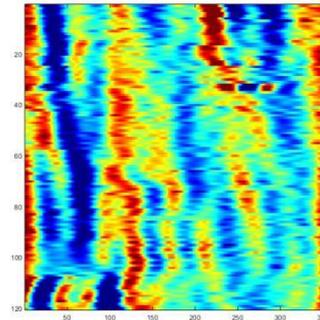
Blackgate 231R flipped humerus



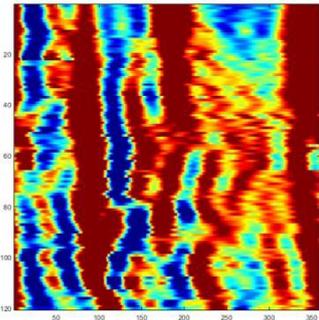
Blackgate 278-1L humerus



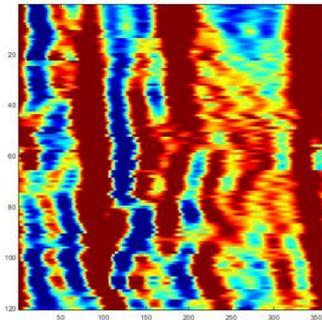
Blackgate 278-2L humerus



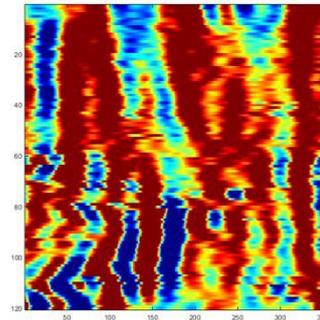
Blackgate 357-2R flipped humerus



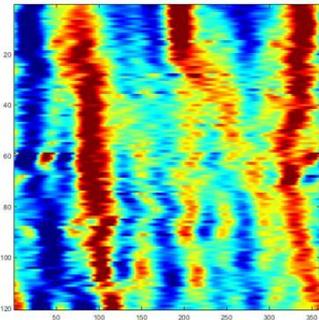
Blackgate 361L humerus



Blackgate 372L humerus



Blackgate 431L humerus



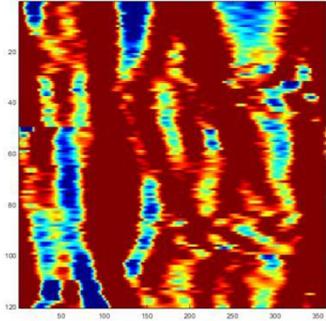
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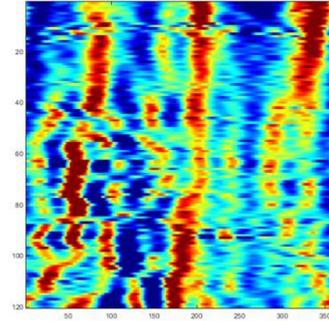
3

1

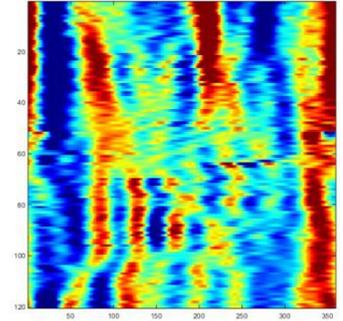
Blackgate 486L humerus



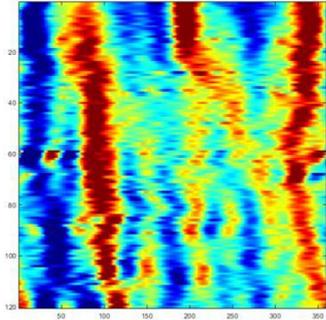
Blackgate 510-2L humerus



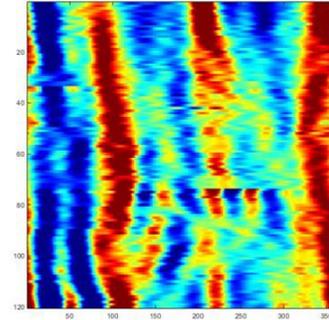
Blackgate 546-1L humerus



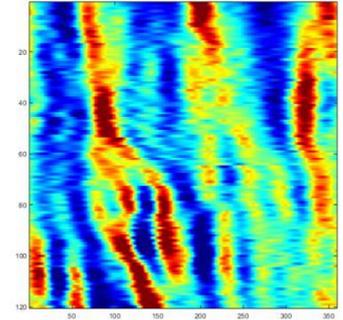
Blackgate 438L humerus



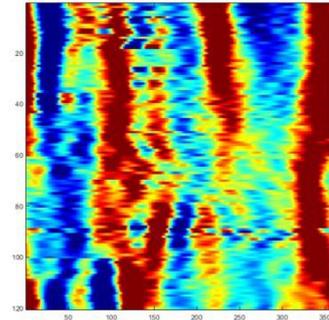
Blackgate 477-2L humerus



Blackgate 574R flipped humerus



Blackgate 584L humerus



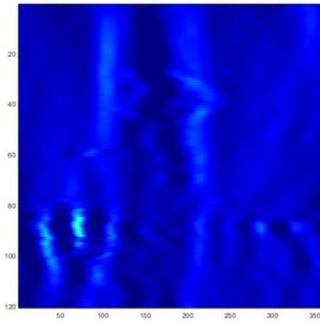
2

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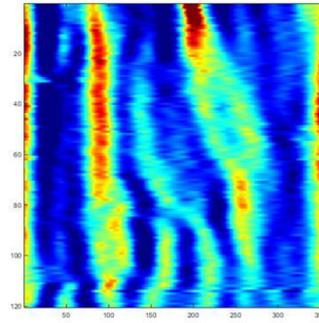
4

Adolescent humeri

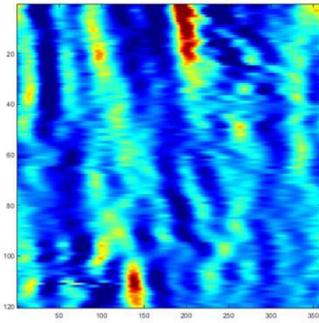
BGZ1 humerus



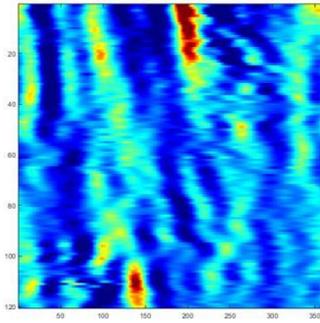
BGz2 humerus



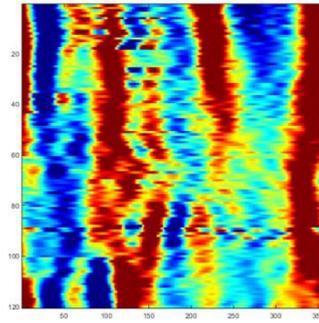
Blackgate Z3 humerus



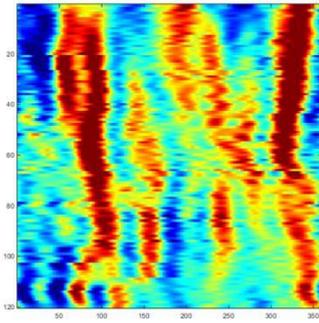
Blackgate Z4 humerus



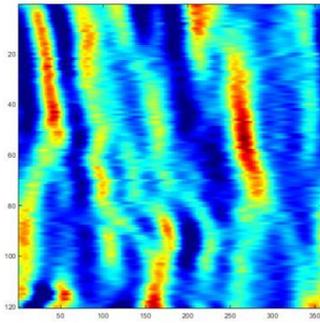
Blackgate 96L humerus



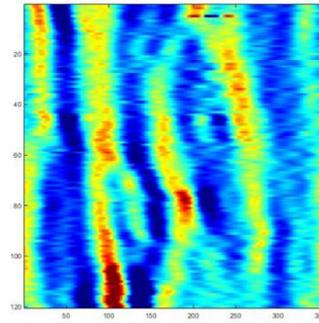
Blackgate 187R flipped humerus



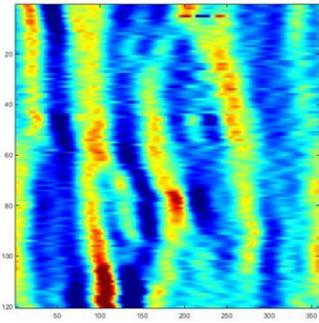
Blackgate 570L humerus



Blackgate 573L humerus



Blackgate 573R flipped humerus



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1 1.4 S4 specimen age estimates and scan parameters

Specimen no.	Age group	new group	Age Estimate*	Original voxel size	No. of slices	Source to object	Source to detector	Resliced Z res. /mm	Length/mm
1	Young	Young	5-6	0.086038	2014	524.4794	1198.746	0.866402	173.3
39	Young	Child	1.5-2.5	0.069528	1723	426.8844	1227.944	0.598986	119.8
48	Young	Young	5-6	0.069528	1590	426.8844	1227.944	0.55275	110.5
48	Child	Child	5-6	0.069528	1590	426.8844	1227.944	0.55275	110.5
96	Adolescent	Adolescent	12-15	0.0574	1462	289.1936	1007.005	0.419594	83.9
96	Adolescent	Adolescent	12-15	0.0574	1462	289.1936	1007.005	0.419594	83.9
101	Young	Infant	1-1.5	0.069528	1665	426.8844	1227.944	0.578823	115.8
110	Child	Infant	1-1.5	0.067141	1415	356.9844	1061.944	0.476143	115.8
110	Infant	Infant	0.5-1.5	0.0673	1415	356.9686	1061.448	0.476148	95.2
135	Older	Older	0.5-1.5	0.097168	1685	591.4686	1217.448	0.820018	95.2
135	Child	Child	6-8	0.086158	1908	507.0458	1178.49	0.819515	164.0
141	Young	Young	4.5-5.5	0.086190	1825	507.0948	1178.77	0.785951	163.9
141	Child	Child	4.5-5.5	0.108038	1265	703.7948	1296.77	0.689071	163.9
171	Infant	Infant	0.5-1	0.108602	1269	703.7958	1296.104	0.685278	137.8
171	Infant	Infant	0.5-1	0.108602	1262	703.7958	1296.104	0.685277	137.8
171	Infant	Infant	0.5-1	0.108602	1262	703.7958	1296.104	0.685277	137.1
187	Adolescent	Adolescent	10-12	0.108602	2005	703.7958	1296.104	1.088733	217.7
227	Young	Young	2.5-3.5	0.080756	1632	478.9878	1186.264	0.658967	131.8
227	Young	Young	2.5-3.5	0.080163	1632	478.9878	1186.264	0.658967	131.8
227	Child	Child	2.5-3.5	0.080756	1632	478.9878	1186.264	0.658967	131.8
231	Young	Young	4.5-5.5	0.086182	1827	507.0945	1178.771	0.785956	157.2
231	Child	Child	4.5-5.5	0.086038	1827	507.0945	1178.771	0.785956	157.2
247	Older	Older	8-9	0.097172	1722	591.4458	1217.49	0.836532	167.3
247	Child	Child	8-9	0.097158	1722	591.4458	1217.49	0.836532	167.3
253	Foetal/Neonate	Foetal/Neonate	36-38 weeks l.u	0.097172	1722	591.4458	1217.49	0.836532	167.3
253	Foetal/Neonate	Foetal/Neonate	36-38 weeks l.u	0.097158	1722	591.4458	1217.49	0.836532	167.3
258	Foetal/Neonate	Foetal/Neonate	36-38 weeks l.u	0.0574	1312	289.1936	1007.005	0.376544	75.3
258	Foetal/Neonate	Foetal/Neonate	36-38 weeks l.u	0.0574	1312	289.1936	1007.005	0.376544	75.3
258	Foetal/Neonate	Foetal/Neonate	36-38 weeks l.u	0.0574	1312	289.1936	1007.005	0.376544	75.3
260	Foetal/Neonate	Foetal/Neonate	1-1.25 MO	0.0574	1312	289.1936	1007.005	0.376544	75.3

	Foetal/Neonate		3-6	0.051	135	261.6	1007.	0.35071	
272	Young Child	Infant	MO	0.086	188	507.0	1178.	0.80918	70.1
278	Young Child	Young Child	5-6	0.038	1	945	771	6	161.8
278	Older Child	Young Child	5-6	0.086	188	507.0	1178.	0.80918	
311	Child	Child	9.5-12.5	0.108	210	703.7	1296.	1.14303	161.8
			32-34 weeks	0.038	134	194.0	1007.	0.25843	228.6
352	Foetal/Neonate	Foetal/Neonate	l.u	0.057	143	289.1	1007.	0.41299	
353	Young Child	Infant	MO	0.057	143	289.1	1007.	0.41299	51.7
353	Young Child	Infant	MO	0.057	143	289.1	1007.	0.41299	82.6
357	Young Child	Foetal/Neonate	0-1	0.044	146	228.4	1034.	0.32422	82.6
361	Child	Young Child	2.5-3.5	0.080	156	478.9	1186.	0.62989	64.8
364	Young Child	Foetal/Neonate	MO	0.064	171	359.8	1123.	0.54779	126.0
372	Child	Infant	1-1.5	0.069	0	926	446	3	70.8
374	Infant	Foetal/Neonate	0-1	0.086	170	507.0	1178.	0.73175	109.6
374	Infant	Foetal/Neonate	0-1	0.086	170	507.0	1178.	0.73175	146.4
379	Infant	Infant	6-9	0.069	135	426.8	1227.	0.46966	146.4
383	Older Child	Older Child	MO	0.108	198	703.7	1296.	1.07841	93.9
383	Older Child	Older Child	8.5-9.5	0.108	198	703.7	1296.	1.07841	215.7
384	Older Child	Older Child	8.5-9.5	0.108	169	703.7	1296.	0.91768	215.7
388	Young Child	Young Child	7-8	0.086	177	507.0	1178.	0.76530	183.5
395	Older Child	Foetal/Neonate	0-1	0.044	151	228.4	1034.	0.33394	153.1
399	Young Child	Young Child	MO	0.064	166	359.8	1123.	0.53465	66.8
406	Young Child	Infant	1.5-2.5	0.080	143	478.9	1186.	0.57901	231.4
431	Young Child	Young Child	5-6	0.064	166	359.8	1123.	0.53465	115.8
438	Young Child	Young Child	5-6	0.069	9	926	446	9	126.5
477	Young Child	Young Child	3.5-4.5	0.069	9	926	446	9	106.9
478	Child	Infant	1-2	0.069	157	426.8	1227.	0.54649	106.9
				0.069	157	426.8	1227.	0.54649	109.3

	Young			0.080	155	478.9	1186.	0.62585	
486	Child	Infant	1.5-2.5	756	0	878	264	7	125.2
	Foetal/Neonate	Foetal/Neonate	0-2	0.051	131	261.6	1007.	0.34214	
508	Older	Older	MO	958	7	095	003	4	68.4
509	Child	Child	5.5-6.5	602	9	982	102	1	176.9
	Young	Young		0.108	172	703.7	1296.	0.93669	
510	Child	Child	5-6	602	5	982	102	4	187.3
			1-3	0.051	138	261.6	1007.	0.36058	
519	Infant	Infant	MO	958	8	095	003	9	72.1
	Young	Young		0.108	161	703.7	1296.	0.87479	
546	Child	Child	4.5-5.5	602	1	982	102	1	175.0
	Young	Young		0.108	161	703.7	1296.	0.87479	
546	Child	Child	4.5-5.5	602	1	982	102	1	175.0
		Young		0.108	161	703.7	1296.	0.87479	
551	Infant	Child	3.5-4.5	602	1	982	102	1	175.0
	Adolescent	Older	9-11	0.108	211	703.7	1296.	1.14629	
568	t	Child	years	602	1	958	104	2	229.3
	Adolescent	Adolescent		0.108	211	703.7	1296.	1.14629	
570	t	t	15-17	602	1	958	104	2	229.3
	Adolescent	Adolescent		0.108	211	703.7	1296.	1.14629	
573	t	t	15-17	602	1	958	104	2	229.3
	Adolescent	Adolescent		0.108	211	703.7	1296.	1.14629	
573	t	t	15-17	602	1	958	104	2	229.3
	Young	Young		0.108	155	703.7	1296.	0.84275	
574	Child	Child	5-6	602	2	982	102	3	168.6
	Older	Older		0.108	175	703.7	1296.	0.95352	
575	Child	Child	11-12	602	6	982	102	8	190.7
	Young	Young	2-3	0.080	153	478.9	1186.	0.61778	
584	Child	Child	years	756	0	878	264	1	123.6

1

2 *Unless otherwise stated-age is in years

1 1.5 *Supplementary figures S5-S7.*

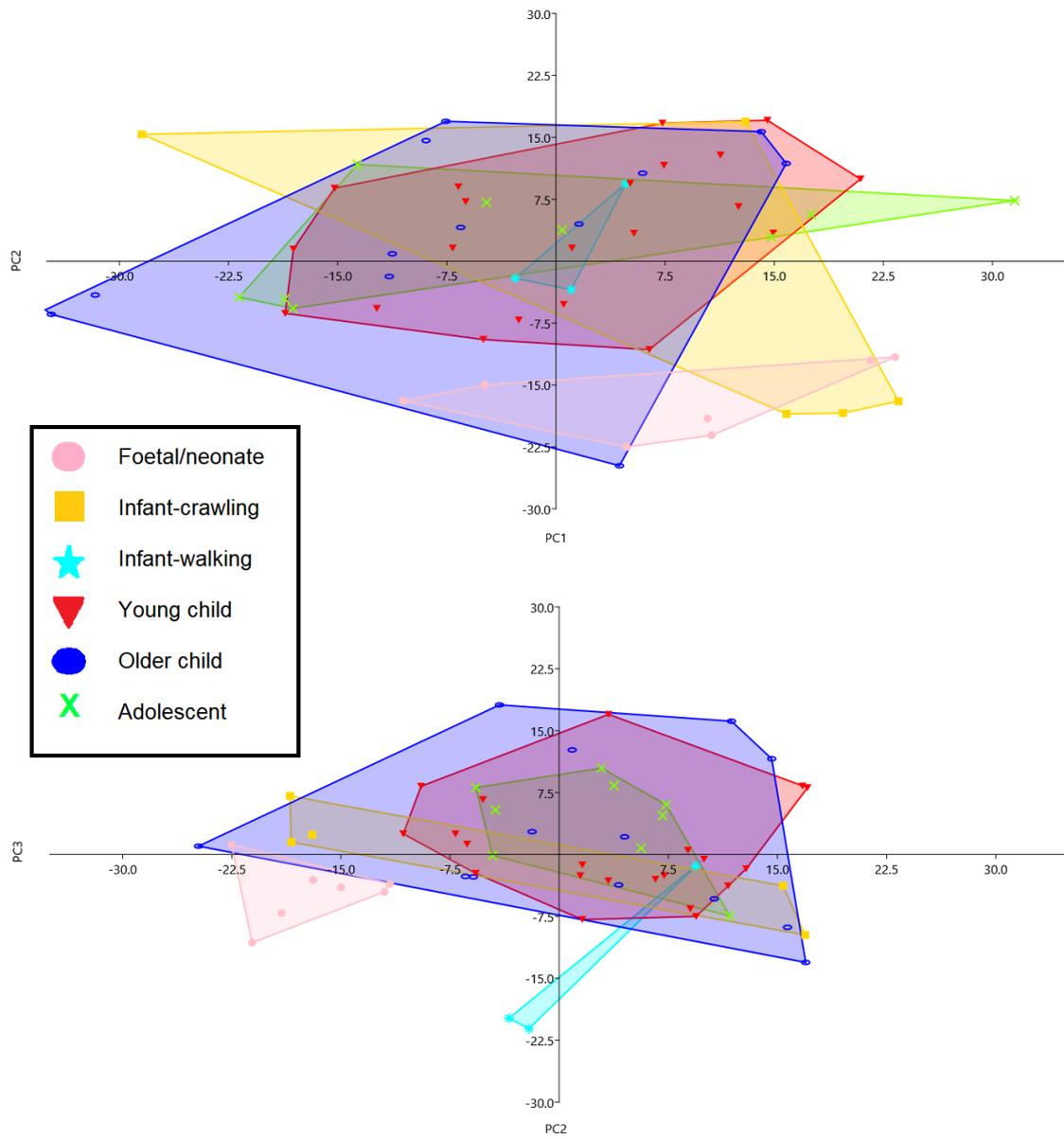
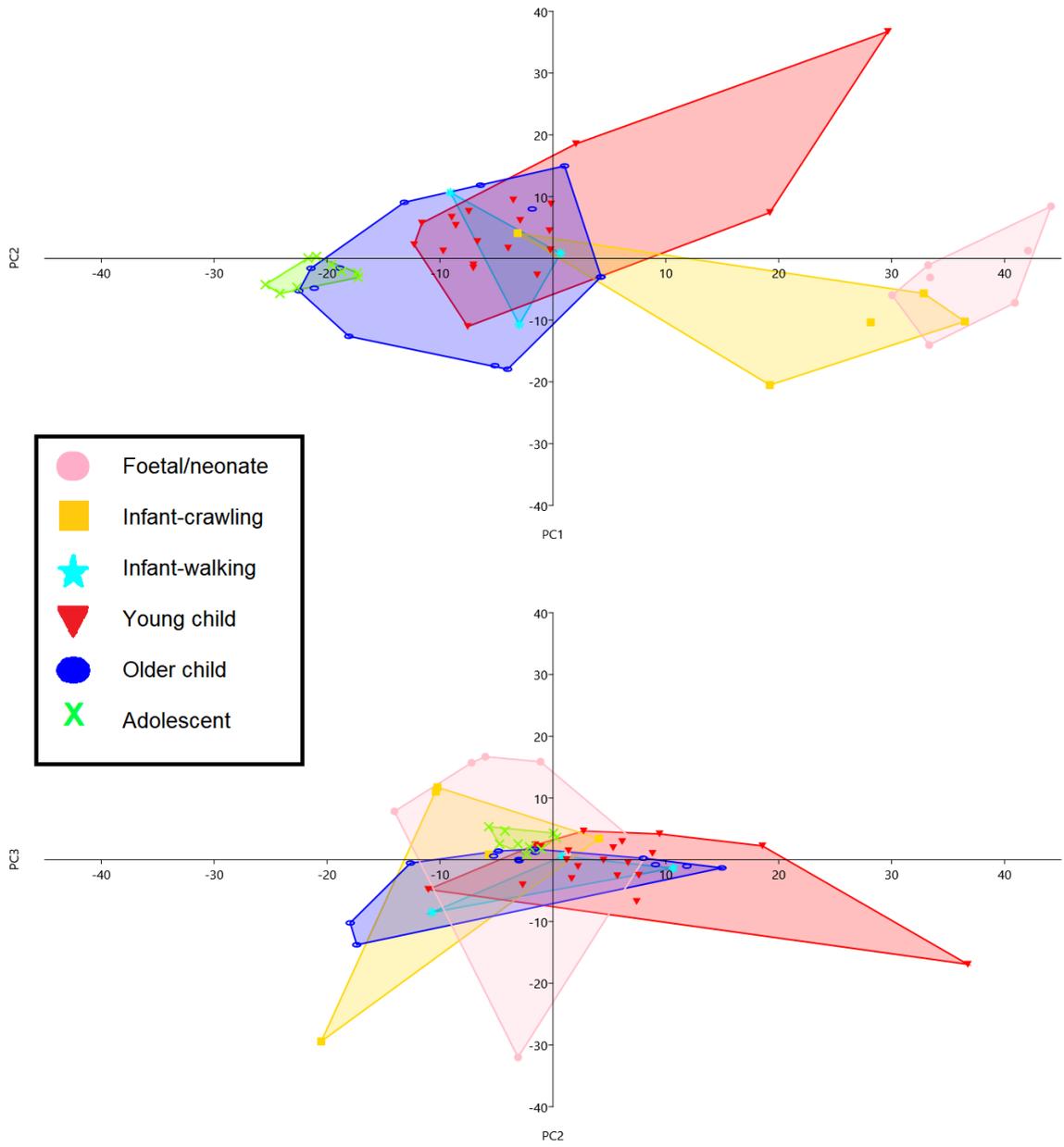


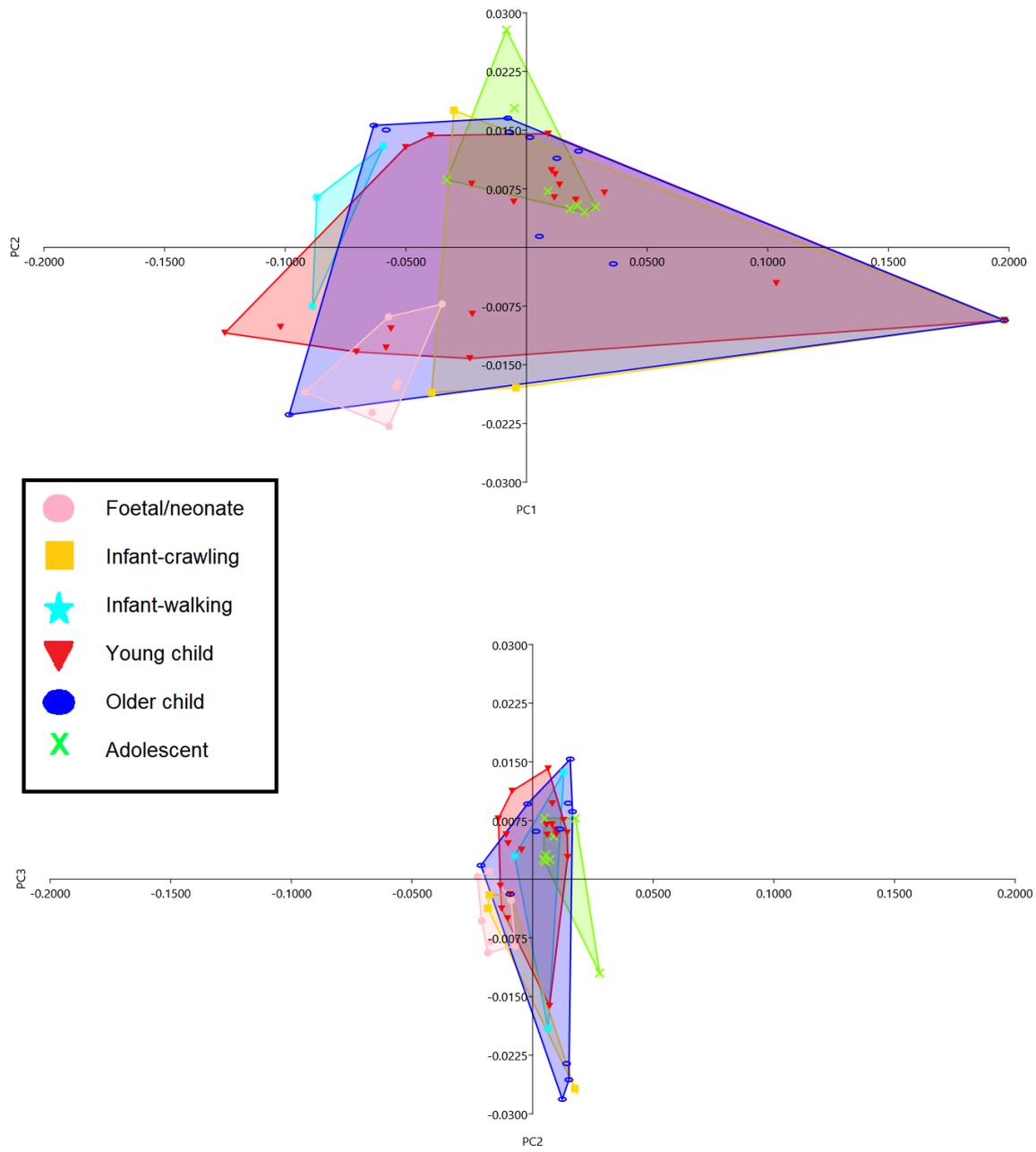
Figure S5. PCA of thickness scores

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Figure S6. PCA of periosteal curvature scores



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Figure S7. PCA of GMM coordinates

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2 1.6 S8. MATLAB code for thickness calculations
3 function calculate_thickness_map
4 % This function looks at all the .tif files in a folder and calculates a thickness map
5 % it assumes that each tiff file is part of an image stack
6 num_samples = 360; % this is the number of samples per revolution, so 360 would give a 1 degree
7 interval
8 slice_subsample = 6; % this is the subsample factor for the innerpoint and outerpoint files
9 sample_subsample = 90; % this is the subsample factor for each slice for the innerpoint and
10 outerpoint files
11 % first get a folder from the user
12 folder_name = uigetdir('', 'Choose the folder that contains the image stack'); if
13 folder_name == 0 error('No folder selected');
14 end
15 %
16 %save_name = uigetdir('', 'Choose the folder to save results into');
17 %if save_name == 0
18 %error('No folder selected');
19 %end
20 % Change the code below to the directory you want to save the results to if
21 ~exist(['C:\Users\~\'], 'dir') mkdir(['C:\Users\~\']) end
22 save_name = 'C:\Users\mqbpkto2\Dropbox (The University of Manchester)\Thesis
23 chapters\thickness mapping\JULY18'
24
25 file_list = dir(fullfile(folder_name, '*.tif')); if
26 isempty(file_list)
27 error('No .tif files found in folder')
28 end
29 %this code will automatically read a csv with metadata in. Change the columns below to %reflect
30 where your voxel sizes are
31 excel_file_list = dir(fullfile(folder_name, '*metadata.csv')); if
32 isempty(excel_file_list) error('No .csv files found in
33 folder')
34 end
35 for file_number = 1:length(excel_file_list) file_name =
36 [folder_name '/' excel_file_list(file_number).name]; metadata =
37 xlsread(file_name);
38 end mm_per_pixel =
39 metadata(2) slice_thickness =
40 metadata(3)
41 %This dialogue lets you tell Matlab the dimensions of your file.
42 %response = inputdlg({'X-Y resolution in mm', 'Z resolution in mm'}, 'Image Resolution', [1 50; 1
43 50]);
44 %if isempty(response)
45 % error('The size of each image pixel must be specified')
46 %end
47
48 %mm_per_pixel = str2double(response{1});

```

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1  %slice_thickness = str2double(response{2});
2  %this dialogue lets you input the start and end percentage for your sequence. %This
3  means that you can just leave all your images in the folder, and not %worry about
4  moving the unwanted slices to another folder.
5  %responseb = inputdlg('Start %','end %', 'Image Start and End Percent', [1 50; 1 50]);
6  %if isempty(responseb)
7      %error('The start and end Percentage must be specified')
8  %end
9  %start_image = str2double(responseb{1});
10 %end_image = str2double(responseb{2});
11 % or you can alter this code below, if you are going to be doing the same set of measurements
12 repeatedly start_image = 40; end_image = 160; start_perc = start_image;
13 end_perc = end_image;
14
15 %start_image = round((length(file_list)/100)*(str2double(responseb{1})));
16 %end_image = round((length(file_list)/100)*(str2double(responseb{2})));
17 %start_image = (round((length(file_list)/100)*(start_perc)));
18 %end_image = round((length(file_list)/100)*(end_perc));
19 file_numbers = end_image - start_image; file_list_subsample =
20 file_list(start_image:end_image); if ~exist([save_name
21 '\outerpoints\'],'dir') mkdir([save_name '\outerpoints\']) end
22 if ~exist([save_name '\innerpoints\'],'dir')
23 mkdir([save_name '\innerpoints\']) end
24 if ~exist([save_name '\slice_geometry\'],'dir')
25 mkdir([save_name '\slice_geometry\']) end
26 if ~exist([save_name '\outerpoints_subsample\'],'dir')
27 mkdir([save_name '\outerpoints_subsample\']) end
28 if ~exist([save_name '\thickness\'],'dir')
29 mkdir([save_name '\thickness\']) end
30 if ~exist([save_name '\innerpoints_subsample\'],'dir')
31 mkdir([save_name '\innerpoints_subsample\']) end
32 if ~exist([save_name '\thickness_plots\'],'dir')
33 mkdir([save_name '\thickness_plots\']) end
34 if ~exist([save_name '\thickness_images\'],'dir')
35 mkdir([save_name '\thickness_images\']) end
36 if ~exist([save_name '\J\'],'dir')
37 mkdir([save_name '\J\']) end
38 if ~exist([save_name '\CA\'],'dir')
39 mkdir([save_name '\CA\']) end
40 if ~exist([save_name '\Ix_Iy\'],'dir')
41 mkdir([save_name '\Ix_Iy\']) end
42 if ~exist([save_name '\Imax_Imin\'],'dir')
43 mkdir([save_name '\Imax_Imin\']) end
44 %thickness_image = zeros(num_samples,(length(end_image-start_image)));
45 thickness_image = zeros(file_numbers, num_samples);
46
47 [pathstr, name, ext] = fileparts(folder_name);

```

```

1  outerpoints_file = fopen([save_name '\outerpoints\' name '_outerpoints.csv'], 'w'); innerpoints_file =
2  fopen([save_name '\innerpoints\' name '_innerpoints.csv'], 'w'); outerpoints_subsample_file =
3  fopen([save_name '\outerpoints_subsample\' name
4  '_outerpoints_subsample.csv'], 'w');
5  innerpoints_subsample_file = fopen([save_name '\innerpoints_subsample\' name
6  '_innerpoints_subsample.csv'], 'w');
7  J_file = fopen([save_name '\J\' name '_J.csv'], 'w');
8  CA_file = fopen([save_name '\CA\' name '_CA.csv'], 'w');
9  Ix_Iy_file = fopen([save_name '\Ix_Iy\' name '_Ix_Iy.csv'], 'w');
10 Imax_Imin_file = fopen([save_name '\Imax_Imin\' name '_Imax_Imin.csv'], 'w'); centroids_file =
11 fopen([save_name '\slice_geometry\' name '_slice_geometry.csv'], 'w'); fprintf(centroids_file, 'slice,
12 centroid_x, centroid_y, min_thickness, max_thickness, TA, Cortical area, Trabecular area, J, Ix/Iy,
13 Imax/Imin\n', 'w');
14 fprintf(J_file, 'slice, J\n', 'w'); fprintf(CA_file, 'slice,
15 CA\n', 'w'); fprintf(Ix_Iy_file, 'slice, Ix/Iy\n', 'w');
16 fprintf(Imax_Imin_file, 'slice, Imax/Imin\n', 'w');
17 %thickness_file = fopen([save_name '\thickness\' name '_thickness.csv'], 'w');
18
19 for slice_counter = 1: length(file_list_subsample);
20
21     current_file = fullfile(folder_name, file_list_subsample(slice_counter).name);    fprintf('%s\n',
22     current_file);
23
24     [thickness, thickness_start, thickness_end, centroid_x, centroid_y] =
25     calculate_thickness(current_file, num_samples);    thickness = thickness .*
26     mm_per_pixel;    thickness_start = thickness_start .* mm_per_pixel;
27     thickness_end = thickness_end .* mm_per_pixel;    centroid_x = centroid_x
28     .* mm_per_pixel;    centroid_y = centroid_y .* mm_per_pixel;
29     max_thickness = max(thickness);
30     min_thickness = min(thickness);
31
32 %these following formulae calculate conventional cross sectional properties.    TotalA =
33 (polyarea(thickness_end(1:1,1:360), thickness_end(2:2,1:360)));
34 TrabA = (polyarea(thickness_start(1:1,1:360), thickness_start(2:2,1:360)));
35 Cortical_area = TotalA - TrabA;
36 %find Imax    distances = sqrt((thickness_end(1:1,1:360) -
37 centroid_x).^2 + (thickness_end(2:2,1:360) - centroid_y).^2);
38 [maxRadius, maxRadiusIndex] = max(distances);    maxPointCoord =
39 thickness_end(:, maxRadiusIndex);    maxPointCoordiner =
40 thickness_start(:, maxRadiusIndex);    opp_point = maxRadiusIndex + 180;
41 if opp_point > 360    opp_point =
42 opp_point - 360
43 else
44     opp_point = opp_point
45 end
46 opp_pointCoord = thickness_end(:, opp_point);
47 opp_pointCoordiner = thickness_start(:, opp_point);    %extract Imax

```

```

1   Imax = sqrt((((maxPointCoord(1))-
2 (opp_pointCoord(1)).^2)+((((maxPointCoord(2))(opp_pointCoord(2))).^2)))));
3   Imax_inner = sqrt((((maxPointCoordiner(1))-
4 (opp_pointCoordiner(1)).^2)+((((maxPointCoordiner(2))-(opp_pointCoordiner(2))).^2)))));
5   %find Imin
6   [minRadius, minRadiusIndex] = min(distances);   minPointCoord =
7 thickness_end(:,minRadiusIndex);   minPointCoordiner =
8 thickness_start(:,minRadiusIndex);   opp_pointmin =
9 minRadiusIndex+180;
10  if opp_pointmin>360
11      opp_pointmin = opp_pointmin-360   else
12      opp_pointmin = opp_pointmin   end
13  opp_pointminCoord = thickness_end(:,opp_pointmin);   opp_pointminCoordiner =
14 thickness_start(:,opp_pointmin);
15  %extract Imin
16  Imin = sqrt(((minPointCoord(1))-(opp_pointminCoord(1))).^2)+((((minPointCoord(2))-
17 (opp_pointminCoord(2))).^2)));
18  Imin_inner = sqrt(((minPointCoordiner(1))-
19 (opp_pointminCoordiner(1)).^2)+((((minPointCoordiner(2))-
20 (opp_pointminCoordiner(2))).^2)));
21
22  %extract max and min second moments of area
23  Second_moment_of_area_min = (pi*((Imin^4)-(Imin_inner^4))/32
24  Second_moment_of_area_max = (pi*((Imax^4)-(Imax_inner^4))/32
25
26  %extractImax/Imin for circularity measure
27  Ix_Iy = Imax/Imin;
28  %extract J
29  J = Second_moment_of_area_min+Second_moment_of_area_max;
30  %Extract moments of area divided
31  Imax_Imin = Second_moment_of_area_max/Second_moment_of_area_min;
32
33  fprintf('Max thickness = %f\n', max_thickness);   fprintf('Min
34 thickness = %f\n', min_thickness);
35  %fprintf('TA = %f\n', TotalA);
36  %fprintf('Cortical area = %f\n', Cortical_area);
37  %fprintf('Trabecular area = %f\n', TrabA);
38  %fprintf('J = %f\n', J);
39  %fprintf('Ix/Iy = %f\n', Ix_Iy);
40  %fprintf('Imax/Imin = %f\n', Imax_Imin);
41
42  fprintf(centroids_file, '%d,%g,%g,%g,%g,%g,%g,%g,%g,%g\n', slice_counter, centroid_x,
43 centroid_y, min_thickness, max_thickness, TotalA, Cortical_area, TrabA, J, Ix_Iy, Imax_Imin);
44  fprintf(J_file, '%d, %g\n', slice_counter, J);
45  fprintf(CA_file, '%d, %g\n', slice_counter, Cortical_area);   fprintf(Ix_Iy_file,
46 '%d, %g\n', slice_counter, Ix_Iy);
47  fprintf(Imax_Imin_file, '%d, %g\n', slice_counter, Imax_Imin);
48

```

```

1
2
3     thickness_image(slice_counter, :) = thickness;
4
5
6     for sample_counter = 1: length(thickness_start);
7         fprintf(innerpoints_file, '%d,%g,%g\n', (slice_counter*slice_thickness), thickness_start(1,
8 sample_counter), thickness_start(2, sample_counter));
9         fprintf(outerpoints_file, '%d,%g,%g\n', (slice_counter*slice_thickness), thickness_end(1,
10 sample_counter), thickness_end(2, sample_counter));
11         fprintf(thickness_file, thickness);
12         if (mod(slice_counter, slice_subsample) == 0 && mod(sample_counter, sample_subsample) ==
13 0)
14             fprintf(innerpoints_subsample_file, '%d,%g,%g\n', slice_counter.*slice_thickness,
15 thickness_start(1), thickness_start(2));
16             fprintf(outerpoints_subsample_file, '%d,%g,%g\n', slice_counter.*slice_thickness,
17 thickness_end(1), thickness_end(2));     end
18
19     end
20
21 end
22
23 fclose(outerpoints_file); fclose(innerpoints_file);
24 fclose(outerpoints_subsample_file);
25 fclose(innerpoints_subsample_file);
26 fclose(centroids_file);
27 fclose(CA_file); fclose(J_file);
28 fclose(Ix_Iy_file);
29 fclose(Imax_Imin_file);
30
31 %thickness_image2 = thickness_image(start_image:end);
32 % write the thickness data to a CSV file
33 %csvwrite((fullfile([folder_name] 'thickness_output.csv'), thickness_image);
34 %[pathstr, name, ext] = fileparts(folder_name);
35 %csvwrite([save_name '\thickness\' name 'thickness2.csv'], thickness_image2);
36 %csvwrite([save_name '\thickness\' name 'thickness.csv'], thickness_image);
37
38 % produce a suitable image of the thickness map
39
40 graph_title1 = ('Cortical thickness of '); graph_title2 = ('
41 humerus. Colour scale is in mm'); graph_bone =
42 (excel_file_list.name(1:end-12)); %graph_bone2 =
43 graph_bone(1:end-12);
44 graph_title = [graph_title1, graph_bone, graph_title2];
45 [pathstr, name, ext] = fileparts(folder_name); figure(1);
46 clf('reset'); set(gcf, 'Color', 'w'); set(gcf, 'Units', 'pixels'); set(gcf,
47 'Position', [50, 50, 1000, 1000]);

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```

1  set(gcf,'PaperType','<custom>'); set(gcf,'Units','inches'); set(gcf,'PaperUnits','inches'); position =
2  get(gcf,'Position'); set(gcf,'PaperPosition',[0,0,position(3:4)]); set(gcf,'PaperSize',position(3:4));
3  imagesc(thickness_image); colormap(jet(256));
4  %axes1 = axes('Parent',figure(1),...
5      %'XTickLabel',{'Anterior','Medial','Posterior','Lateral','Anterior'},...
6      % 'XTick',[0 90 180 270 360],...
7      %'Layer','top',...
8      %'YDir','reverse',...
9      %'YTick',zeros(1,0));
10 %% Uncomment the following line to preserve the X-limits of the axes
11 % xlim(axes1,[0.5 360.5]);
12 %% Uncomment the following line to preserve the Y-limits of the axes
13 % ylim(axes1,[0.5 4.5]);
14 %box(axes1,'on');
15 %hold(axes1,'on');
16
17 % Create image
18 %image(cdata1,'Parent',axes1,'CDataMapping','scaled');
19
20 % Create xlabel
21 xlabel('Bone Position');
22
23 % Create ylabel
24 ylabel({'Distal to proximal humerus.});
25
26 % Create title title(graph_title);
27 % Create colorbar colorbar('EastOutside'); % Create arrow
28 annotation('arrow',[0.0613750000000001 0.0593750000000001],...
29     [0.922330097087376 0.107142857142857]); set(gca,
30     'XTick',[0 90 180 270 360]);
31     'XTickLabel',{'Anterior','Medial','Posterior','Lateral','Anterior'},...
32     plot_name = fullfile(folder_name, 'thickness_plot');
33     print(gcf,'-dpdf',[save_name '\thickness_plots\' name 'thickness plot', '.pdf'],'-r 150) print(gcf,'-
34     depsc2',[save_name '\thickness_plots\' name 'thickness plot', '.eps'],'-r 150) print(gcf,'-
35     dtiff',[save_name '\thickness_plots\' name 'thickness plot', '.png'],'-r 72) figure(2);
36     clf('reset'); set(gcf, 'Color', 'w'); set(gcf,'Units','pixels'); set(gcf,
37     'Position', [50, 50, 1000, 1000]);
38     set(gcf,'PaperType','<custom>'); set(gcf,'Units','inches'); set(gcf,'PaperUnits','inches'); position =
39     get(gcf,'Position'); set(gcf,'PaperPosition',[0,0,position(3:4)]); set(gcf,'PaperSize',position(3:4));
40     imagesc(thickness_image); colormap(jet(256));
41     plot_name2 = fullfile(folder_name, 'thickness_image');
42     print(gcf,'-dpdf',[save_name '\thickness_images\' name 'thickness_image', '.pdf'],'-r 150) print(gcf,'-
43     depsc2',[save_name '\thickness_images\' name 'thickness_image', '.eps'],'-r 150) print(gcf,'-
44     dtiff',[save_name '\thickness_images\' name 'thickness_image', '.png'],'-r 72)
45
46 % ask if the thickness file should be saved somewhere %[pathstr,
47 name, ext] = fileparts(folder_name); default_name = [name,
48 '_thickness.csv'];

```

```

1  %[file_name, path_name] = uiputfile('*.csv', 'Save the thickness image', default_name);
2  %if file_name ~= 0
3      %csvwrite(fullfile(path_name, file_name), thickness_image); return
4  function [thickness, thickness_start, thickness_end, centroid_x, centroid_y] =
5  calculate_thickness(current_file, num_samples)
6
7  % this function calculates the thickness of the bone wall
8  % it produces num_samples values from angle zero to 360
9  % zero angle is aligned with the X axis and increases counterclockwise
10
11 % read the image data =
12 imread(current_file); [height,
13 width, channels] = size(data);
14
15 % now do some sanity checking on the image
16 if channels ~= 1
17     error('Only greyscale images supported'); end
18
19 if data(1, 1) ~= data(1, width) || data(1, 1) ~= data(height, width) || data(1, 1) ~= data(height, 1)
20     error('All 4 corners of the image must have the same greyscale value'); end
21
22 background = data(1, 1);
23
24 % find the centroid xsum
25 = 0; ysum = 0; count = 0;
26 for ix = 1: width    for iy
27 = 1: height
28     if data(iy, ix) ~= background
29 xsum = xsum + ix;      ysum = ysum
30 + iy;      count = count + 1;
31     end
32     end end
33 if count == 0 % must be a completely blank image so set all the thicknesses to zero
34 fprintf('Centroid not found\n'); thickness = zeros(1, file_numbers); return end
35 centroid_x = xsum / count; centroid_y =
36 ysum / count;
37 fprintf('Centroid x = %f y = %f\n', centroid_x, centroid_y);
38 % now work radially around from centroid
39 thickness = 9999 * ones(1, num_samples); % create a suitable row vector to hold the thicknesses using
40 dummy big values
41 thickness_start = zeros(2, num_samples);
42 thickness_end = zeros(2, num_samples); for i = 1:
43 num_samples
44     circle_fraction = (i - 1) / num_samples;
45 angle = 2 * pi() * circle_fraction; del_x =
46 cos(angle); del_y = sin(angle); % look for
47 the inner edge

```

```

1     for r = 0: 0.5: max([width, height]) % the 0.5 here gets us around any potential rounding error
2     problems
3         x = r * del_x + centroid_x;    y
4     = r * del_y + centroid_y;    ix =
5     round(x);    iy = round(y);
6         if (ix < 1 || ix > width || iy < 1 || iy > height)
7             % if we can't find the inner edge then there is a complete hole here so set the thickness to zero
8             thickness(i) = 0;
9             break;
10        end
11        if data(iy, ix) ~= background % found the inner edge
12        thickness_start(1, i) = ix;    thickness_start(2, i) = iy;
13            break;    end
14    end    if thickness(i) ~=
15    0
16        % look for the outer edge
17        for r = max([width, height]): -0.5: 0 % the -0.5 here gets us around any potential rounding error
18        problems
19            x = r * del_x + centroid_x;
20        y = r * del_y + centroid_y;    ix
21        = round(x);    iy = round(y);
22            if (ix < 1 || ix > width || iy < 1 || iy > height)
23                continue; % this isn't an error, we just haven't found the edge of the image yet
24        end
25            if data(iy, ix) ~= background % found the outer edge
26        thickness_end(1, i) = ix;    thickness_end(2, i) = iy;
27            break;
28        end    end
29        % if the outer edge is the same as the inner edge it means that the radial line has met at the same
30        pixel
31        % so in fact the distance between the outer edge and inner edge is always 1 pixel too small so
32        %we need to correct for this
33        thickness(i) = 1 + sqrt((thickness_end(1, i) - thickness_start(1, i))^2 + (thickness_end(2, i) -
34        thickness_start(2, i))^2);
35
36    end
37
38    end
39
40    return
41
42
43
44

```

1 **1.7 S9. MATLAB code for periosteal curvature calculations**

```
2     function k_fouriercurvature

3     %subsample = 10
4
5     % read the csv folder containing the outline coordinates for each stack
6     folder_name = uigetdir('', 'Choose the folder that contains the image stack'); if
7     folder_name == 0     error('No folder selected');
8     end
9     file_list = dir(fullfile(folder_name, '*.csv')); if
10    isempty(file_list)
11        error('No .csv files found in folder')
12    end
13    %make a subdirectory for each output to be saved in.
14    if ~exist([folder_name '\curvature_rawpoints\'],'dir')
15        mkdir([folder_name '\curvature_rawpoints\']) end
16    if ~exist([folder_name '\curvature_heatmap\'],'dir')
17        mkdir([folder_name '\curvature_heatmap\']) end
18    if ~exist([folder_name '\curvature_2dgraph\'],'dir')
19        mkdir([folder_name '\curvature_2dgraph\']) end
20    if ~exist([folder_name '\curvature_values\'],'dir')
21        mkdir([folder_name '\curvature_values\']) end
22    if ~exist([folder_name '\smoothed_values\'],'dir')
23        mkdir([folder_name '\smoothed_values\']) end
24
25    for file_number = 1:length(file_list)
26
27        file_name = [folder_name '/' file_list(file_number).name];
28        [pathstr, name, ext] = fileparts(file_name);
29        file_name2 = [folder_name '\curvature_values\' file_list(file_number).name(1:end-4)
30        'curvature.csv'];
31        file_name3 = [folder_name '\smoothed_values\' file_list(file_number).name(1:end-4) 'smoothed
32        outline.csv'];
33        heatmap_name = [folder_name '\curvature_heatmap\' file_list(file_number).name(1:end-4)
34        'curvature_heatmap'];
35        smoothoutline_name = [folder_name '\curvature_2dgraph\' file_list(file_number).name(1:end-4)
36        'curvature_smoothed'];
37        outline_name = [folder_name '\curvature_rawpoints\' file_list(file_number).name(1:end-4)
38        'original_curvature'];
39        graph_bone_name = [name(1:end-12)];
40        fourierpoints = csvread(file_name);
41
42        slice_number = fourierpoints(:, 1); x_list =
43        fourierpoints(:, 2);
44        y_list = fourierpoints(:, 3);
45
```

```

1  % count the number of points in a slice
2  points_per_slice = 1; for i = 1:
3  length(slice_number) - 1  if (slice_number(i +
4  1) ~= slice_number(i))  break;  end
5  points_per_slice = points_per_slice + 1; end
6
7  slice_number = reshape(slice_number, [points_per_slice, length(slice_number) / points_per_slice]);
8  % this reshape needs checking
9  x_list = reshape(x_list, [points_per_slice, length(x_list) / points_per_slice]); y_list =
10 reshape(y_list, [points_per_slice, length(y_list) / points_per_slice]);
11
12 [r, c] = size(slice_number); num_slices =
13 c; num_points_wanted = 360;
14 k_map = zeros(num_slices, num_points_wanted);
15 l = zeros(num_slices*num_points_wanted,3);
16 for i = 1:3  figure(i)  clf('reset');  set(gcf,
17 'Color', 'w');  set(gcf,'Units','pixels');
18 set(gcf, 'Position', [i + 50, i + 50, 1000, 1000]); end
19
20
21 for slice = 1: num_slices
22 x = x_list(1:points_per_slice, slice);
23 y = y_list(1:points_per_slice, slice);
24
25 figure(1);  plot(x,
26 y);
27 hold on;
28 plot_name3 = outline_name;
29 title(['Original endosteal contour of ' graph_bone_name ' humerus from a  $\mu$ CT scan']);
30 xlabel('X'); ylabel('Y');
31 %print(gcf,'-dtiff',[plot_name3, '.png'],'-r 72');
32 %print({(gcf'-dtiff', plot_name3, '.png')} '-r 72');
33 %print(gcf,'-depsc2','.eps')
34 %hold off;
35 %print(gcf,'-dtiff',[plot_name3, '.png'],'-r 72')
36
37
38 outline = [x, y];
39 iNoOfHarmonicsAnalyse = points_per_slice / 2;
40 bNormaliseSizeState = 0;  bNormaliseOrientationState
41 = 0;
42 rFSDs = fEfourier(outline, iNoOfHarmonicsAnalyse, bNormaliseSizeState,
43 bNormaliseOrientationState);
44
45 % the degree of smoothing depends on the number of harmonics we choose
46 iNoOfHarmonicsReconstruct = 10;  iNoOfPointsReconstruct =
47 num_points_wanted;
48 smoothed_outln = rEfourier(rFSDs, iNoOfHarmonicsReconstruct, iNoOfPointsReconstruct);

```

```

1
2
3     %%% Jamie added in bit to output smoothed_outln variable
4 smoothed_outln_stored(:,2*slice-1) = smoothed_outln(:,1); smoothed_outln_stored(:,2*slice) =
5 smoothed_outln(:,2);
6
7     if slice == num_slices
8         %B = reshape(smoothed_outln_stored,[],2)
9         csvwrite([file_name(1:end-4) '_smoothed_outln.csv'],smoothed_outln_stored)
10        %csvwrite([file_name(1:end-4) '_smoothed_outln2.csv'],B) end
11    if slice == num_slices
12        B = reshape(smoothed_outln_stored,[],2)
13        csvwrite([file_name(1:end-4) '_smoothed_outln2.csv'],B) end
14
15    %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
16    %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
17
18    %l_map(slice, :) = smoothed_outln; figure(2);
19    plot(smoothed_outln(:, 1), smoothed_outln(:, 2)); hold
20    on;
21    k_coeff = calc_k_coefficient(smoothed_outln(:, 1), smoothed_outln(:, 2)); k_map(slice,
22    :) = k_coeff;
23
24    title(['Smoothed endosteal contour of ' graph_bone_name ' humerus from a  $\mu$ CT scan']); xlabel('X');
25    ylabel('Y');
26    plot_name2 = smoothoutline_name;
27    %print(gcf,'-dtiff',[plot_name2, '.png'],'-r 72'); end
28    print(gcf,'-dtiff',[plot_name2, '.png'],'-r 72')
29    print(gcf,'-dtiff',[plot_name3, '.png'],'-r 72')
30    figure(3) clf('reset'); set(gcf, 'Color', 'w');
31    set(gcf,'Units','pixels');
32    set(gcf, 'Position', [50, 50, 1000, 1000]); imagesc(k_map);
33
34    set(gcf,'PaperType','<custom>');
35    set(gcf,'Units','inches');
36    set(gcf,'PaperUnits','inches'); position =
37    get(gcf,'Position');
38    set(gcf,'PaperPosition',[0,0,position(3:4)]);
39    set(gcf,'PaperSize',position(3:4)); plot_name =
40    [heatmap_name];
41    colormap(jet(256));
42    colorbar('EastOutside'); xlabel('Bone
43    Position'); ylabel({'Slice
44    number.','Lower numbers are more
45    proximal'}); title(['Surface curvature of '
46    graph_bone_name ' humerus']);
47    %print(gcf,'-dtiff',[plot_name3, '.png'],'-r 72');
48    %print(gcf,'-dpdf','Curvature Map.pdf','-r 150')

```

```

1  %print(gcf,'-depsc2','Curvature Map.eps','-r 150')
2  %print (gcf,'-depsc2','filename2 Curvature Map.eps','-r 150')
3
4  print(gcf,'-dpdf',[plot_name, '.pdf'],'-r 300') print(gcf,'-depsc2',[plot_name,
5  '.eps'],'-r 300') print(gcf,'-dtiff',[plot_name, '.png'],'-r 72')
6  % output the k values per slice to a file
7
8  %if (file_name2 ~= 0)  fout =
9  fopen((file_name2), 'w');  for slice =
10  1: num_slices  fprintf(fout, '%d',
11  slice);  k = k_map(slice, :);  for
12  t = 1: length(k)  fprintf(fout,
13  ',%f', k(t));  end
14  fprintf(fout, '\n');
15  end  fclose(fout);
16  fout2 = fopen((file_name3), 'w');
17
18  end
19  function rFSDs = fEfourier(outline, iNoOfHarmonicsAnalyse, bNormaliseSizeState,
20  bNormaliseOrientationState)
21  % Forward elliptical Fourier transform - see Kuhl FP and Giardina CR %
22  "Elliptic Fourier features of a closed contour" Computer Graphics and %
23  Image Processing 18:236-258 1982 for theory.
24  % Returns a shape spectrum of input x,y data "outline" with %
25  iNoOfHarmonicsAnalyse elements.
26  % The output FSDs will be normalised for location, size and orientation
27  % if bNormaliseSizeState and bNormaliseOrientationState are TRUE
28
29  % Pre-calculate some constant arrays
30  % n * 2 * pi
31  % n^2 * 2* pi^2
32  % where n is the number of harmonics to be used in the analysis rTwoNPi =
33  (1:1:iNoOfHarmonicsAnalyse)* 2 * pi; rTwoNSqPiSq = (1:1:iNoOfHarmonicsAnalyse) .*
34  (1:1:iNoOfHarmonicsAnalyse)* 2 * pi * pi;
35
36  iNoOfPoints = size(outline,1) - 1; % hence there is 1 more data point in outline than iNoOfPoints
37  rDeltaX = zeros(iNoOfPoints+1,1); % pre-allocate some arrays rDeltaY = zeros(iNoOfPoints+1,1);
38  rDeltaT = zeros(iNoOfPoints+1,1);
39
40  for iCount = 2 : iNoOfPoints + 1
41  rDeltaX(iCount-1) = outline(iCount,1) - outline(iCount-1,1);
42  rDeltaY(iCount-1) = outline(iCount,2) - outline(iCount-1,2); end
43
44  % Calculate 'time' differences from point to point - actually distances, but we are
45  % carrying on the fiction of a point running around the closed figure at constant speed.
46  % We are analysing the projections on to the x and y axes of this point's path around the figure for
47  iCount = 1 : iNoOfPoints

```

```

1   rDeltaT(iCount) = sqrt((rDeltaX(iCount)^2) + (rDeltaY(iCount)^2));
2   end check = (rDeltaT ~= 0); % remove zeros from rDeltaT, rDeltaX...
3   rDeltaT = rDeltaT(check); rDeltaX =
4   rDeltaX(check); rDeltaY =
5   rDeltaY(check);
6
7   iNoOfPoints = size(rDeltaT,1) - 1; % we have removed duplicate points %
8   now sum the incremental times to get the time at any point rTime(1) = 0;
9   for iCount = 2 : iNoOfPoints + 1
10    rTime(iCount) = rTime(iCount - 1) + rDeltaT(iCount-1); end
11
12  rPeriod = rTime(iNoOfPoints+1); % rPeriod defined for readability
13  % calculate the A-sub-0 coefficient rSum1 =
14  0;
15  for iP = 2 : iNoOfPoints + 1
16    rSum2 = 0; rSum3 = 0;
17    rInnerDiff = 0;
18    % calculate the partial sums - these are 0 for iCount = 1
19    if iP > 1 for ij = 2 : iP-1
20      rSum2 = rSum2 + rDeltaX(ij-1);
21    rSum3 = rSum3 + rDeltaT(ij-1); end
22    rInnerDiff = rSum2 - ((rDeltaX(iP-1) / rDeltaT(iP-1)) * rSum3); end
23    rIncr1 = ((rDeltaX(iP-1) / (2*rDeltaT(iP-1)))*(rTime(iP)^2-rTime(iP-1)^2) +
24    rInnerDiff*(rTime(iP)rTime(iP-1))); rSum1 = rSum1 + rIncr1; end
25    rFSDs(1,1) = ((1 / rPeriod) * rSum1) + outline(1,1); % store A-sub-0 in output FSDs array - this array
26    will be 4 x iNoOfHarmonicsAnalyse % calculate the a-sub-n coefficients
27  for iHNo = 2 : iNoOfHarmonicsAnalyse
28    rSum1 = 0; for iP = 1 : iNoOfPoints
29      rIncr1 = (rDeltaX(iP) / rDeltaT(iP))*((cos(rTwoNPi(iHNo-1)*rTime(iP+1)/rPeriod) -
30    cos(rTwoNPi(iHNo-1)*rTime(iP)/rPeriod)));
31      rSum1 = rSum1 + rIncr1;
32    end
33    rFSDs(1,iHNo) = (rPeriod / rTwoNSqPiSq(iHNo-1)) * rSum1; end %
34    "foriHNo = 1 :..."
35
36  rFSDs(2,1) = 0; % there is no 0th order sine coefficient
37  % calculate the b-sub-n coefficients
38  for iHNo = 2 : iNoOfHarmonicsAnalyse
39    rSum1 = 0; for iP = 1 : iNoOfPoints
40      rIncr1 = (rDeltaX(iP) / rDeltaT(iP))*((sin(rTwoNPi(iHNo-1)*rTime(iP+1)/rPeriod) -
41    sin(rTwoNPi(iHNo-1)*rTime(iP)/rPeriod)));
42      rSum1 = rSum1 + rIncr1; end
43      rFSDs(2,iHNo) = (rPeriod / rTwoNSqPiSq(iHNo-1)) * rSum1;
44  end % "foriHNo = 1 :..." % calculate the C-sub-0 coefficient
45  rSum1 = 0;
46  for iP = 2 : iNoOfPoints + 1
47    rSum2 = 0; rSum3 = 0;
48    rInnerDiff = 0;

```

```

1   % calculate the partial sums - these are 0 for iCount = 1
2   if iP > 1     for iJ = 2 : iP-1
3       rSum2 = rSum2 + rDeltaY(iJ-1);
4   rSum3 = rSum3 + rDeltaT(iJ-1);     end
5       rInnerDiff = rSum2 - ((rDeltaY(iP-1) / rDeltaT(iP-1)) * rSum3);     end
6       rIncr1 = ((rDeltaY(iP-1) / (2*rDeltaT(iP-1)))*(rTime(iP)^2-rTime(iP-1)^2) +
7   rInnerDiff*(rTime(iP)rTime(iP-1)));   rSum1 = rSum1 + rIncr1; end
8   rFSDs(3,1) = ((1 / rPeriod) * rSum1) + outline(1,2); % store C-sub-0 in output FSDs array - this array
9   will be 4 x iNoOfHarmonicsAnalyse
10
11  % calculate the C-sub-n coefficients
12  for iHNo = 2 : iNoOfHarmonicsAnalyse
13  rSum1 = 0;   for iP = 1 : iNoOfPoints
14      rIncr1 = (rDeltaY(iP) / rDeltaT(iP))*((cos(rTwoNPNi(iHNo-1)*rTime(iP+1)/rPeriod) -
15  cos(rTwoNPNi(iHNo-1)*rTime(iP)/rPeriod)));
16      rSum1 = rSum1 + rIncr1;
17  end
18      rFSDs(3,iHNo) = (rPeriod / rTwoNSqPiSq(iHNo-1)) * rSum1; end %
19  "foriHNo = 1 :..."
20
21  rFSDs(4,1) = 0; % there is no 0th order sine coefficient
22
23  % calculate the D-sub-n coefficients
24  for iHNo = 2 : iNoOfHarmonicsAnalyse
25  rSum1 = 0;   for iP = 1 : iNoOfPoints
26      rIncr1 = (rDeltaY(iP) / rDeltaT(iP))*((sin(rTwoNPNi(iHNo-1)*rTime(iP+1)/rPeriod) -
27  sin(rTwoNPNi(iHNo-1)*rTime(iP)/rPeriod)));
28      rSum1 = rSum1 + rIncr1;
29  end
30      rFSDs(4,iHNo) = (rPeriod / rTwoNSqPiSq(iHNo-1)) * rSum1; end %
31  "foriHNo = 1 :..."
32
33  % the non-normalised coefficients are now in rFSDs % if we want the
34  normalised ones, this is where it happens if (bNormaliseSizeState == 1) ||
35  (bNormaliseOrientationState == 1)   % rTheta1 is the angle through
36  which the starting position of the first
37  % harmonic phasor must be rotated to be aligned with the major axis of
38  % the first harmonic ellipse   rFSDsTemp
39  = rFSDs;
40      rTheta1 = 0.5 * atan(2 * (rFSDsTemp(1,2) * rFSDsTemp(2,2) + rFSDsTemp(3,2) * rFSDsTemp(4,2)) /
41  ...
42      (rFSDsTemp(1,2)^2 + rFSDsTemp(3,2)^2 - rFSDsTemp(2,2)^2 - rFSDsTemp(4,2)^2));
43      % calculate the partially normalised coefficients - normalised for
44      % starting point
45      for iHNo = 1 : iNoOfHarmonicsAnalyse
46          rStarFSDs(1,iHNo) = cos((iHNo-1) * rTheta1) * rFSDsTemp(1,iHNo) + sin((iHNo-1) * rTheta1) *
47  rFSDsTemp(2,iHNo);
48          rStarFSDs(2,iHNo) = -sin((iHNo-1) * rTheta1) * rFSDsTemp(1,iHNo) + cos((iHNo-1) * rTheta1)

```

```

1 * rFSDsTemp(2,iHNo);
2     rStarFSDs(3,iHNo) = cos((iHNo-1) * rTheta1) * rFSDsTemp(3,iHNo) + sin((iHNo-1) * rTheta1) *
3 rFSDsTemp(4,iHNo);
4     rStarFSDs(4,iHNo) = -sin((iHNo-1) * rTheta1) * rFSDsTemp(3,iHNo) + cos((iHNo-1) * rTheta1)
5 * rFSDsTemp(4,iHNo);
6     end % for iHNo = 1 : iNoOfHarmonicsAnalyse
7
8     rPsi1 = atan(rStarFSDs(3,2) / rStarFSDs(1,2));
9     rSemiMajor = sqrt(rStarFSDs(1,2)^2 + rStarFSDs(3,2)^2); % find the semi-major axis of the first
10 ellipse
11
12     rFSDs(:, :) = rStarFSDs(:, :) ./ rSemiMajor; % if we haven't asked for normalisation of orientation,
13 % return the coefficients normalised for starting point and size     if bNormaliseOrientationState
14 == 1
15     % now find the orientation normalised values - return them in rFSDs
16 for iHNo = 1 : iNoOfHarmonicsAnalyse
17     rFSDsTemp(1,iHNo) = (cos(rPsi1) * rStarFSDs(1,iHNo) + sin(rPsi1) * rStarFSDs(3,iHNo)) /
18 rSemiMajor;
19     rFSDsTemp(2,iHNo) = (cos(rPsi1) * rStarFSDs(2,iHNo) + sin(rPsi1) * rStarFSDs(4,iHNo)) /
20 rSemiMajor;
21     rFSDsTemp(3,iHNo) = (-sin(rPsi1) * rStarFSDs(1,iHNo) + cos(rPsi1) * rStarFSDs(3,iHNo)) /
22 rSemiMajor;
23     rFSDsTemp(4,iHNo) = (-sin(rPsi1) * rStarFSDs(2,iHNo) + cos(rPsi1) * rStarFSDs(4,iHNo)) /
24 rSemiMajor;
25     end % for iHNo = 1 : iNoOfHarmonicsAnalyse     rFSDs =
26 rFSDsTemp; % return fully normlised coefficients     end
27 end % if (bNormaliseSizeState == 1) || (bNormaliseOrientationState == 1)
28
29 return
30
31 function outln = rFourier( rFSDs, iNoOfHarmonicsReconstruct,iNoOfPointsReconstruct)
32 % Reverse elliptical Fourier transform on the input Fourier series
33 % rFSDs generated by rFourier.m. This reconstructs an approximation to the original outline figure
34 % using the specified number of harmonics and data points. See Kuhl FP and Giardina CR %
35 "Elliptical Fourier features of a closed contour" Computer Graphics and % Image Processing
36 18:236-258 1982 for theory and details.
37
38 iStartHarmonic = 2; % start at 2 - No.1 is just an offset and is added in later (lines 17 & 27)
39 ReconnedOutline = 0; % reconstruct the
40 x-projection for iTime =
41 1:iNoOfPointsReconstruct
42     rSum = 0.0;
43     for iHNo = iStartHarmonic:iNoOfHarmonicsReconstruct     rSum = rSum + (rFSDs(1,iHNo)
44 * cos(2*(iHNo-1)*pi*iTime / iNoOfPointsReconstruct) + ...
45     rFSDs(2,iHNo) * sin(2*(iHNo-1)*pi*iTime / iNoOfPointsReconstruct));
46     end % for iHNo = 1 : iNoOfHarmonicsReconstruct     ReconnedOutline(iTime,1)
47 = rFSDs(1,1) + rSum; end % for iTime = 1 : iNoOfPointsReconstruct
48

```

```

1  % reconstruct the y-projection for iTime =
2  1:iNoOfPointsReconstruct
3      rSum = 0.0;
4      for iHNo = iStartHarmonic:iNoOfHarmonicsReconstruct      rSum = rSum + (rFSDs(3,iHNo) *
5  cos(2*(iHNo-1)*pi*iTime / iNoOfPointsReconstruct) + ...
6      rFSDs(4,iHNo) * sin(2*(iHNo-1)*pi*iTime / iNoOfPointsReconstruct));
7      end % for iHNo = 1 : iNoOfHarmonicsReconstruct
8  ReconnedOutline(iTime,2) = rFSDs(3,1) + rSum; end % for
9  iTime = 1 : iNoOfPointsReconstruct outln =
10 ReconnedOutline;
11
12 return
13
14 function k_coeff = calc_k_coefficient(x, y)
15
16     x_diff = circular_diff(x, 1);   x_diff2 =
17     circular_diff(x_diff, 1);   y_diff =
18     circular_diff(y, 1);
19     y_diff2 = circular_diff(y_diff, 1);
20
21     k_coeff = zeros(1, length(x_diff));   for t =
22     1: length(x_diff)
23         numerator = x_diff(t) * y_diff2(t) - y_diff(t) * x_diff2(t);
24         denominator = (x_diff(t)^2 + y_diff(t)^2)^(3/2);   k_coeff(t) =
25         numerator / denominator;   end
26
27     return
28     % do a simple linear difference differentiation on circular data
29     function yy = circular_diff(xx, interval) yy = xx; for i = 1: length(xx)   if
30     (i == 1)
31         yy(i) = (xx(i + 1) - xx(end)) / (2 * interval);
32     continue   end
33     if (i == length(xx))
34         yy(i) = (xx(1) - xx(i - 1)) / (2 * interval);
35     continue   end
36     yy(i) = (xx(i + 1) - xx(i - 1)) / (2 * interval); end
37     return
38
39

```

1 1.8 S10. MATLAB code for size standardisation of thickness maps

```
2 function standardise_gridto1
3 %This function will standardise a matrix so that all values fall between 0
4 %and 1. It can also be used to standardise values according to the matrices
5 %median values by uncommenting the appropriate commands
6 % first get a folder from the user
7 folder_name = uigetdir('','Choose the folder that contains the landmark coordinates');
8 if folder_name == 0
9     error('No folder selected');
10 end
11 % make a series of folders for your results to go into
12 file_list = dir(fullfile(folder_name, '*.csv'));
13 if isempty(file_list)
14     error('No .csv files found in folder')
15 end
16 if ~exist([folder_name '\normgrids0_1\'],'dir')
17     mkdir([folder_name '\normgrids0_1\'])
18 end
19 %if ~exist([folder_name '\normgridstomedian\'],'dir')
20 %mkdir([folder_name '\normgridstomedian\'])
21 %end
22 if ~exist([folder_name '\norm_heatmap0_1\'],'dir')
23     mkdir([folder_name '\norm_heatmap0_1\'])
24 end
25 if ~exist([folder_name '\norm_heatmap0_1b\'],'dir')
26     mkdir([folder_name '\norm_heatmap0_1b\'])
27 end
28 file_number = 1:length(file_list)
29
30     file_name = [folder_name '/' file_list(file_number).name];
31     [pathstr, name, ext] = fileparts(file_name);
32
33 %This standardises all the values to the overall median value of the matrix
34 for file_number = 1:length(file_list)
35     file_name = [folder_name '/' file_list(file_number).name];
36     grid = csvread(file_name);
37     ncols = size(grid,2)
38     grid2 = grid([1:120],[1:ncols])
39     gridmax = max(grid2(:))
40     gridmin = min(grid2(:))
41     standmin = (grid2-gridmin)
42     stan0_1 = standmin./(gridmax-gridmin)
43     %medianvalue = median(grid2(:))
44     %standardised_grid = 1./grid2
45     %standardised_grid2=grid2-medianvalue
46     heatmap_name = [folder_name '\norm_heatmap0_1\' file_list(file_number).name(1:end-4)
47 'stand_heatmap'];
48     heatmap_name2 = [folder_name '\norm_heatmap0_1b\' file_list(file_number).name(1:end-4)
49 'stand_heatmap2'];
```

```

1     csvwrite([folder_name '\normgrids0_1\' file_list(file_number).name(1:end-4) 'normgrid.csv'],
2     stan0_1);
3     % csvwrite([folder_name '\normgridstomedian\' file_list(file_number).name(1:end-4)
4     'normgrid2.csv'], standardised_grid2);
5     graph_bone_name = [file_list(file_number).name(1:end-4)];
6     figure(1)
7     clf('reset');
8     set(gcf, 'Color', 'w');
9     set(gcf, 'Units', 'pixels');
10    set(gcf, 'Position', [50, 50, 1000, 1000]);
11    imagesc(stan0_1)
12    %plot_name = heatmap_name
13    set(gcf, 'PaperType', '<custom>');
14    set(gcf, 'Units', 'inches');
15    set(gcf, 'PaperUnits', 'inches');
16    position = get(gcf, 'Position');
17    set(gcf, 'PaperPosition', [0,0,position(3:4)]);
18    set(gcf, 'PaperSize', position(3:4));
19    %axes1 = axes('Parent', figure1, ...
20
21    plot_name = [heatmap_name];
22    colormap(jet(256));
23    colorbar('EastOutside');
24    xlabel('Bone Position');
25    ylabel({'Slice number.', 'Lower numbers are more proximal'});
26    %MODIFY THIS TITLE AS SEEN FIT
27    title(['Standardised cortical thickness of ' file_list(file_number).name(1:13) ' humerus']);
28    print(gcf, '-dtiff', [plot_name, '.png'], '-r 72')
29
30    figure(2)
31    clf('reset');
32    set(gcf, 'Color', 'w');
33    set(gcf, 'Units', 'pixels');
34    set(gcf, 'Position', [50, 50, 1000, 1000]);
35
36    imagesc(stan0_1)
37    set(gcf, 'PaperType', '<custom>');
38    set(gcf, 'Units', 'inches');
39    set(gcf, 'PaperUnits', 'inches');
40    position = get(gcf, 'Position');
41    set(gcf, 'PaperPosition', [0,0,position(3:4)]);
42    set(gcf, 'PaperSize', position(3:4));
43    plot_name2 = [heatmap_name2];
44    colormap(jet(256));
45    print(gcf, '-dtiff', [plot_name2, '.png'], '-r 72')
46    end
47
48
49
50

```

1 **1.9 S11 MATLAB code for combining matrices and running PCA.**

```
2 function combine_run_pca
3 % first get a folder from the user
4 folder_name = uigetdir('', 'Choose the folder that contains the landmark
5 coordinates');
6 if folder_name == 0
7     error('No folder selected');
8 end
9
10 file_list = dir(fullfile(folder_name, '*.csv'));
11 if isempty(file_list)
12     error('No .csv files found in folder')
13 end
14 for file_number = 1:length(file_list)
15
16     file_name = [folder_name '/' file_list(file_number).name];
17     data1 = csvread(file_name);
18     data1 = data1(1:120,1:360)
19     data1a=reshape(data1,43200,1)
20
21     combineda(file_number,:) = horzcat(data1a);
22
23 end
24 %Runs PCA and exports csv files of scores.Replace *NAME* with an
25 appropriate prefix.
26 [coeff,score,latent,tsquared,explained,mu] = pca(combineda)
27 csvwrite('*NAME*combinedvaluesforpca.csv',combineda)
28 csvwrite('*NAME*_scores.csv',score)
29 csvwrite('*NAME*_coeff.csv',coeff)
30 csvwrite('*NAME*_explained.csv',explained)
31
32 end
33
34
35
```